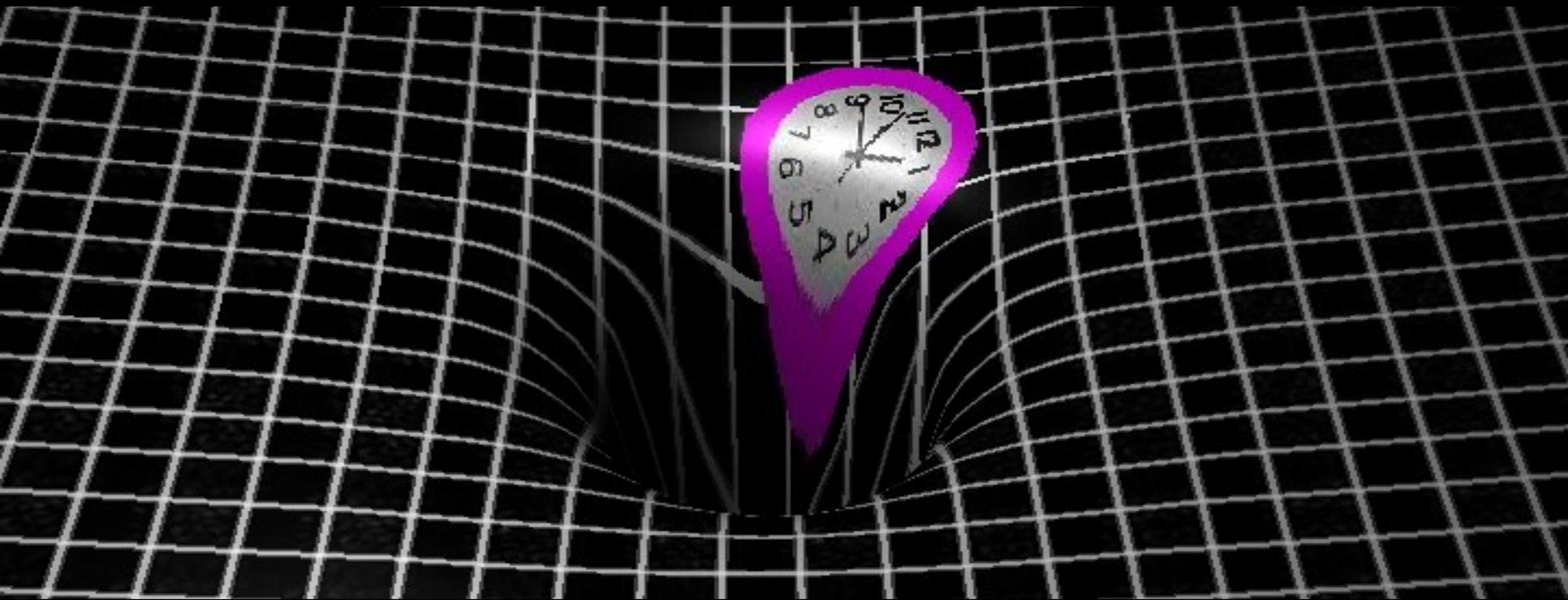


Tests of Lorentz Symmetry with STE-QUEST



Jay D. Tasson

Carleton College

outline

- Lorentz invariance
 - meaning
 - violation
 - motivation for testing
 - test framework
- clock tests
 - theoretical analysis
 - STE-QUEST sensitivity
- WEP tests
 - theoretical analysis
 - STE-QUEST sensitivity

Based on STE-QUEST analysis
with Brett Altschul & Quentin Bailey

relativity

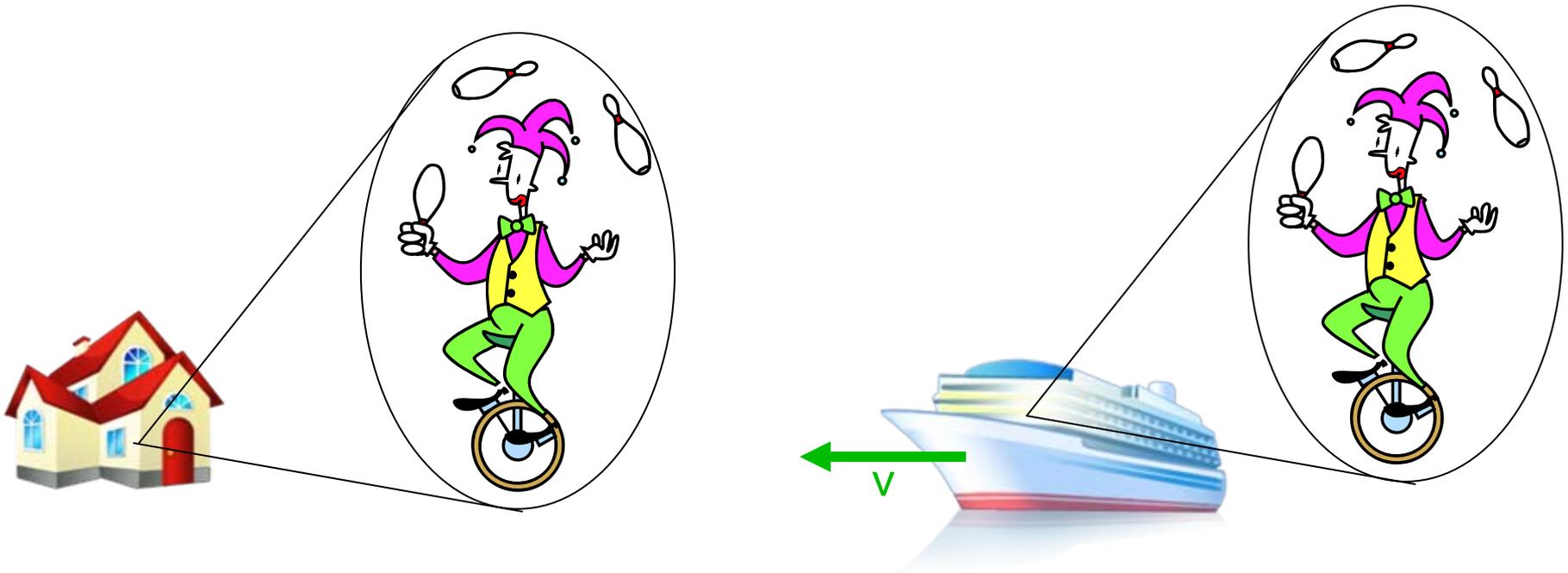
- physical results are independent of the velocity of the experiment and the **direction** it points



- juggling facing the other way still works
- rotation invariance – results are independent of the direction the experiment points

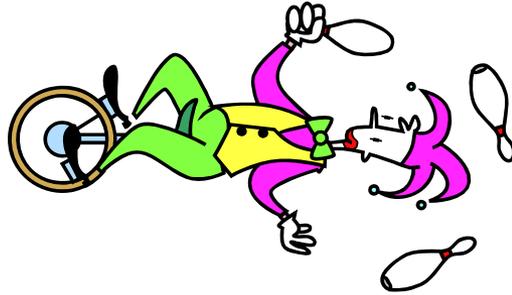
relativity

- physical results are independent of the **velocity** of the experiment and the direction it points



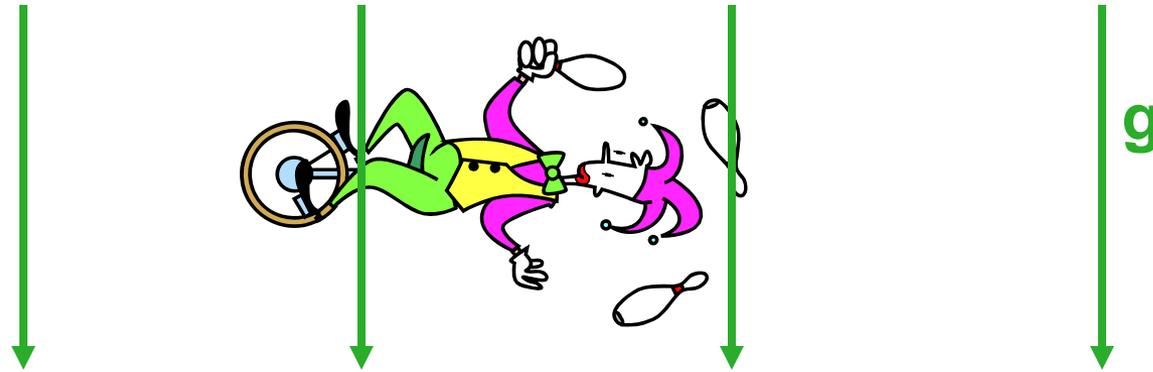
- juggling on ship moving at constant velocity without rocking still works
- boost invariance – results are independent of the constant velocity of the experiment

what does relativity violation look like?



- juggling while lying on your back is different

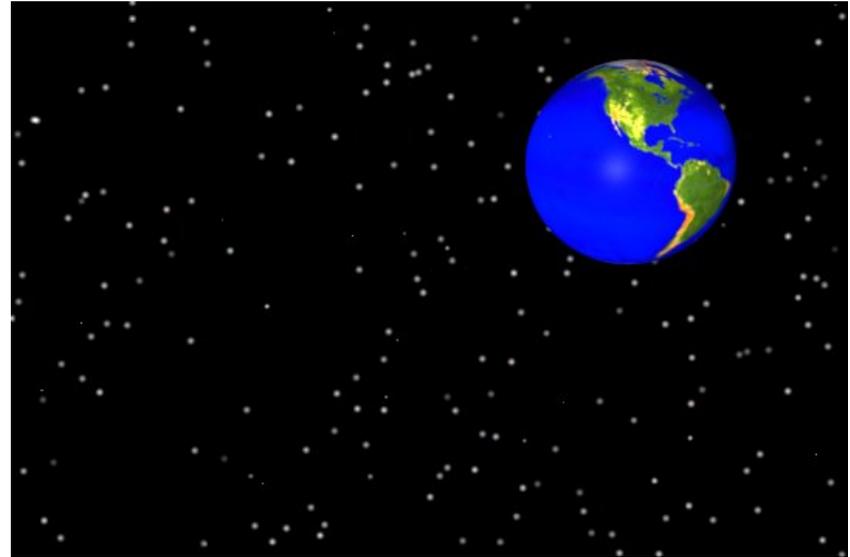
what does relativity violation look like?



- juggling while lying on your back is different
- apparent relativity violation
- resolution: Earth is part of experiment. It should be turned with the juggler.

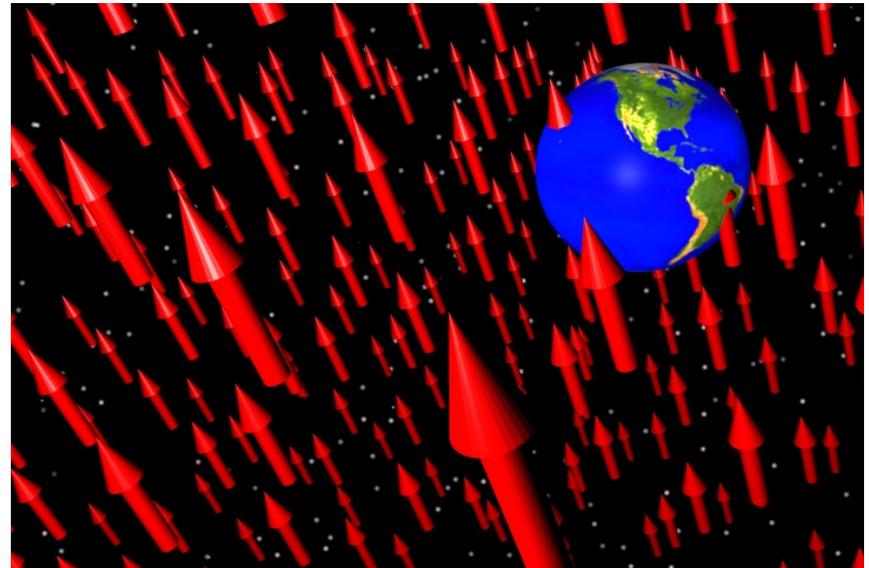
fundamental relativity violation

- relativity

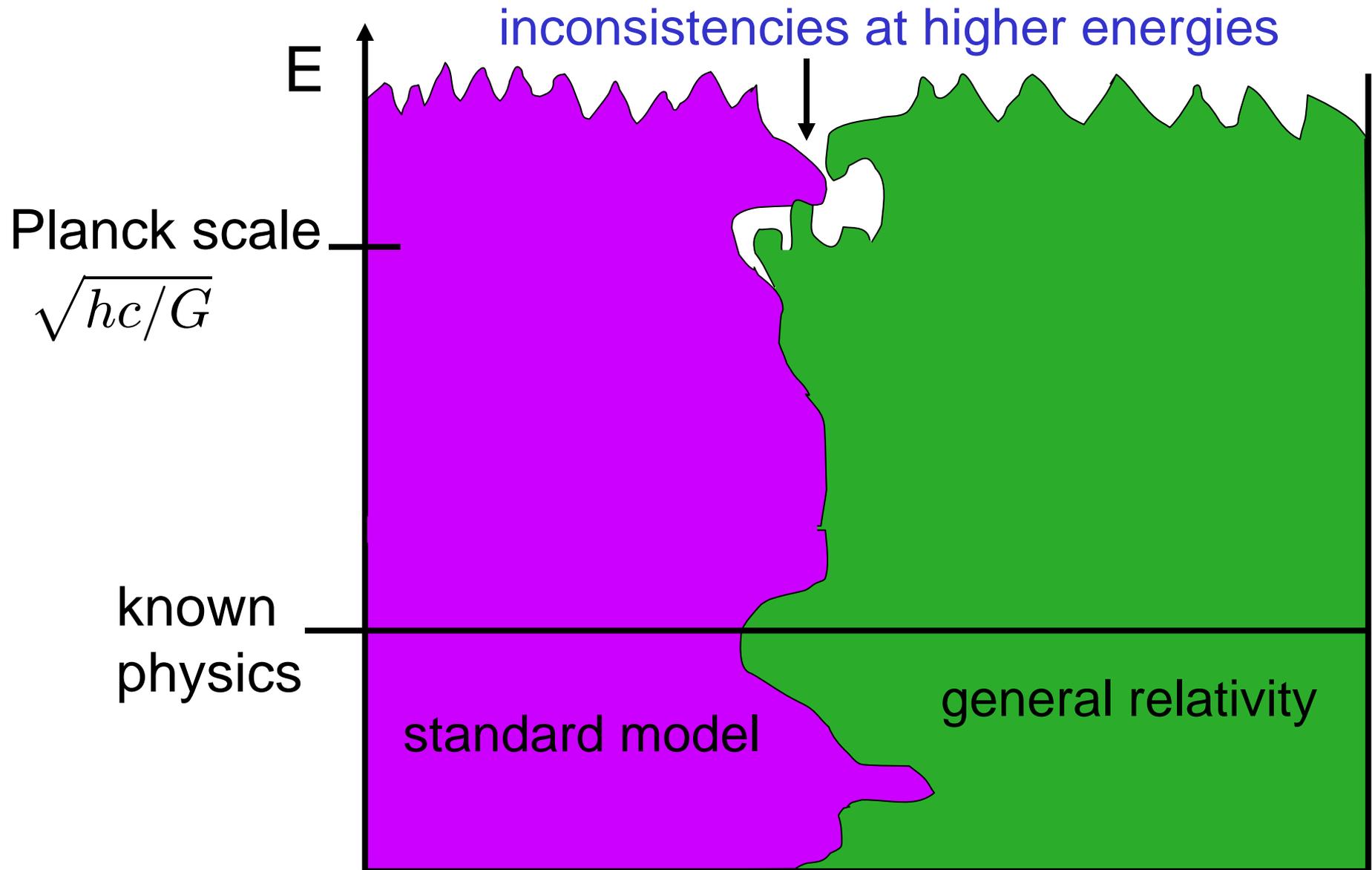


- relativity violation

(in general, there can be time components and higher rank tensors, but they're hard to draw)



motivation



underlying theory at Planck scale

options for probing experimentally

- galaxy-sized accelerator

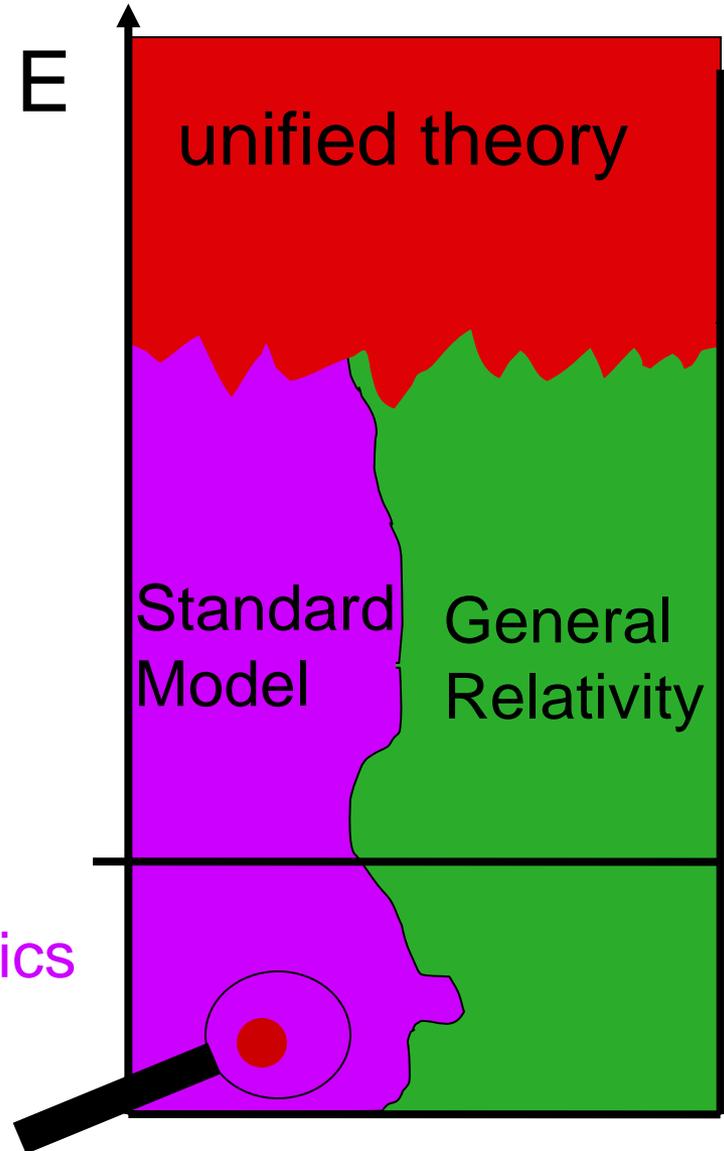


- suppressed effects in sensitive experiments

Lorentz violation

- can arise in theories of new physics
- difficult to mimic with conventional effects

STE-Quest can probe Planck-scale physics!



general test framework

Gravitational Standard-Model Extension (SME):

effective theory which contains

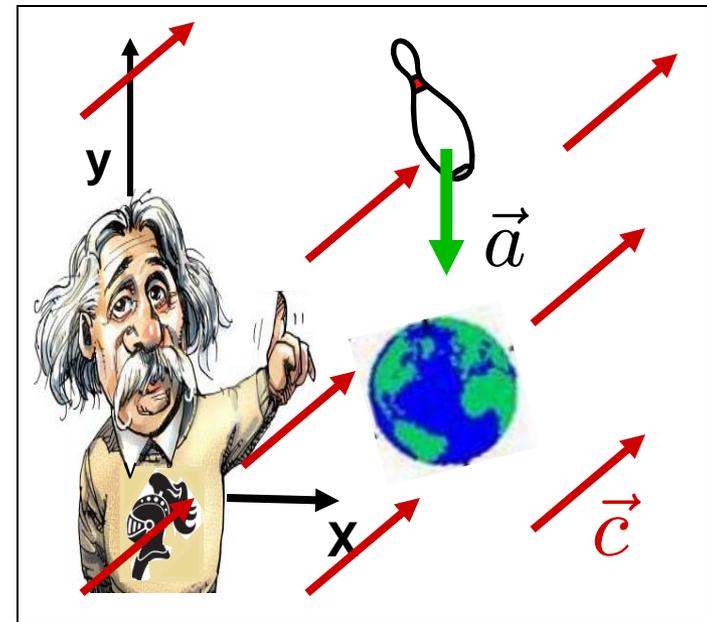
- General Relativity
- the Standard Model
- all Lorentz-violating terms
- broad search for LV

Lorentz-violating terms

- constructed from known physics (fields, particles, interactions)
- parameterized by coefficients
- sample

$$\vec{a} = \vec{g} + \vec{c}(\vec{c} \cdot \vec{g})$$

different for various particles



gravitational SME

- effective field theory
- expansion of Lagrangian about known physics

$$L_{\text{SME}} = \underbrace{L_{\text{SM}} + L_{\text{GR}}}_{\text{known physics}} + \underbrace{L_{\text{LV}} + L_{\text{LV}} + \dots}_{\text{Lorentz violating corrections}}$$

known physics

Lorentz violating corrections

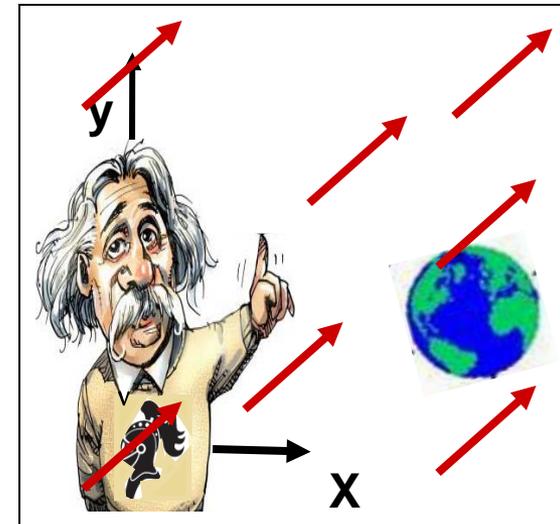
$$L_{\text{LV}} = L_{\text{fermion}} + L_{\text{photon}} + L_{\text{pure gravity}} + \dots$$

- nongravitational minimal QED limit

$$L_{\text{fermion}} = \frac{1}{2} i \bar{\psi} (\gamma^\mu - c^\mu{}_\nu \gamma^\nu - e^\mu \dots) \overleftrightarrow{D}_\mu \psi - \bar{\psi} (m + a_\mu \gamma^\mu + b_\mu \gamma_5 \gamma^\mu + \dots) \psi$$

coefficients for Lorentz violation

- particle-species dependent
- to first approximation, constant in Sun-centered frame



PPN vs. SME

framework	PPN	SME
parameterizes deviations from:	General Relativity (including some Lorentz violation)	exact Lorentz invariance (including some corrections to GR)
expansion about:	GR metric	GR + standard model Lagrangian
GR corrections?	Yes	Yes, different ones!
matter sector /standard model corrections?	No	Yes

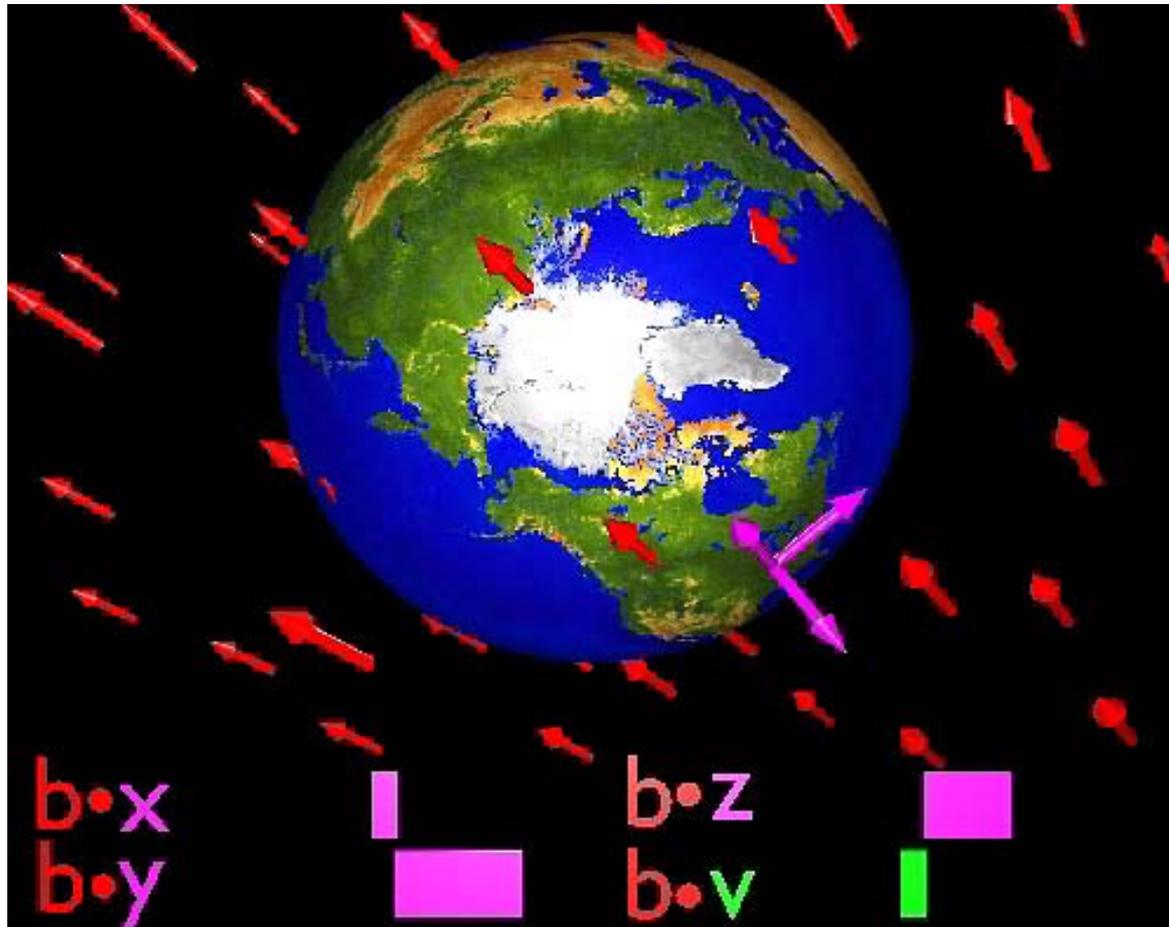
tests

- compare experiments pointing in different directions
- compare experiments traveling at different velocities
- SME
 - predictive
 - quantitative comparisons
- find
 - relativity violation
 - field of unknown origin eg. best existing bounds on spacetime torsion¹

1) Kostelecký, Russell, Tasson PRL '08

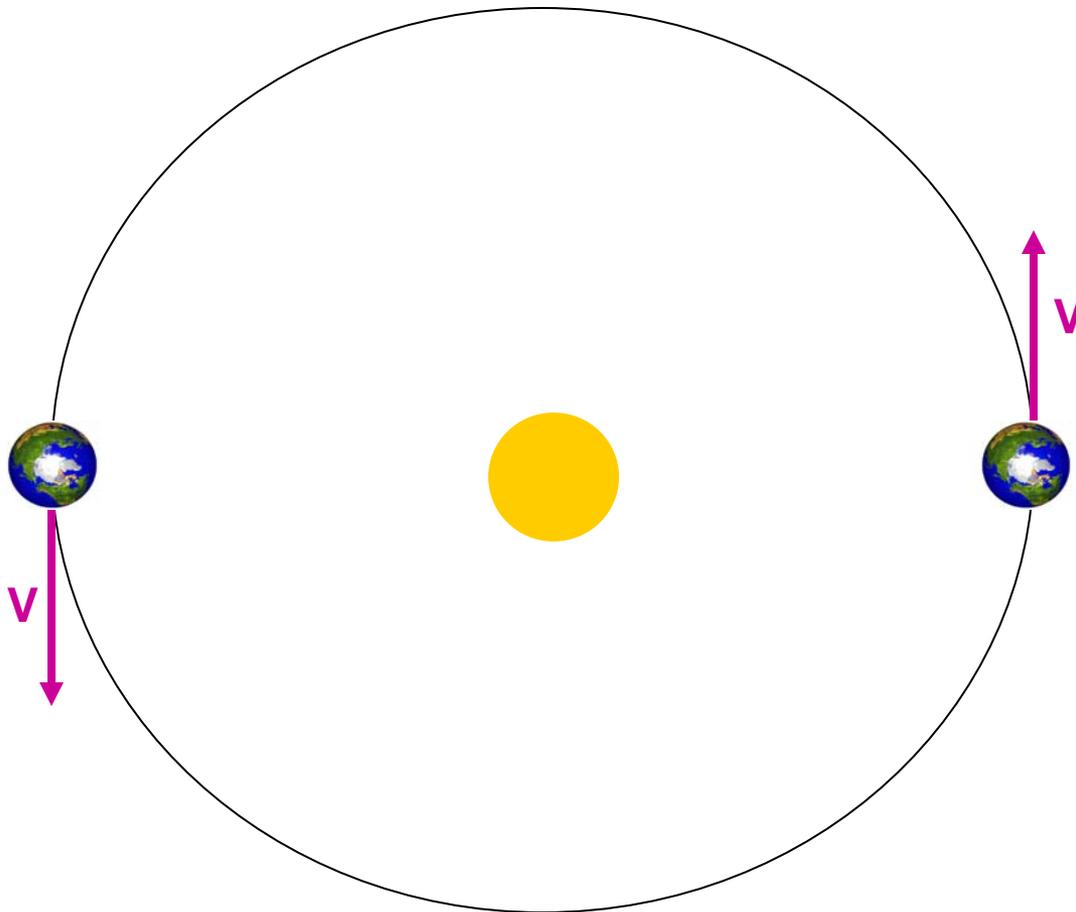
Earth rotation

- orientation & velocity of experiment constantly changes
- periodic at rotational (sidereal) period
- test relativity by comparing experimental results at an infinite number of orientations & velocities



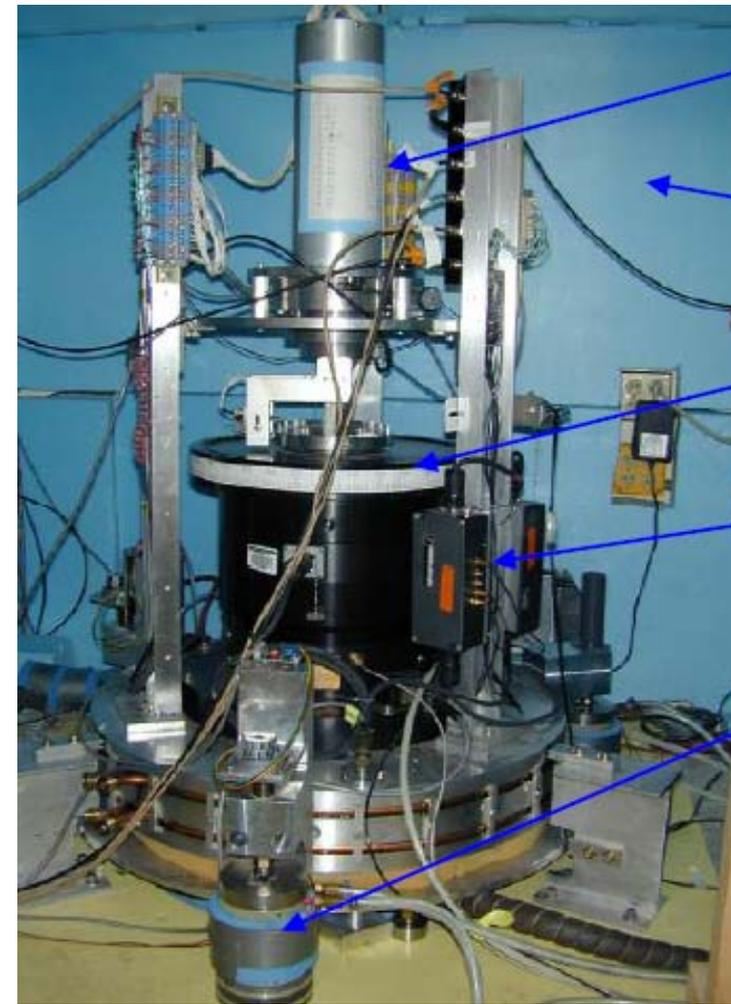
Earth revolution

- velocity of experiment constantly changes
- annual periodicity
- test relativity by comparing experimental results at an infinite number of velocities

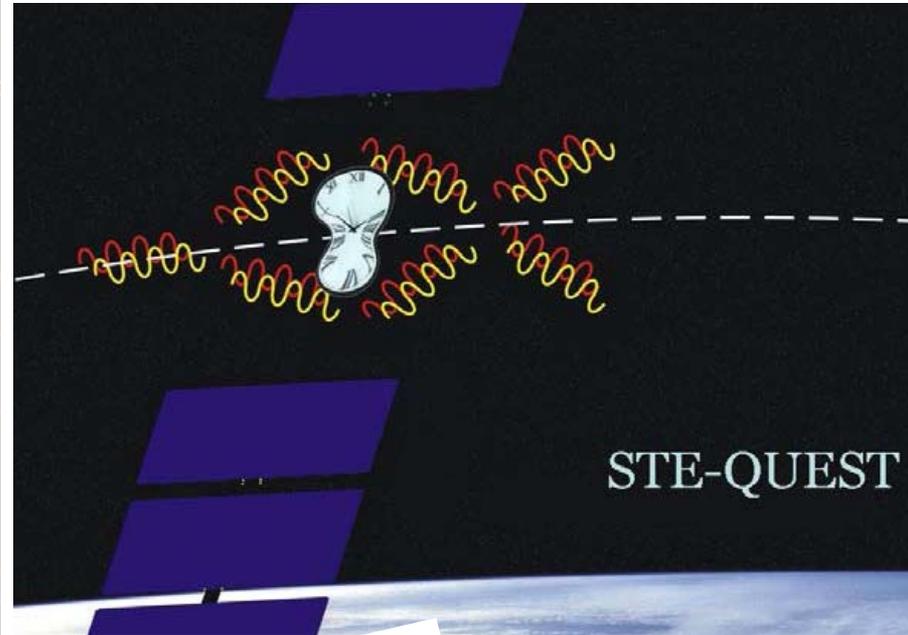
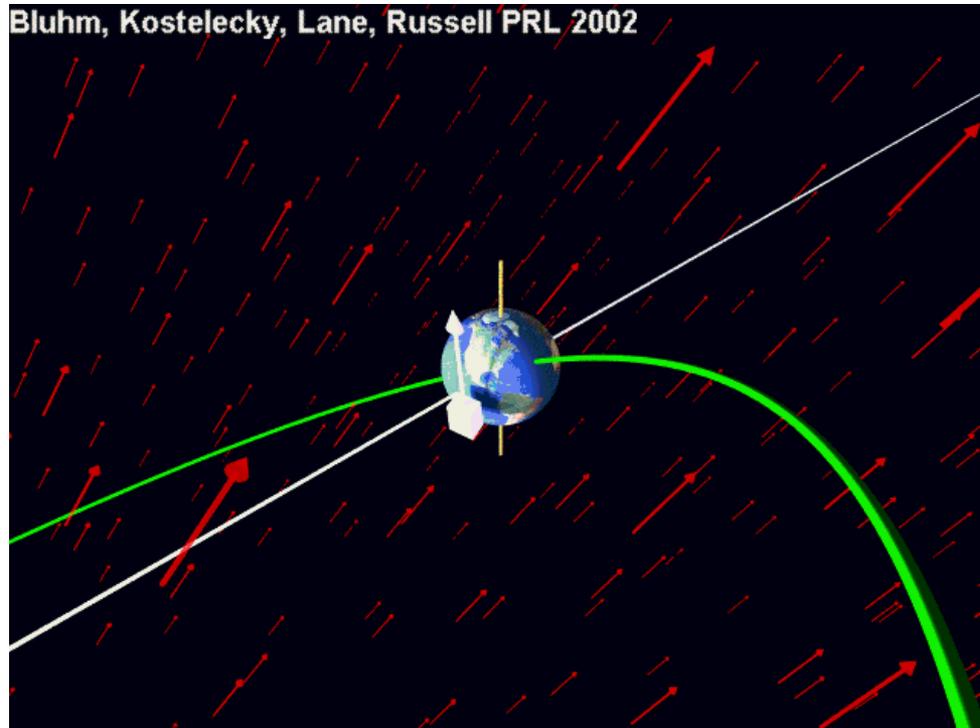


Turntable

- variation in direction about an axis different from Earth
- additional sensitivities
- systematics



Satellite



- rapidly sample large space of Lorentz frames, higher boost, chosen directions
- STE-QUEST variable orbit – additional independent sensitivities
- additional advantages in the context of gravitational tests

clock comparisons

$$L_{LV} = L_{\text{fermion}} + L_{\text{photon}} + L_{\text{pure gravity}} + \dots$$



tests:

- clock comparisons
- spin-polarized solids
- pulsar-timing observations
- particle traps
- neutrino oscillations
- muons

clock comparisons

$$L_{LV} = L_{\text{fermion}} + L_{\text{boson}}$$



tests:

- clock comparisons
- spin-polarized solids
- pulsar-timing observations
- particle traps
- neutrino oscillations
- muons

Much experimental/observational work:

IceCube Collaboration, R. Abbasi et al., *Phys. Rev. D* 82, 112003 (2010) ; MiniBooNE Collaboration, T. Katori; MINOS Collaboration, P. Adamson et al., *Phys. Rev. Lett.* 105, 151601 (2010); MINOS Collaboration, P. Adamson et al., *Phys. Rev. Lett.* 101, 151601 (2008); LSND Collaboration, L.B. Auerbach et al., *Phys. Rev. D* 72, 076004 (2005) ; BNL *g-2* collaboration, G.W. Bennett et al., *Phys. Rev. Lett.* 100, 091602 (2008); V.W. Hughes et al., *Phys. Rev. Lett.* 87, 111804 (2001); BNL *g-2* collaboration, M. Deile et al.; H. Dehmelt et al., *Phys. Rev. Lett.* 83, 4694 (1999) ; R. Mittleman et al., *Phys. Rev. Lett.* 83, 2166 (1999); G. Gabrielse et al., *Phys. Rev. Lett.* 82, 3198 (1999). ; B. Heckel et al., *Phys. Rev. D* 78, 092006 (2008) ; B. Heckel et al., *Phys. Rev. Lett.* 97, 021603 (2006) ; L.-S. Hou et al., *Phys. Rev. Lett.* 90, 201101 (2003) PRL server; B. Heckel et al., web manuscript. C. Gemmel et al., *Phys. Rev. D* 82, 111901 (R) (2010) ; K. Tullney et al., ; J.M. Brown et al., *Phys. Rev. Lett.* 105, 151604 (2010) ; I. Altarev et al., *Phys. Rev. Lett.* 103, 081602 (2009) ; T.W. Kornack, G. Vasilakis, and M. Romalis, in *CPT and Lorentz Symmetry IV*, *op. cit.*, p.206; P. Wolf et al., *Phys. Rev. Lett.* 96, 060801 (2006) ; P. Wolf et al., ; P. Wolf et al., ; F. Cane et al., *Phys. Rev. Lett.* 93, 230801 (2004) ; D.F. Phillips et al., *Phys. Rev. D* 63, 111101 (2001) ; M.A. Humphrey et al., *Phys. Rev. A* 68, 063807 (2003) ; D. Bear et al., *Phys. Rev. Lett.* 85, 5038 (2000) ; R. Walsworth et al., *AIP Conf. Proc.* 539, 119 (2000) ; L.R. Hunter et al., in *CPT*

sensitivities with ordinary matter

Coefficient	Electron	Proton	Neutron				
				\tilde{d}_Z	10^{-19} GeV	–	–
\tilde{b}_X	10^{-31} GeV	10^{-31} GeV	10^{-32} GeV	\tilde{H}_{XT}	10^{-26} GeV	–	10^{-26} GeV
\tilde{b}_Y	10^{-31} GeV	10^{-31} GeV	10^{-32} GeV	\tilde{H}_{YT}	10^{-26} GeV	–	10^{-26} GeV
\tilde{b}_Z	10^{-29} GeV	–	–	\tilde{H}_{ZT}	10^{-26} GeV	–	10^{-27} GeV
\tilde{b}_T	10^{-26} GeV	–	10^{-26} GeV				
$\tilde{b}_J^*, (J = X, Y, Z)$	10^{-22} GeV	–	–	\tilde{g}_T	10^{-27} GeV	–	10^{-27} GeV
				\tilde{g}_c	10^{-26} GeV	–	10^{-27} GeV
\tilde{c}_-	10^{-18} GeV	10^{-24} GeV	10^{-28} GeV	\tilde{g}_Q	–	–	–
\tilde{c}_Q	10^{-17} GeV	10^{-21} GeV	10^{-10} GeV	\tilde{g}_-	–	–	–
\tilde{c}_X	10^{-19} GeV	10^{-25} GeV	10^{-28} GeV	$\tilde{g}_{TJ}, (J = X, Y, Z)$	–	–	–
\tilde{c}_Y	10^{-19} GeV	10^{-25} GeV	10^{-28} GeV	\tilde{g}_{XY}	10^{-17} GeV	–	–
\tilde{c}_Z	10^{-19} GeV	10^{-24} GeV	10^{-29} GeV	\tilde{g}_{YX}	10^{-17} GeV	–	–
\tilde{c}_{TX}	10^{-18} GeV	10^{-20} GeV	–	\tilde{g}_{ZX}	10^{-18} GeV	–	–
\tilde{c}_{TY}	10^{-18} GeV	10^{-20} GeV	–	\tilde{g}_{XZ}	10^{-17} GeV	–	–
\tilde{c}_{TZ}	10^{-20} GeV	10^{-20} GeV	–	\tilde{g}_{YZ}	10^{-17} GeV	–	–
\tilde{c}_{TT}	10^{-18} GeV	10^{-11} GeV	10^{-11} GeV	\tilde{g}_{ZY}	10^{-18} GeV	–	–
				\tilde{g}_{DX}	10^{-22} GeV	10^{-25} GeV	10^{-28} GeV
\tilde{d}_+	10^{-27} GeV	–	10^{-27} GeV	\tilde{g}_{DY}	10^{-22} GeV	10^{-25} GeV	10^{-28} GeV
\tilde{d}_-	10^{-26} GeV	–	10^{-26} GeV	\tilde{g}_{DZ}	10^{-22} GeV	–	–
\tilde{d}_Q	10^{-26} GeV	–	10^{-26} GeV				
\tilde{d}_{XY}	10^{-26} GeV	–	10^{-27} GeV				
\tilde{d}_{YZ}	10^{-26} GeV	–	10^{-26} GeV				
\tilde{d}_{ZX}	10^{-26} GeV	–	–				
\tilde{d}_X	10^{-22} GeV	10^{-25} GeV	10^{-28} GeV				
\tilde{d}_Y	10^{-22} GeV	10^{-25} GeV	10^{-28} GeV				

Data Tables for Lorentz and CPT violation
Kostelecký, Russell Rev. Mod. Phys '11
2013 edition arXiv:0801.0287v6

sensitivities with ordinary matter

Coefficient	Electron	Proton	Neutron
\tilde{b}_X	10^{-31} GeV	10^{-31} GeV	10^{-32} GeV
\tilde{b}_Y	10^{-31} GeV	10^{-31} GeV	10^{-32} GeV
\tilde{b}_Z	10^{-29} GeV		–
\tilde{b}_T	10^{-26} GeV		10^{-26} GeV
$\tilde{b}_J^*, (J = X, Y, Z)$	10^{-22} GeV	–	–

- 1st – ever measurements possible in STE-QUEST clock test
- numerous other competitive measurements
- 10^{-21} to 10^{-28} level sensitivities

\tilde{c}_{TZ}	10^{-20} GeV	10^{-20} GeV	–
\tilde{c}_{TT}	10^{-18} GeV	10^{-11} GeV	10^{-11} GeV
\tilde{d}_+	10^{-27} GeV		10^{-27} GeV
\tilde{d}_-	10^{-26} GeV		10^{-26} GeV
\tilde{d}_Q	10^{-26} GeV		10^{-26} GeV
\tilde{d}_{XY}	10^{-26} GeV		10^{-27} GeV
\tilde{d}_{YZ}	10^{-26} GeV		10^{-26} GeV
\tilde{d}_{ZX}	10^{-26} GeV		–
\tilde{d}_X	10^{-22} GeV	10^{-25} GeV	10^{-28} GeV
\tilde{d}_Y	10^{-22} GeV	10^{-25} GeV	10^{-28} GeV

\tilde{d}_Z	10^{-19} GeV		–
\tilde{H}_{XT}	10^{-26} GeV		10^{-26} GeV
\tilde{H}_{YT}	10^{-26} GeV		10^{-26} GeV
\tilde{H}_{ZT}	10^{-26} GeV		10^{-27} GeV
\tilde{g}_T	10^{-27} GeV	–	10^{-27} GeV
\tilde{g}_c	10^{-26} GeV		10^{-27} GeV
\tilde{g}_Q	–	–	–
\tilde{g}_-	–	–	–
$(J = X, Y, Z)$	–	–	–
\tilde{g}_{XY}	10^{-17} GeV		–
\tilde{g}_{YX}	10^{-17} GeV		–
\tilde{g}_{ZX}	10^{-18} GeV		–
\tilde{g}_{XZ}	10^{-17} GeV		–
\tilde{g}_{YZ}	10^{-17} GeV		–
\tilde{g}_{ZY}	10^{-18} GeV		–
\tilde{g}_{DX}	10^{-22} GeV	10^{-25} GeV	10^{-28} GeV
\tilde{g}_{DY}	10^{-22} GeV	10^{-25} GeV	10^{-28} GeV
\tilde{g}_{DZ}	10^{-22} GeV		–

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path to atomic experiment analysis

$\mathcal{L}_{\text{fermion}}$ expand to desired order in LV

↓ field redefinition

$\mathcal{L}'_{\text{fermion}}$

↓ Euler-Lagrange eq.

$H_{\text{Relativistic}} \longrightarrow$ relativistic quantum experiments

↓ Foldy-Wouthuysen expansion

$H_{\text{NonRel}} \longrightarrow$ non-relativistic quantum experiments

$$H_{\text{nonrel}} = \dots + b_j \sigma^j + m \left(-c_{jk} - \frac{1}{2} c_{00} \delta_{jk} \right) \frac{p_j p_k}{m^2} + \dots$$

↑
spin

periodic energy level perturbations!

periodic energy level perturbations

$$\langle F, m_F | H_{\text{nonrel}} | F, m_F \rangle = \dots + \frac{m_F}{F} \sin \chi \sum_w \beta_w b_Y^w \sin \omega t + \dots$$

total angular momentum

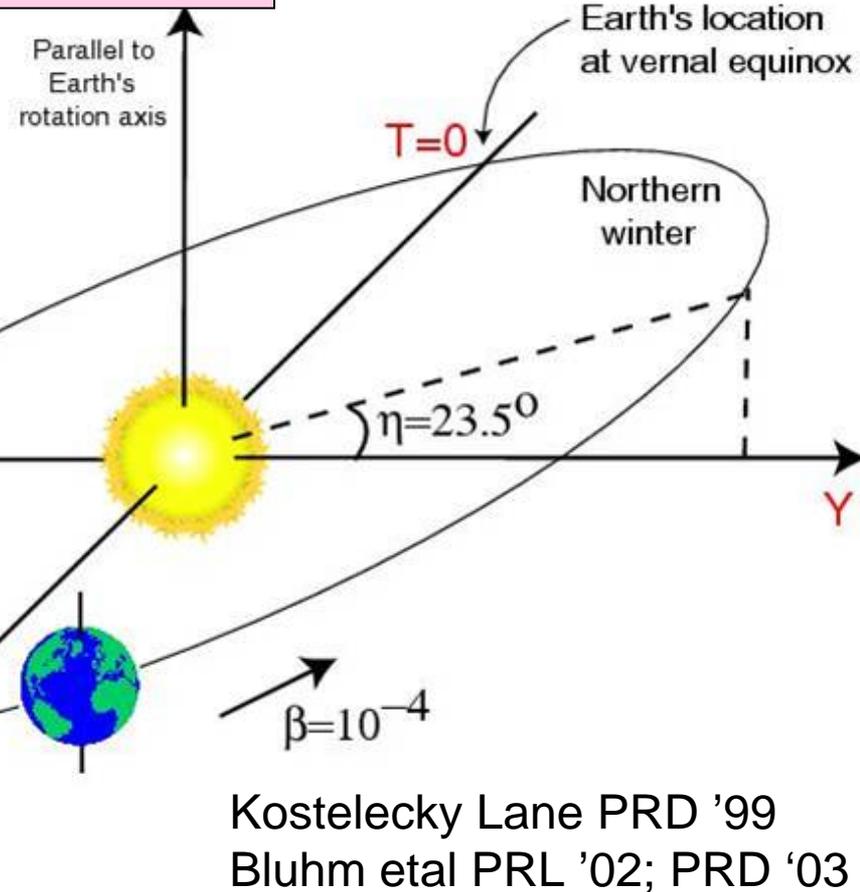
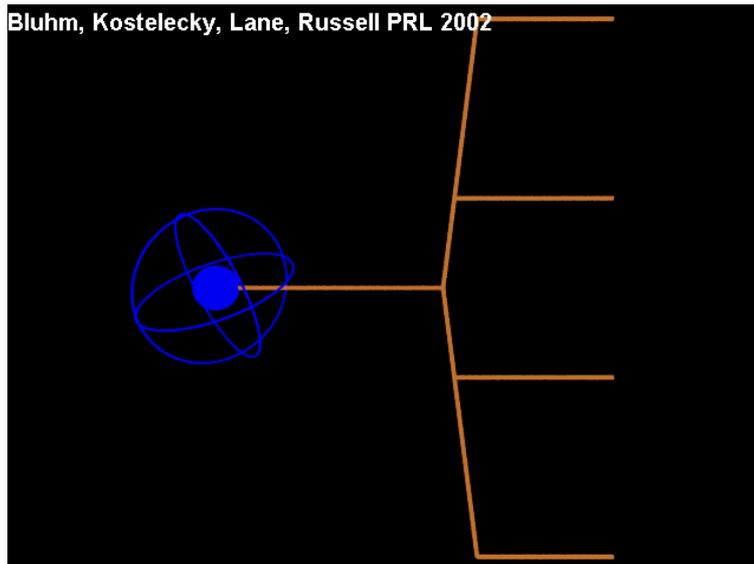
$$\beta_w := - \sum_{N=1}^{N_w} \langle [\sigma^3]_{w,N} \rangle$$

sum over N particles
of species w

rotation frequency

Schmidt model:
primary proton secondary
electron sensitivity

Bluhm, Kostelecky, Lane, Russell PRL 2002



Kostelecky Lane PRD '99
Bluhm etal PRL '02; PRD '03

sensitivities with ordinary matter

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\tilde{b}_Y	10^{-31} GeV	10^{-31} GeV	10^{-32} GeV
\tilde{b}_Z	10^{-29} GeV		–
\tilde{b}_T	10^{-26} GeV		10^{-26} GeV
$\tilde{b}_J^*, (J = X, Y, Z)$	10^{-22} GeV	–	–

- 1st – ever measurements possible in STE-QUEST clock test
- numerous other competitive measurements
- 10^{-21} to 10^{-28} level sensitivities
- 25 independent combinations

\tilde{d}_Z	10^{-19} GeV		–
\tilde{H}_{XT}	10^{-26} GeV		10^{-26} GeV
\tilde{H}_{YT}	10^{-26} GeV		10^{-26} GeV
\tilde{H}_{ZT}	10^{-26} GeV		10^{-27} GeV
\tilde{g}_T	10^{-27} GeV	–	10^{-27} GeV
\tilde{g}_c	10^{-26} GeV		10^{-27} GeV
\tilde{g}_Q	–	–	–
\tilde{g}_-	–	–	–
$(J = X, Y, Z)$	–	–	–
\tilde{g}_{XY}	10^{-17} GeV		–
\tilde{g}_{YX}	10^{-17} GeV		–
\tilde{g}_{ZX}	10^{-18} GeV		–
\tilde{g}_{XZ}	10^{-17} GeV		–
\tilde{g}_{YZ}	10^{-17} GeV		–
\tilde{g}_{ZY}	10^{-18} GeV		–
\tilde{g}_{DX}	10^{-22} GeV	10^{-25} GeV	10^{-28} GeV
\tilde{g}_{DY}	10^{-22} GeV	10^{-25} GeV	10^{-28} GeV
\tilde{g}_{DZ}	10^{-22} GeV		–

\tilde{d}_+	10^{-27} GeV		10^{-27} GeV
\tilde{d}_-	10^{-26} GeV		10^{-26} GeV
\tilde{d}_Q	10^{-26} GeV		10^{-26} GeV
\tilde{d}_{XY}	10^{-26} GeV		10^{-27} GeV
\tilde{d}_{YZ}	10^{-26} GeV		10^{-26} GeV
\tilde{d}_{ZX}	10^{-26} GeV		–
\tilde{d}_X	10^{-22} GeV	10^{-25} GeV	10^{-28} GeV
\tilde{d}_Y	10^{-22} GeV	10^{-25} GeV	10^{-28} GeV

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WEP tests

$$L_{LV} = L_{\text{fermion}} + L_{\text{photon}} + L_{\text{pure gravity}} + \dots$$

↑
gravitational couplings

tests:

- lab tests
 - gravimeter
 - Weak Equivalence P. (WEP)
- space-based WEP
- exotic tests
 - charged matter
 - antimatter
 - higher-generation matter
- solar-system tests
 - laser ranging
 - perihelion precession
- light-travel/clock tests
 - time delay
 - Doppler shift
 - red shift
- ...

WEP tests

place constraints on coefficients unobservable in flat spacetime

Coefficient	Electron	Proton	Neutron
$\alpha\bar{a}_T$	10^{-11} GeV	10^{-11} GeV	10^{-11} GeV
$\alpha\bar{a}_X$	10^{-6} GeV	10^{-6} GeV	10^{-5} GeV
$\alpha\bar{a}_Y$	10^{-5} GeV	10^{-5} GeV	10^{-4} GeV
$\alpha\bar{a}_Z$	10^{-5} GeV	10^{-5} GeV	10^{-4} GeV
$\alpha\bar{e}_T$	10^{-8}	10^{-11}	10^{-11}
$\alpha\bar{e}_X$	10^{-3}	10^{-6}	10^{-5}
$\alpha\bar{e}_Y$	10^{-2}	10^{-5}	10^{-4}
$\alpha\bar{e}_Z$	10^{-2}	10^{-5}	10^{-4}

* few independent constraints

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Kostelecký, Russell Rev. Mod. Phys '11
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WEP tests

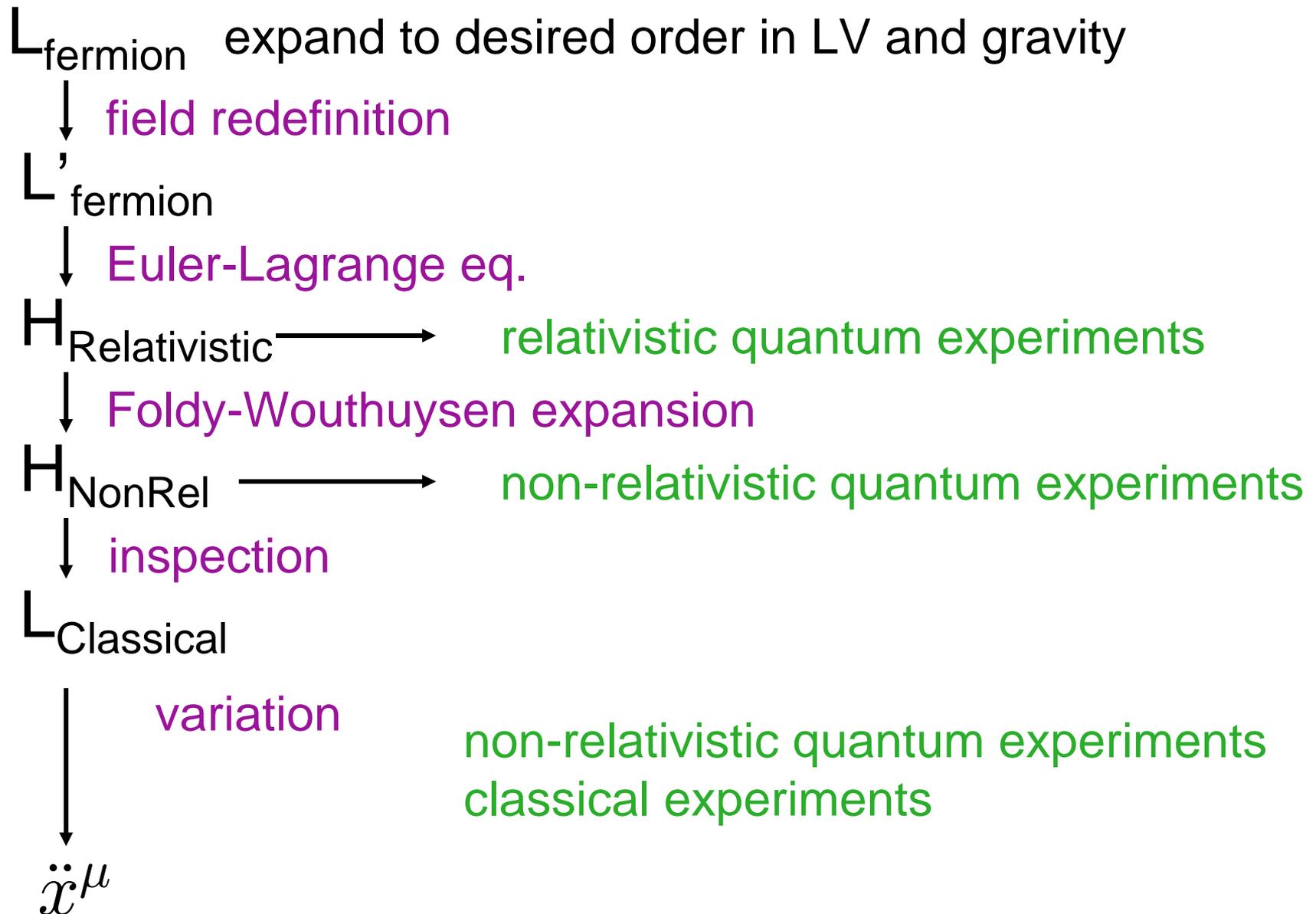
place constraints on coefficients unobservable in flat spacetime

Coefficient	Electron	Proton	Neutron
$\alpha\bar{a}_T$	10^{-11} GeV	10^{-11} GeV	10^{-11} GeV
$\alpha\bar{a}_X$	10^{-6} GeV	10^{-6} GeV	10^{-5} GeV
$\alpha\bar{a}_Y$	10^{-5} GeV	10^{-5} GeV	10^{-4} GeV
$\alpha\bar{a}_Z$	10^{-5} GeV	10^{-5} GeV	10^{-4} GeV
$\alpha\bar{e}_T$	10^{-8}	10^{-11}	10^{-11}
$\alpha\bar{e}_X$	10^{-3}	10^{-6}	10^{-5}
$\alpha\bar{e}_Y$	10^{-2}	10^{-5}	10^{-4}
$\alpha\bar{e}_Z$	10^{-2}	10^{-5}	10^{-4}

- extend range to 10^{-10} to 10^{-14}
- 3 – 5 order of magnitude improvement
- many more independent sensitivities

Data Tables for Lorentz and CPT violation
Kostelecký, Russell Rev. Mod. Phys '11
2013 edition arXiv:0801.0287v6

path to experimental analysis



classical results

$$U = \frac{2Gm}{r} \left(1 + \bar{c}_{00}^S + \frac{2}{m} (\bar{a}_{\text{eff}}^S)_0 \right) + \dots$$

$$\ddot{x}^j = -\frac{1}{2} \partial^j U + (\bar{c}^T)^j_k \partial^k U + \frac{1}{m^T} \alpha (\bar{a}_{\text{eff}}^T)_0 \partial^j U + \dots$$

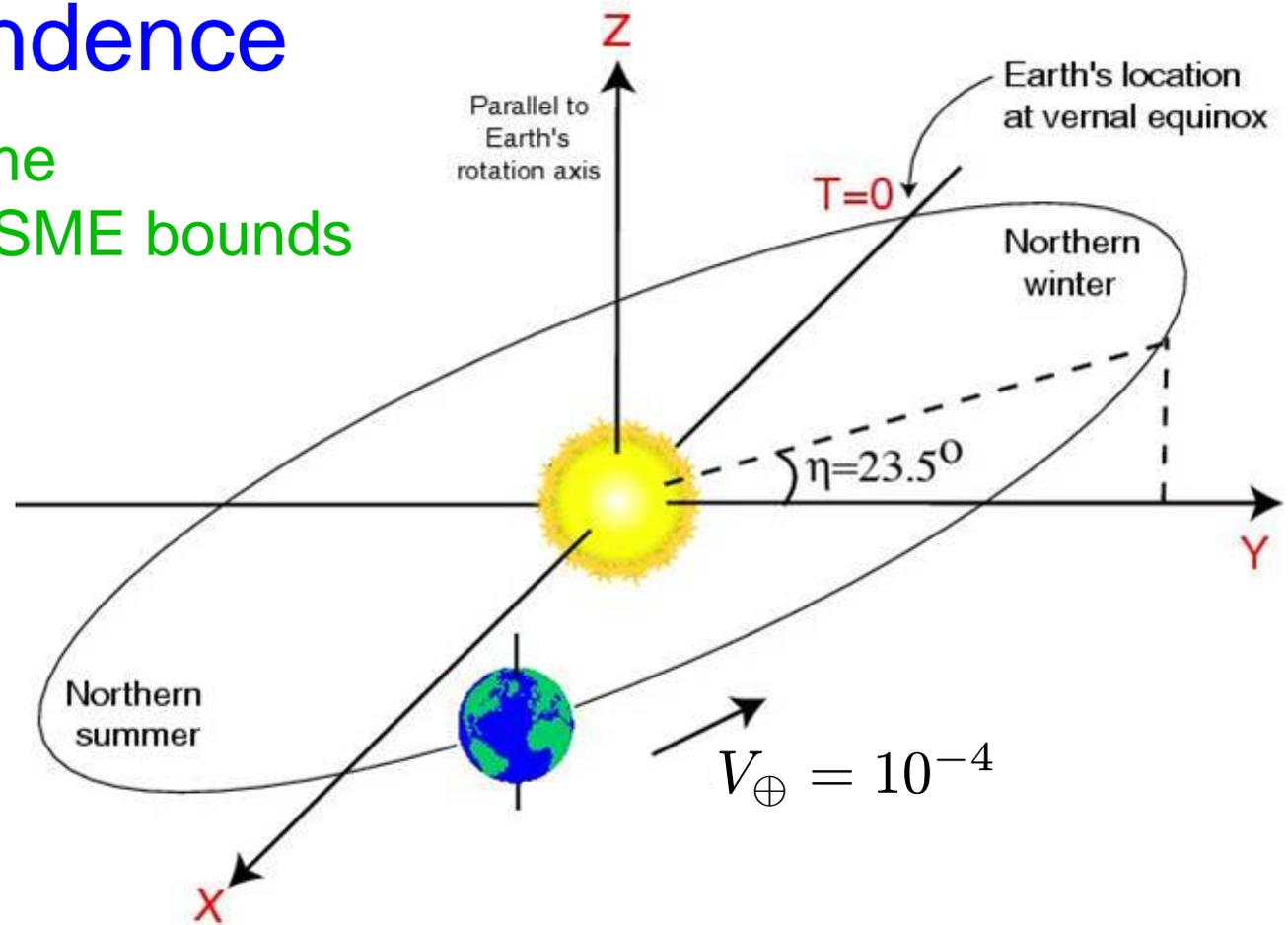
S and T denote
composite coefficients
for source and test respectively

$$(\bar{a}_{\text{eff}})_\mu = a_\mu - m e_\mu$$


- modified metric & particle equation of motion
- experimental hooks
 - particle-species dependence
 - time dependence

time dependence

- standard frame for reporting SME bounds



- boost and rotation of test \longrightarrow annual & sidereal variations

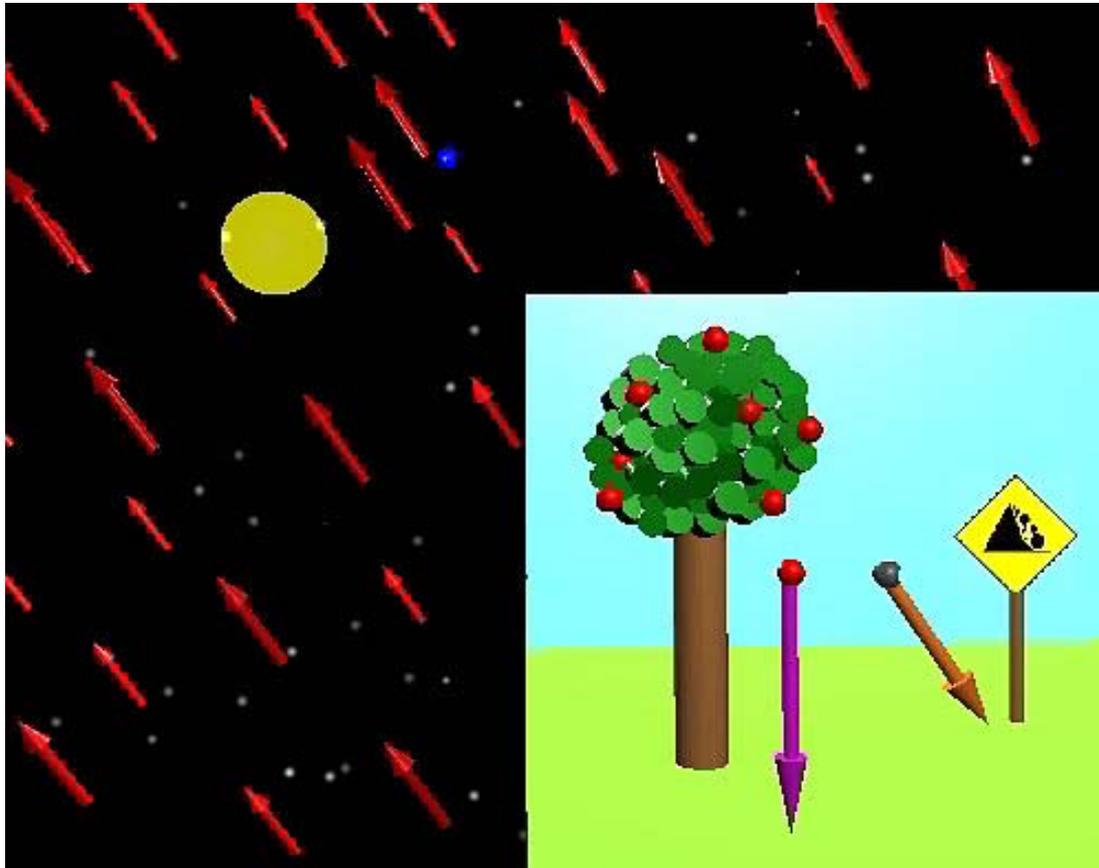
$$\ddot{\vec{x}} \supset -2g \alpha \bar{a}_T \hat{z} - 2g V_{\oplus} \alpha \bar{a}_X \sin(\Omega T) \hat{z} - \frac{2}{5} g V_L \alpha \bar{a}_X \sin(\omega T + \psi) \hat{y}$$

lab tests

acceleration of a test particle T

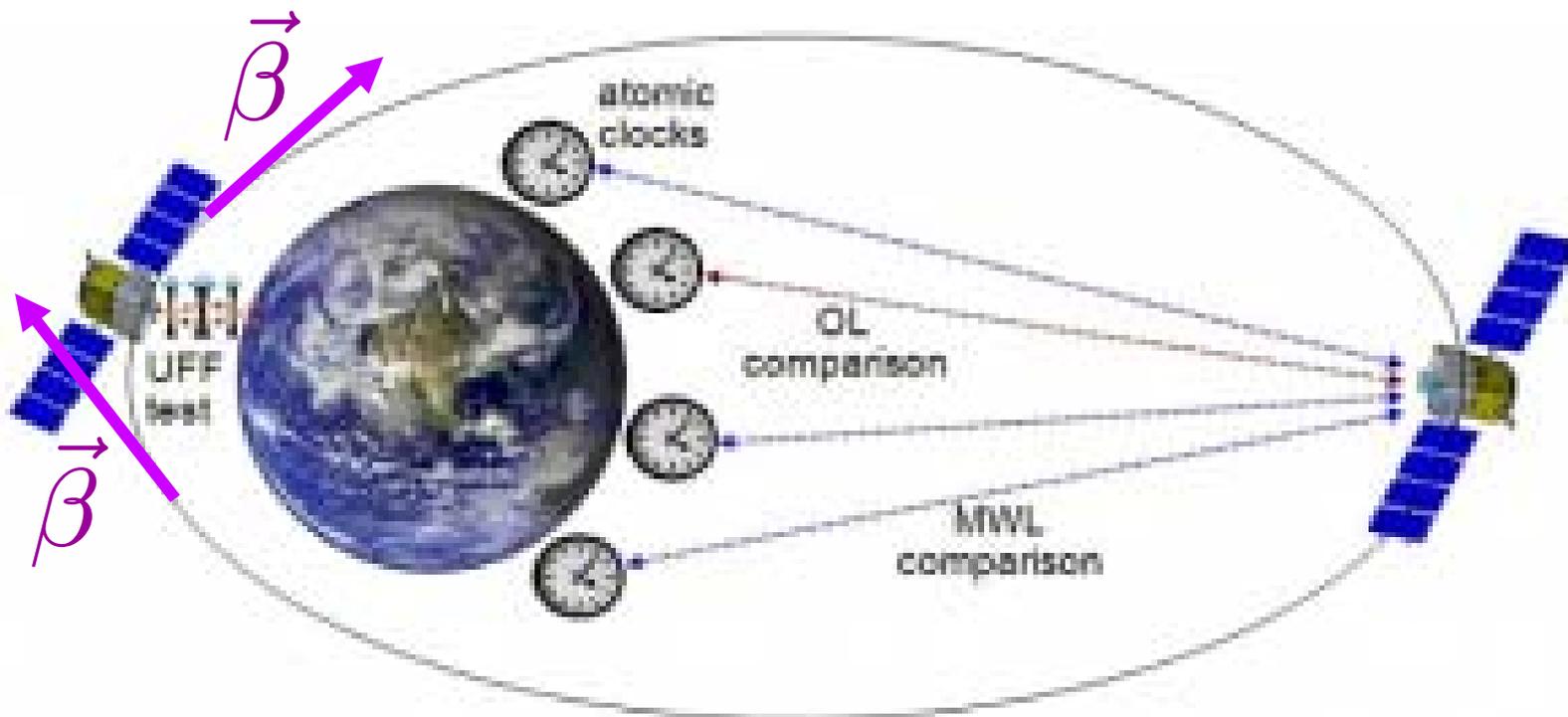
$$\ddot{\vec{x}} \supset -2\frac{1}{m}gV_{\oplus} \alpha(\bar{a}_{\text{eff}}^T)_X \sin(\Omega T) \hat{z} + gV_{\oplus} (\bar{c}^T)_{TX} \sin 2\chi \sin(\Omega T) \hat{x}$$

boost variation frequency



- monitor acceleration of one particle over time → gravimeter
- monitor relative behavior of particles → WEP (Weak Equivalence Principle) test
- frequency and phase distinguish from other effects

STE-QUEST



- improved overall WEP sensitivity
- more independent measurements via sampling of many frames

WEP tests

place constraints on coefficients unobservable in flat spacetime

Coefficient	Electron	Proton	Neutron
$\alpha\bar{a}_T$	10^{-11} GeV	10^{-11} GeV	10^{-11} GeV
$\alpha\bar{a}_X$	10^{-6} GeV	10^{-6} GeV	10^{-5} GeV
$\alpha\bar{a}_Y$	10^{-5} GeV	10^{-5} GeV	10^{-4} GeV
$\alpha\bar{a}_Z$	10^{-5} GeV	10^{-5} GeV	10^{-4} GeV
$\alpha\bar{e}_T$	10^{-8}	10^{-11}	10^{-11}
$\alpha\bar{e}_X$	10^{-3}	10^{-6}	10^{-5}
$\alpha\bar{e}_Y$	10^{-2}	10^{-5}	10^{-4}
$\alpha\bar{e}_Z$	10^{-2}	10^{-5}	10^{-4}

- extend range to 10^{-10} to 10^{-14}
- 3 – 5 order of magnitude improvement
- many more independent sensitivities

Data Tables for Lorentz and CPT violation
Kostelecký, Russell Rev. Mod. Phys '11
2013 edition arXiv:0801.0287v6

additional possibilities

$$L_{LV} = L_{\text{fermion}} + L_{\text{pure gravity}} + \dots$$

gravitational couplings

- red-shift tests
- orbital tests

Kostecky Bailey PRD '06

Bailey PRD '09

Kostecky Tasson PRL '09; PRD '11

Gravitomagnetic effect on intrinsic spin

$$\vec{b} \leftrightarrow \frac{G}{r^3} \vec{J}_{\oplus}$$

Tasson PRD '12

$$L_{LV} = L_{\text{minimal}} + L_5 + L_6 + L_7 + \dots$$

existing tests

large space for new searches

Kostecky Mewes PRD '12

Summary

- STE-QUEST can probe Planck-scale physics via Lorentz symmetry tests
- sensitivities to large classes of presently uninvestigated coefficients can be attained
- significant sensitivities can be achieved via both clock-comparison tests and WEP tests that have qualitatively unique signatures
- sampling many Lorentz frames is an advantage of STE-QUEST in obtaining a maximum number of independent sensitivities to Lorentz violation