

**3D analysis of the ring current  
for the 20 April 2002 event using  
ENA image inversions (IMAGE/HENA) and  
the curlometer technique (Cluster/FGM data).**

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# Methodology

**Goal:** 3D Mapping of a well-developed ring current (20 April 2002) using in-situ and remote-sensing data.

## 1- In-situ: Cluster perigee pass inside the ring current (polar orbit)

- ⇒ 4 simultaneous points of measurement of B.
- ⇒ J estimate using Maxwell-Ampere's law (*curlometer technique*).
- ⇒ Provides the latitudinal evolution of the J vector (all along the Cluster orbit).
- ⇒ Local particle flux measurements.

## 2- Remote-sensing: IMAGE-HENA gives a global view of the ENA population issued from charge exchange processes

- ⇒ Provides a global picture of the equatorial ring current ions distribution (*inversion algorithm*).
- ⇒ Allows an estimate of the kinetic pressure distribution. (under study)



# MHD theory

- MHD momentum equation:

$$\rho \frac{d\vec{U}}{dt} = -\nabla \cdot \vec{p} + \vec{J} \times \vec{B}$$

$\left\{ \begin{array}{l} U: \text{flow velocity.} \\ P: \text{pressure tensor.} \\ J: \text{current density.} \end{array} \right.$

- Solution in the plane perpendicular to  $\mathbf{B}$  (static):

$$\vec{J}_{\perp} \approx \frac{\vec{B}}{B^2} \times \left[ \underbrace{\nabla_{\perp} p_{\perp}}_{\text{Current due to Pressure gradients}} + \underbrace{\frac{(p_{\parallel} - p_{\perp})}{B^2} [(\vec{B} \cdot \nabla) \cdot \vec{B}]}_{\text{Current due to the } \mathbf{B} \text{ curvature and anisotropy}} \right]$$

Current due to  
Pressure gradients

Current due to the  
 $\mathbf{B}$  curvature and anisotropy





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In situ Cluster data:  
the curlometer technique

## 1- In situ Cluster data

## Curlometer technique

Maxwell-Ampère's law:

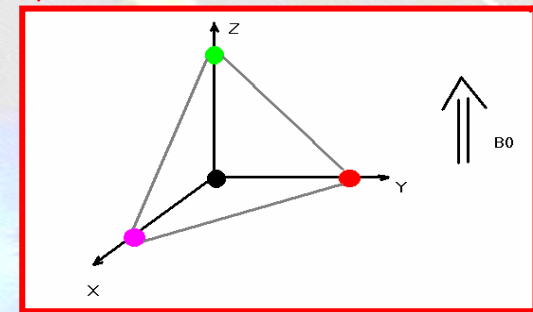
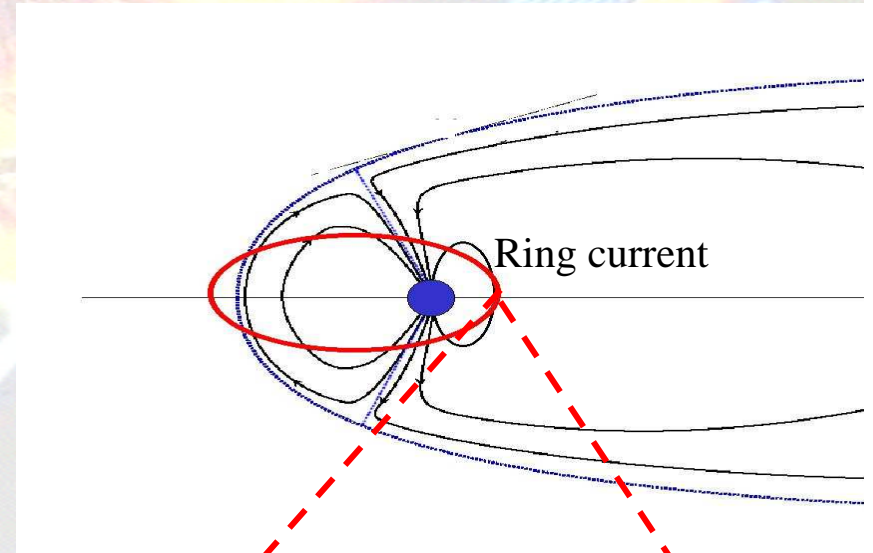
$$\nabla \times \vec{B} = \mu_0 \cdot \vec{J}$$

$$(\nabla \times B)_x = \frac{\Delta B_z}{\Delta y} - \frac{\Delta B_y}{\Delta z}$$

$$(\nabla \times B)_y = \frac{\Delta B_x}{\Delta z} - \frac{\Delta B_z}{\Delta x}$$

$$(\nabla \times B)_z = \frac{\Delta B_y}{\Delta x} - \frac{\Delta B_x}{\Delta y}$$

$$\mu_0 \vec{J}_{average} (\Delta \vec{r}_i \times \Delta \vec{r}_j) = \Delta \vec{B}_i \cdot \Delta \vec{r}_j - \Delta \vec{B}_j \cdot \Delta \vec{r}_i$$



⇒ **Curlometer technique:** Local current density estimate (strength and orientation) deduced from the 4 SC magnetic field data.



## 1- In situ Cluster data    Curlometer technique limitations

- **Tetrahedron size and shape** (elongation and planarity of the tetrahedron).
- **Linear interpolations** (truncations errors and reference spacecraft).
- **Accuracy of the magnetic field measurement** (gain and offset).

Perigee passes of Cluster (ring current crossing) with a **100 km separation strategy (20 April 2002 event)** :

⇒ **Most of the error carried by  $J_z$  ( up to 20% )**.

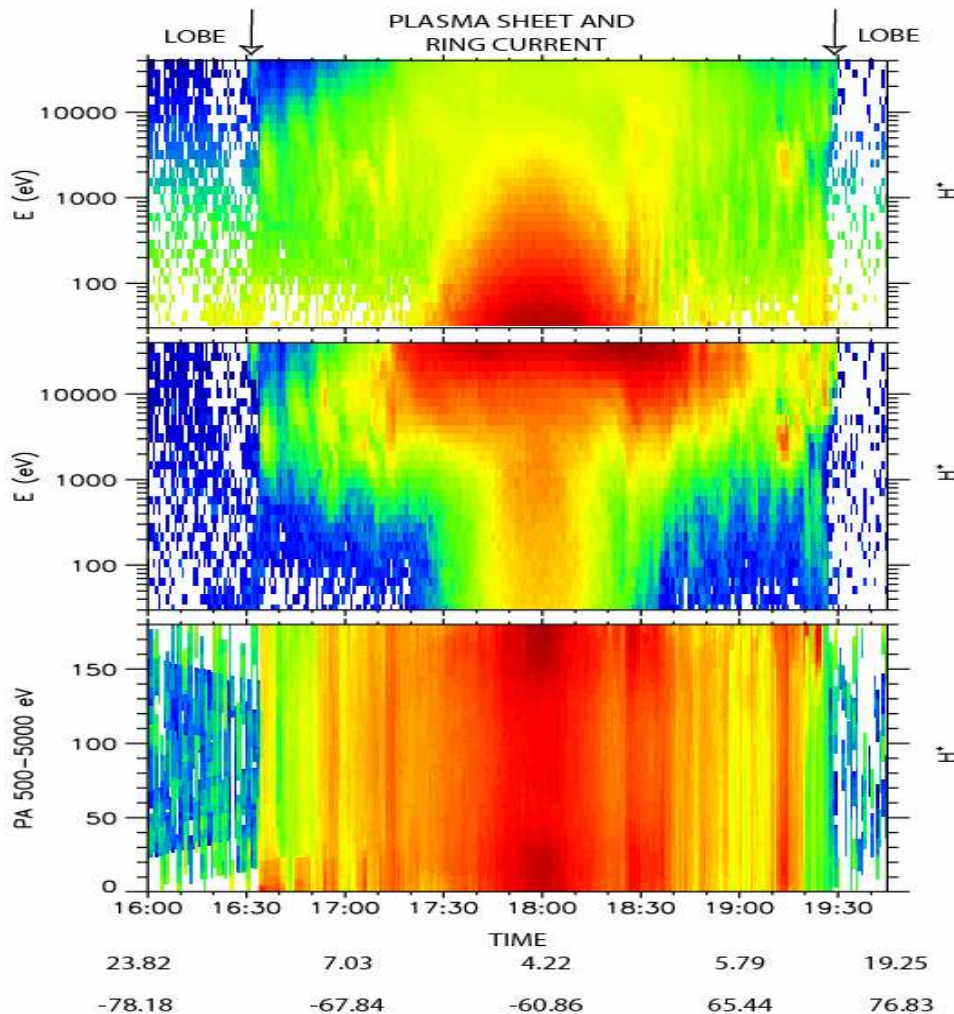
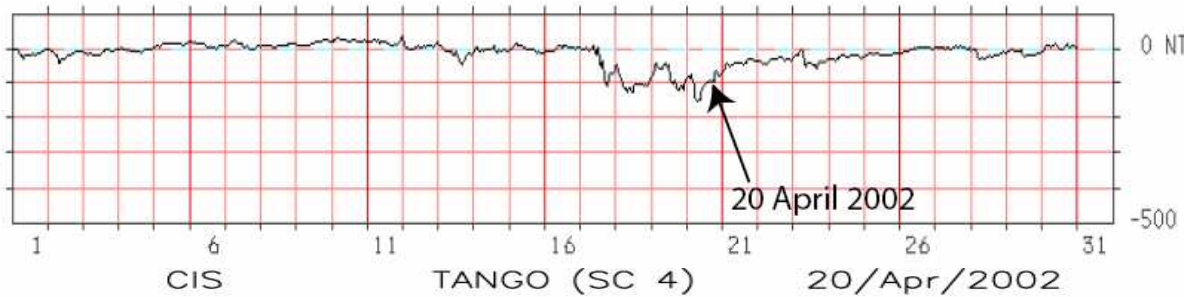
⇒ **Good estimation of  $J_x$  and  $J_y$  (accuracy of about 2% - 5%).**

[*Vallat et al., Ann. Geophysicae, 2005*]



# 1- In situ Cluster data

## 20 April 2002 (1)



- Storm conditions.
- Dst ~ -100 nT:  
Well-developed ring current.

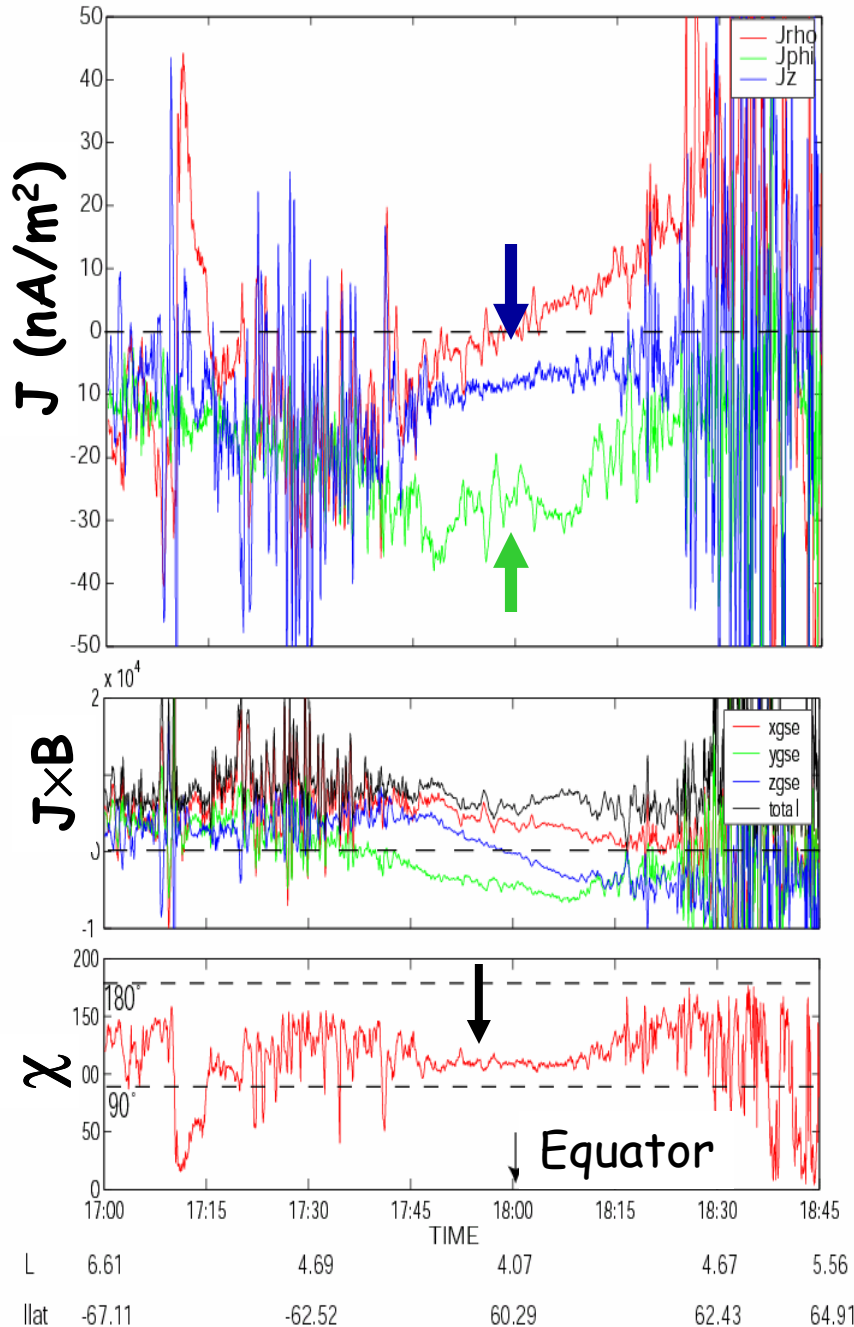
- Cluster perigee crossing:  
MLT ~ 21

- CIS/Cluster ion data:  
Gradual transition between  
the plasma sheet and the ring  
current.



# 1- In situ Cluster data

## 20 April 2002 (2)



- Negative and constant  $J_z$  component all along the ring current traversal

- The largest component of  $J$  is azimuthal:  $\langle J_\phi \rangle \sim -25 \pm 20\% \text{ nA/m}^2$  (westward current)

- $J \times B \propto \nabla P$  (gives the position w.r.t the maximum pressure):

$\Rightarrow P_{\max}$  situated downward (towards the tail axis) and slightly Earthward of the spacecraft location.

- Ring current is not fully azimuthal during disturbed periods:

$\Rightarrow$  Existence of a small parallel component near the Equator.

(Seasonal effects due to the different ionospheric conductivities of the two hemispheres?)





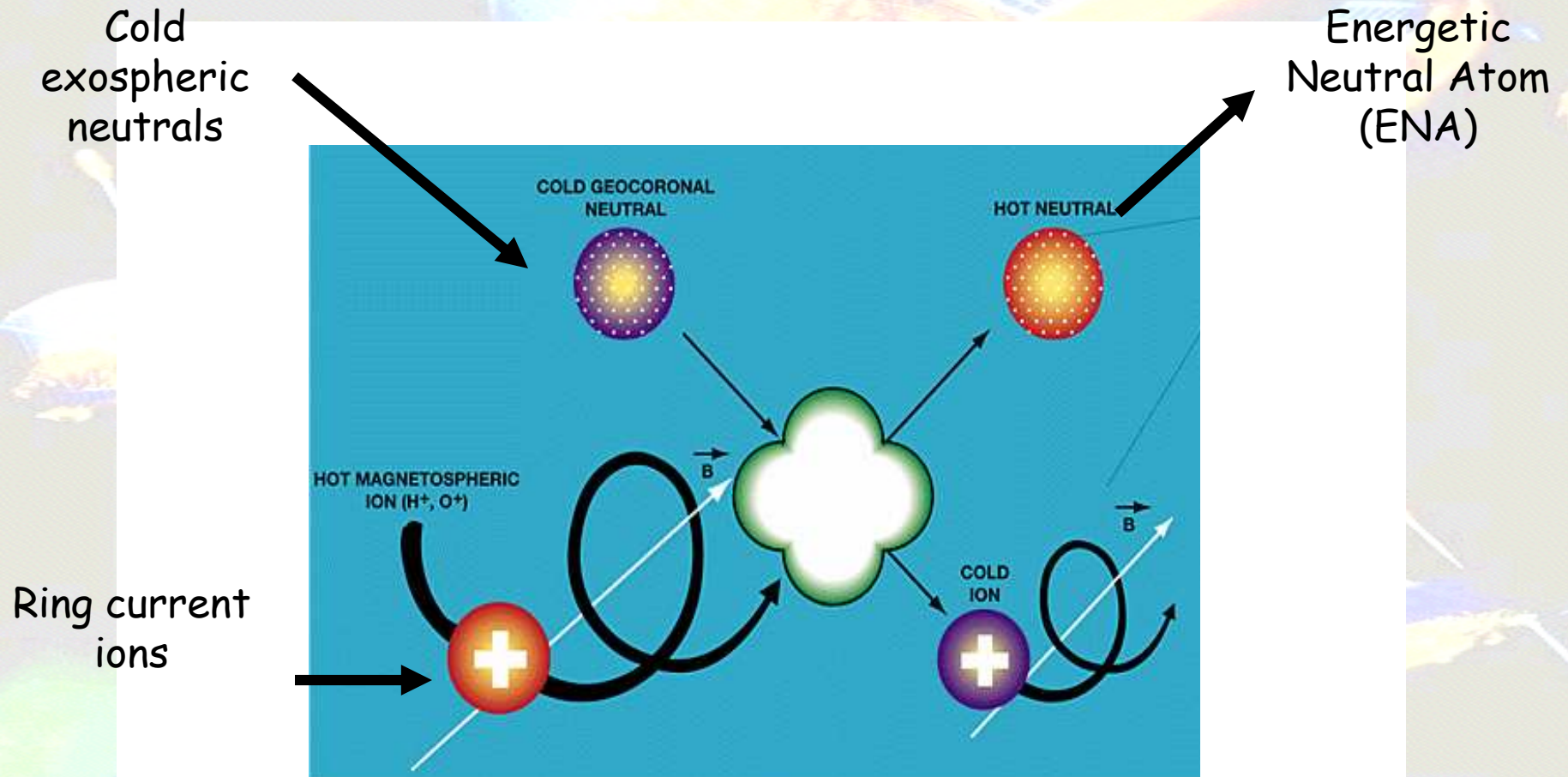
2

IMAGE ENA imaging:  
the image inversion technique



## 2- IMAGE-HENA imaging

## Charge exchange



$$j_{ena}(E) = \int_0^{s_e} n^H(s) \sigma_H^{10}(E) j_{ion}(s, E) ds + j_{ena}^e(s_e) \quad [Roelof, 1989]$$

Energetic neutral atoms have the same direction and the same energy as the incoming ion.

=> ENA bring crucial information concerning the ring current ions.



## 2- IMAGE-HENA imaging

## Inversion method

1\_ Number of counts received by the neutral imager (HENA)

$$C_i = \int_0^\infty \int_0^\infty \int_0^{2\pi} \int_0^\pi \sin \varepsilon A_i(\varepsilon, \beta, E, t) j_{ena} d\varepsilon d\beta dE dt$$

2\_ Neutral intensity

$$j_{ena} = \int_0^{s_e} n^H(s) \sigma_H^{10}(E) j_{ion}(s, E) ds + j_{ena}^e(s_e)$$

1 + 2: Linear inversion method.  
Solution can be written as :

$$J_{ion} = (K^T \sigma_C^{-2} K + \gamma H)^{-1} K^T \sigma_C^{-2} C$$

[DeMajistre et al., JGR, 2004]

⇒ Using ENA imaging, we can access to the equatorial distribution of the parents ions (i.e. the current carriers) for the energy range considered.



## 2- IMAGE-HENA imaging

20 April 2002 (2)

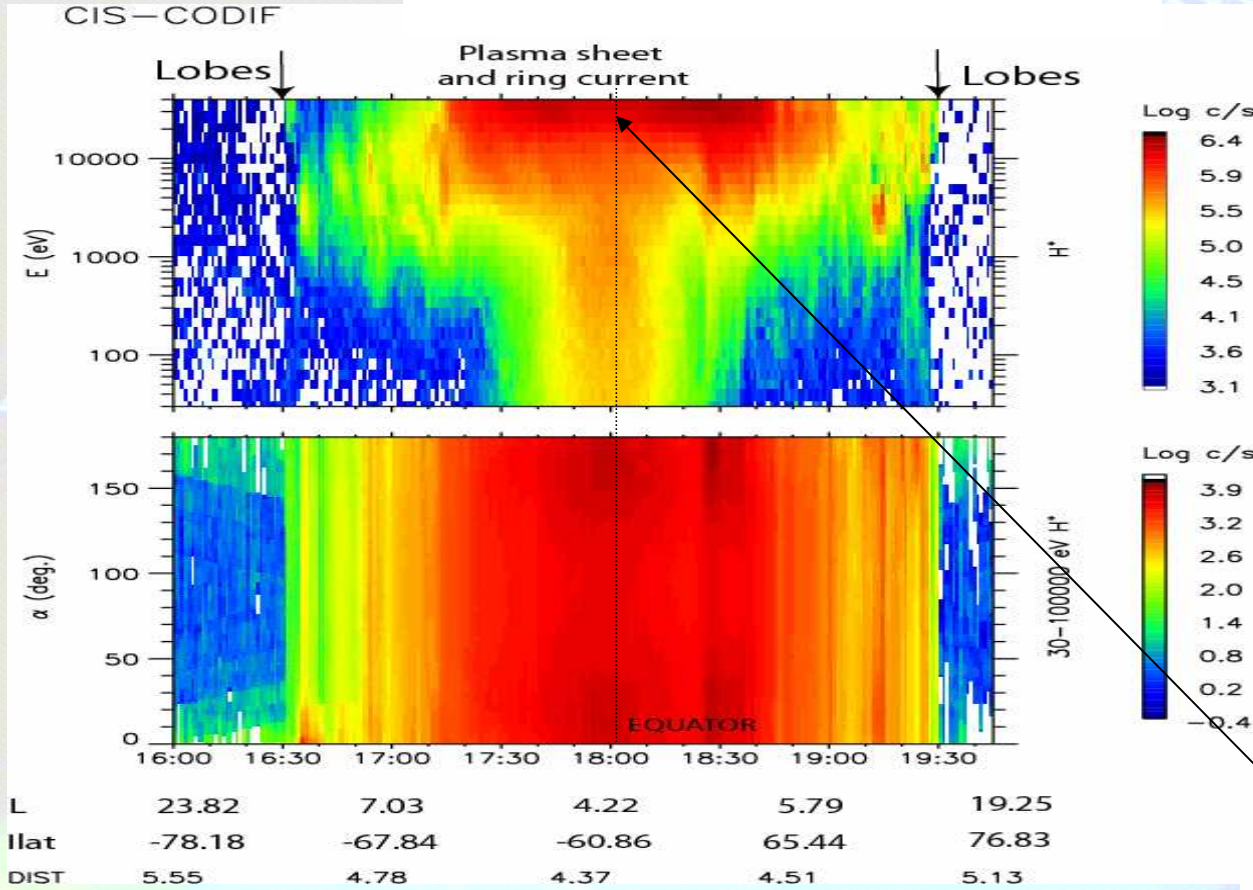
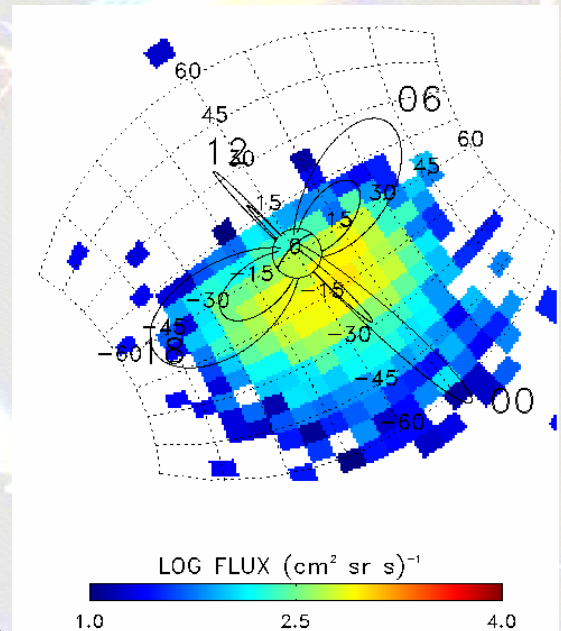


IMAGE-HENA  
27-39 keV range

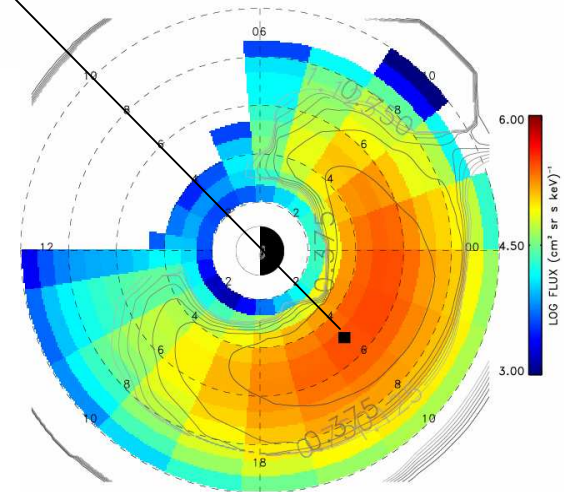


- Quantitatively: consistent results (factor of  $\sim 1.3$ ) between in-situ and ENA image inversion data ( $H^+$ ,  $27 < E < 39$  keV):

$$\text{CIS: } f_i \approx 1.78 \times 10^5 \text{ (cm}^2 \text{ sr s keV)}^{-1}.$$

$$\text{HENA inversions: } f_i \approx 2.43 \times 10^5 \text{ (cm}^2 \text{ sr s keV)}^{-1}.$$

- Morphology of the ring current (position of Cluster w.r.t the ring current bulk) is well reproduced by the image inversion [Vallat et al., JGR, 2004].





## The curlometer technique:

## Conclusions...

\* Latitudinal evolution of the J orientation :

- Filamentation of the current density components in the plasma sheet.

⇒ Consequence of non-linear gradients due to the small size of the current layers (< tetrahedron size).

- Shows the existence of a small parallel component near the Equator.

⇒ Seasonal effects due to the different ionospheric conductivity between the two hemispheres?

\* Position of the maximum pressure is situated dawnward and Earthward of the spacecraft location for the event studied.

## The energetic neutral atom image inversion:

\* Position of the maximum pressure is situated dawnward (towards the tail axis) of the spacecraft location.

⇒ Consistent with the curlometer results.

\* Possibility to calculate equatorial currents from the pressure distribution (under study).