

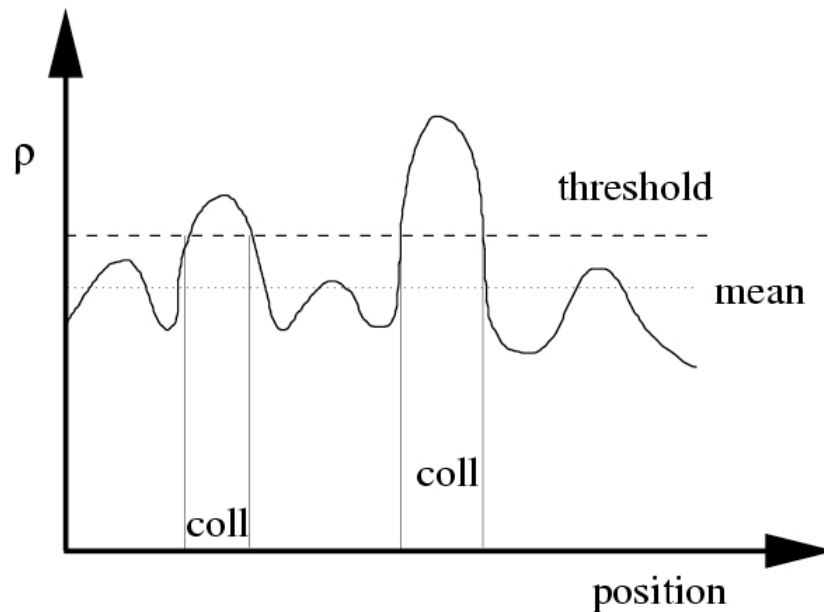


# Cosmological Constraints with Galaxy Cluster Counts with the Euclid Imaging Survey

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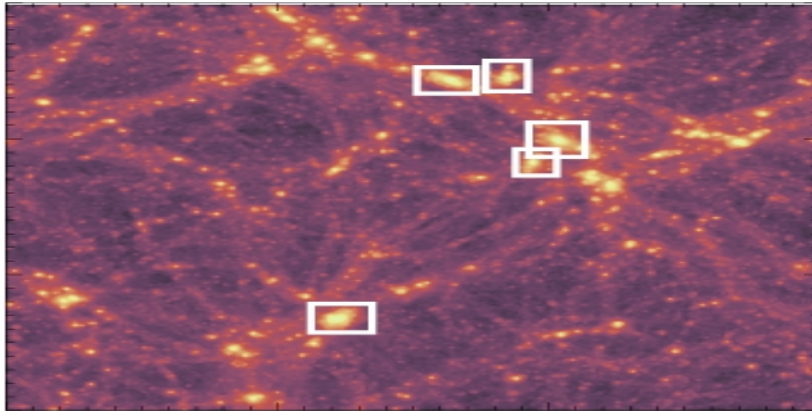
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Amara (ETH), Joel Berge (JPL), Marian Douspis (Orsay),  
Tom Kitching (Edinburgh), Lauro Moscardini (Bologna),  
Alexandre Refregier (Saclay), Stella Seitz (LMU, MPE)

# Galaxy Clusters as a Probe of Structure Formation in the Universe

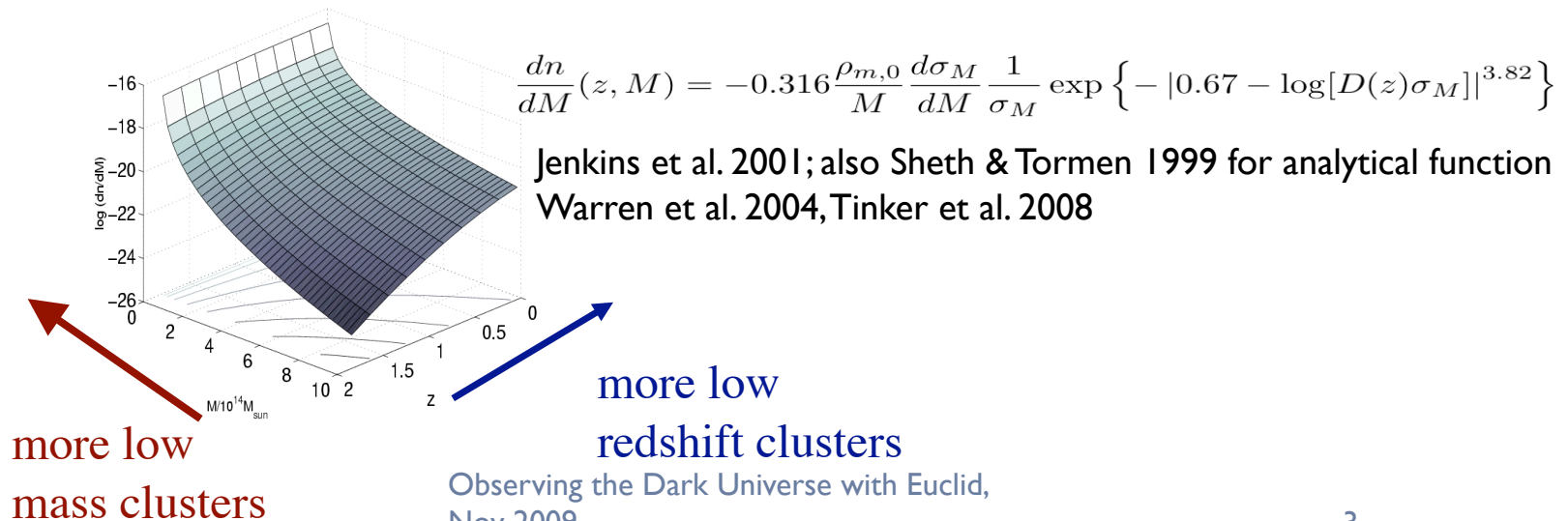


- If linear density perturbation exceeds threshold density the region will collapse and form a cluster
- Mass function sensitive to amplitude of perturbations ( $\sigma_8$ ) and mass contents of the Universe ( $\Omega_m$ ); but also other cosmological parameters ( $w$ ) !

# Counting Dark Matter Halos



- Count halos in N-body simulations
- Measure “universal” mass function - density of cold dark matter halos of given mass



# Cosmology Dependence of the Mass Function

$$\frac{dn}{dM}(z, M) = -0.316 \frac{\rho_{m,0}}{M} \frac{d\sigma_M}{dM} \frac{1}{\sigma_M} \exp \left\{ - \left| 0.67 - \log [D(z) \sigma_M] \right|^{3.82} \right\}$$

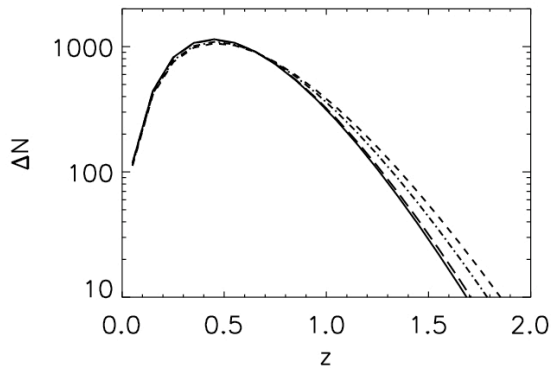
- mass density
- power law dependence on fluctuation amplitude
- power law dependence on growth factor

# Predicting Cluster Number Counts

$$\Delta N(z) = \Delta\Omega \int_{z-\Delta z/2}^{z+\Delta z/2} dz \frac{d^2V}{d\Omega dz} \int_{M_{\text{lim}}}^{\infty} \frac{dn}{dM} dM$$

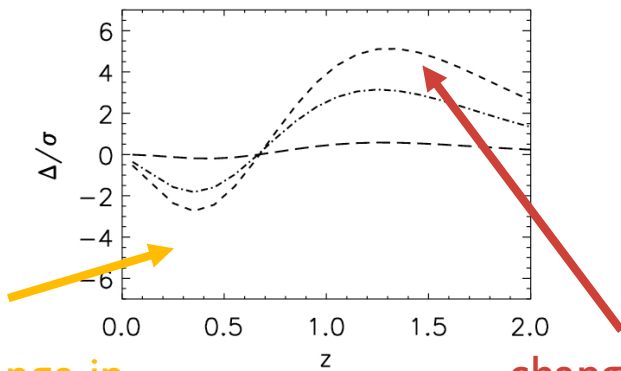
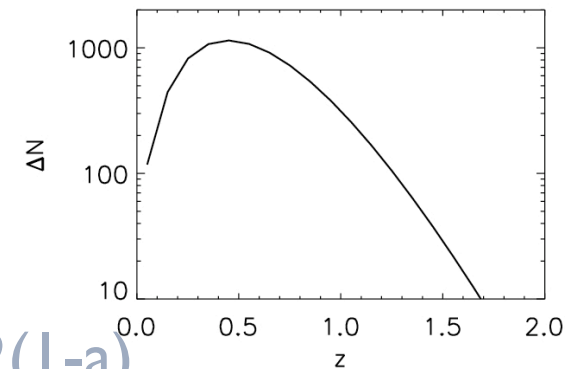
- Survey sky coverage
- Redshift bins
- Volume element
- Limiting mass of survey (redshift dependent)
- Cosmology dependence driven by volume element and mass function

# Cosmology Dependence of Number Counts



- concordance cosmology:  
 $\Omega_m = 0.3$ ;  
 $\sigma_8 = 0.78$ ;  $n=1$ ,  $h=0.72$ ;  
 $w=-1$ ,  $\Delta\Omega = 4.000 \text{ deg}^2$   
 $M_{\text{lim}} = 1.7 \times 10^{14} h^{-1} M_\odot$

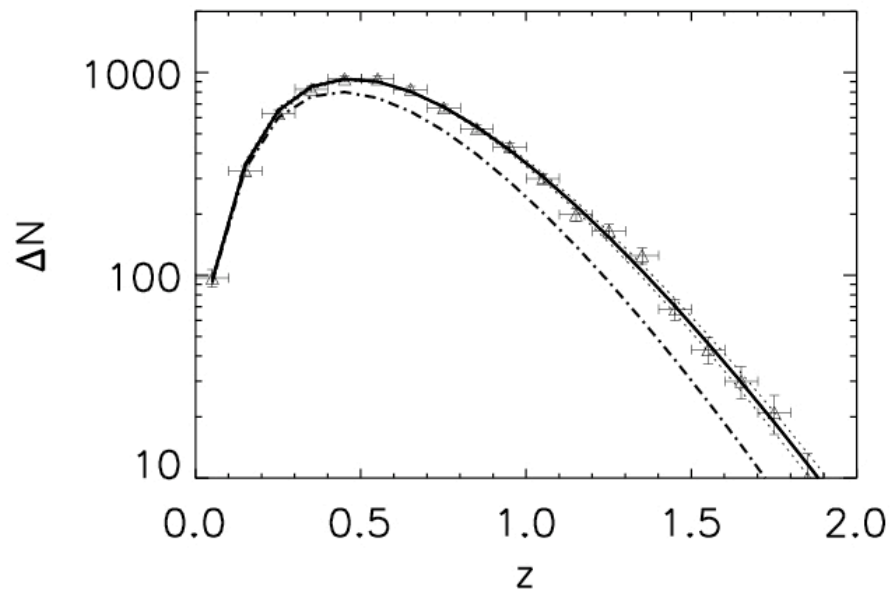
- $\Omega_m = 0.4$
- $\sigma_8 = 0.85$
- $w = -0.8$
- $w = -0.7$
- $w = -1 + 0.2(1-a)$



change in volume

change in growth factor

# Cluster Counts in DGP Model



- DGP number counts for  $\sigma_8 = 0.75$ ,  $n=1$ ,  $M_{\text{lim}} = 1.7 \times 10^{14} h^{-1} M_{\odot}$  (from 'SPT')
- mock data assuming Poisson errors
- mimic DE model

significant difference between  
mimic DE and DGP:  $> 1\sigma$



# Selection Clusters with Euclid

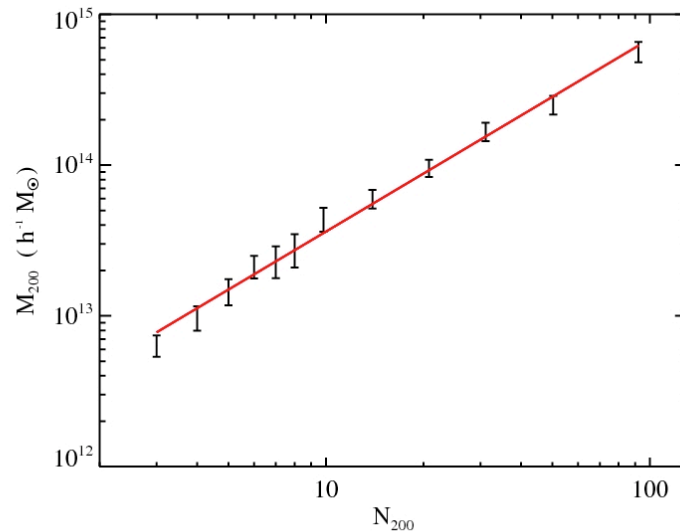
- Weak lensing: e.g. peak statistics
- Galaxy overdensities
  - maxBCG
  - Voronoi Tessellation
  - Matched filters
  - Counts in Cells
  - Percolation Algorithms (FoF)
  - smoothing kernels
  - surface brightness enhancements
  - ...
- Strong Lensing



# maxBCG as Baseline Method

- Brightest Cluster Galaxy (BCG) at centre of every cluster
- tight color-magnitude relation of BCG
  - used to (pre-) select
- Identifying ridgeline galaxies
  - use model for radial and color distribution
- maximize the two models as a function of redshift: estimate of redshift of cluster
- Iterative scheme: removal of most likely clusters and their satellites
- Apply probability chain, which has been calibrated with mock observations
- Successfully applied to SDSS sample (Rozo et al.)
- Biggest problem: Completeness and Purity of Sample
  - projection effects along line of sight; misestimate of cluster members

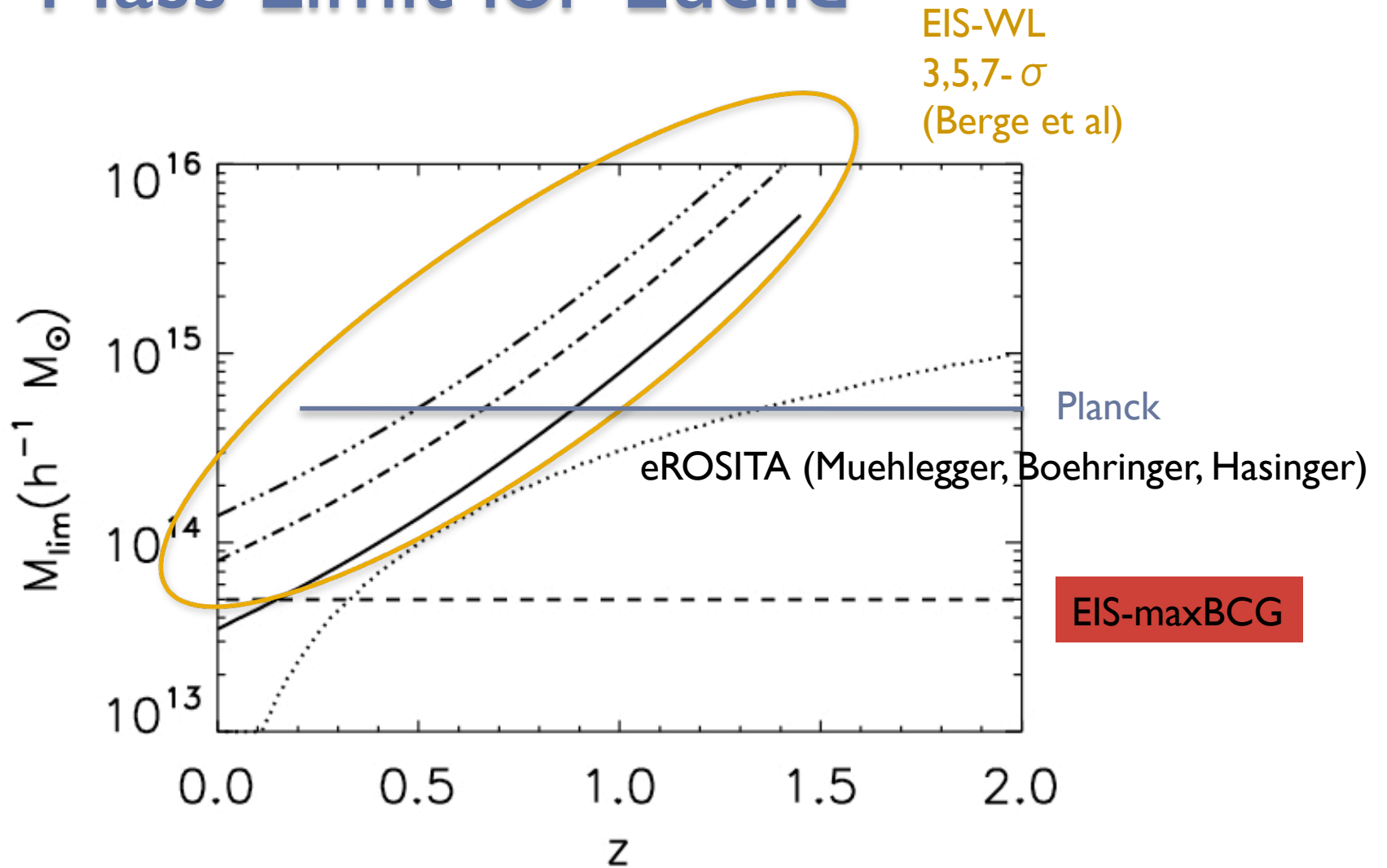
# maxBCG Selection SDSS: A Lesson for Euclid ?



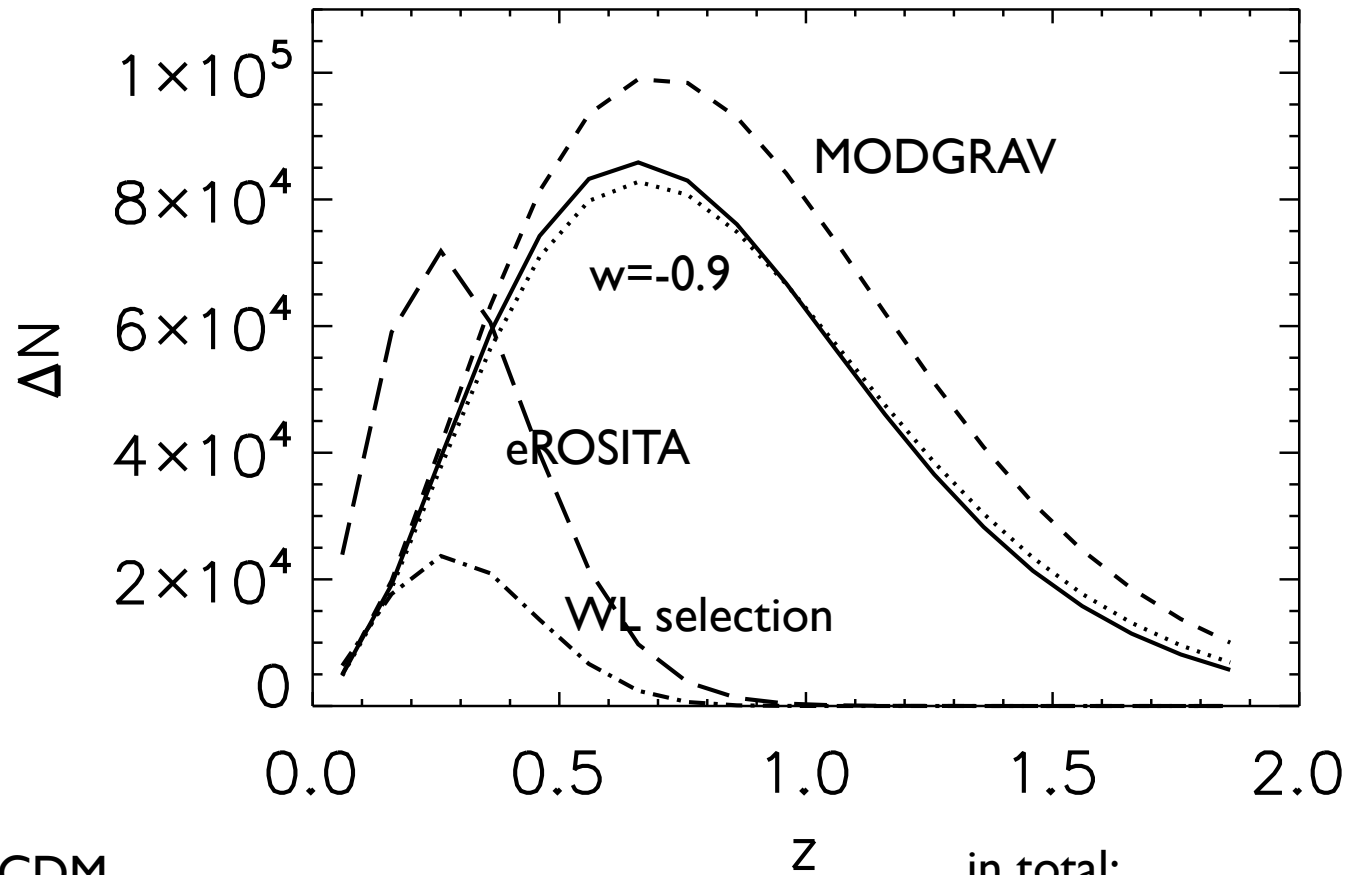
Johnston et al. 2007

- Mass – Richness relation
  - calibrated with statistical weak lensing measurements (for 130,000 groups)
  - Johnston et al. 2007
- Good purity and completeness to about:  $M \sim 10^{13.5} h^{-1} M_{\odot}$
- however for SDSS only to:  $z \sim 0.3$
- depth of Y, J and H filters
  - should be able to find ridgeline galaxies out to  $z = 1.3-2.0$
  - how far out do we find robust red sequence ?

# Mass Limit for Euclid



# Cluster Numbers for Euclid



solid:  $\Lambda$ CDM

in total:

well over 750,000#

Observing the Dark Universe with Euclid,  
Nov 2009

# Uncertainty in Mass Limit

- Mean mass observable relation
  - scaling laws dependent on method – not entirely determined: redshift and mass dependence
  - different methods can be used for cross calibration
- individual scatter in mass observable relation
  - how behave the tails
    - high redshift, low mass, high mass, etc.
  - degenerate with cosmology
  - can also be estimated by surveys
    - Rozo et al.: optical, x-ray and weak lensing find  $0.45 \pm 0.20$

# General Form for Scaling and Scatter

- assign likelihood for observed mass for a true mass  $p(M_{\text{obs}} | M)$  with a bias and a scatter included; allow to differ in redshift and mass bins

$$p(M_{\text{obs}} | M) = \frac{1}{\sqrt{2\pi}\sigma_{\ln M}} \exp[-x^2(M_{\text{obs}})]$$

$$x(M_{\text{obs}}) = \frac{\ln M_{\text{obs}} - \ln M - \ln M_{\text{bias}}}{\sigma_{\ln M}}$$

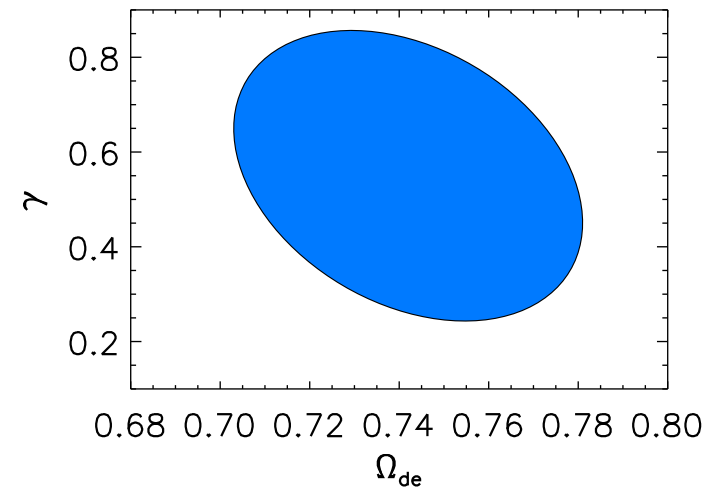
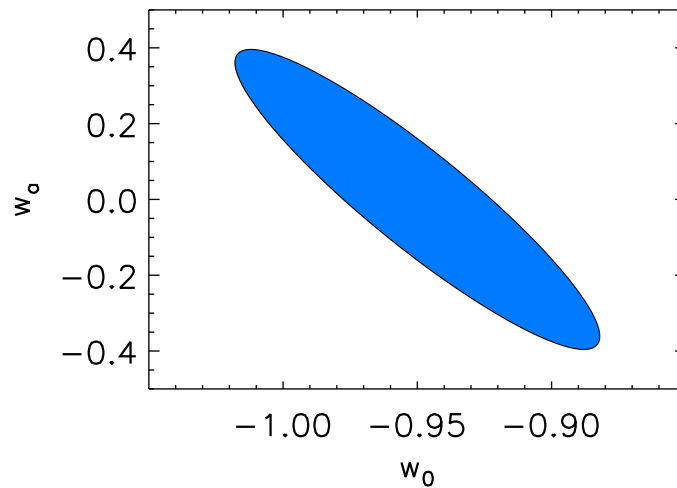
- completely free form does not allow cosmology fit (Lima & Hu)
- $\ln M_{\text{bias}} = A + n \ln(1+z)$ 
  - better form for particular selections possible
- $\sigma_{\ln M}^2 = A + Bz + Cz^2 + \dots$ 
  - so far this is ad hoc

# Self-Calibration

$$n_i = \int_{M_{obs}^i}^{M_{obs}^{i+1}} \frac{dM_{obs}}{M_{obs}} \int \frac{dM}{M} \frac{dn}{d \ln M} p(M_{obs}|M)$$

- Exploit shape of mass function to calibrate for bias and scatter in constant mass bins
- Further use clustering of clusters (cross-correlated to other probes ? Not used here! )
- Result: scatter in mass-observable relation is not the problem: Increases number of clusters, hence better statistics
- Uncertainty in scatter is **PROBLEM**

# Constraints from EIS Cluster Counts

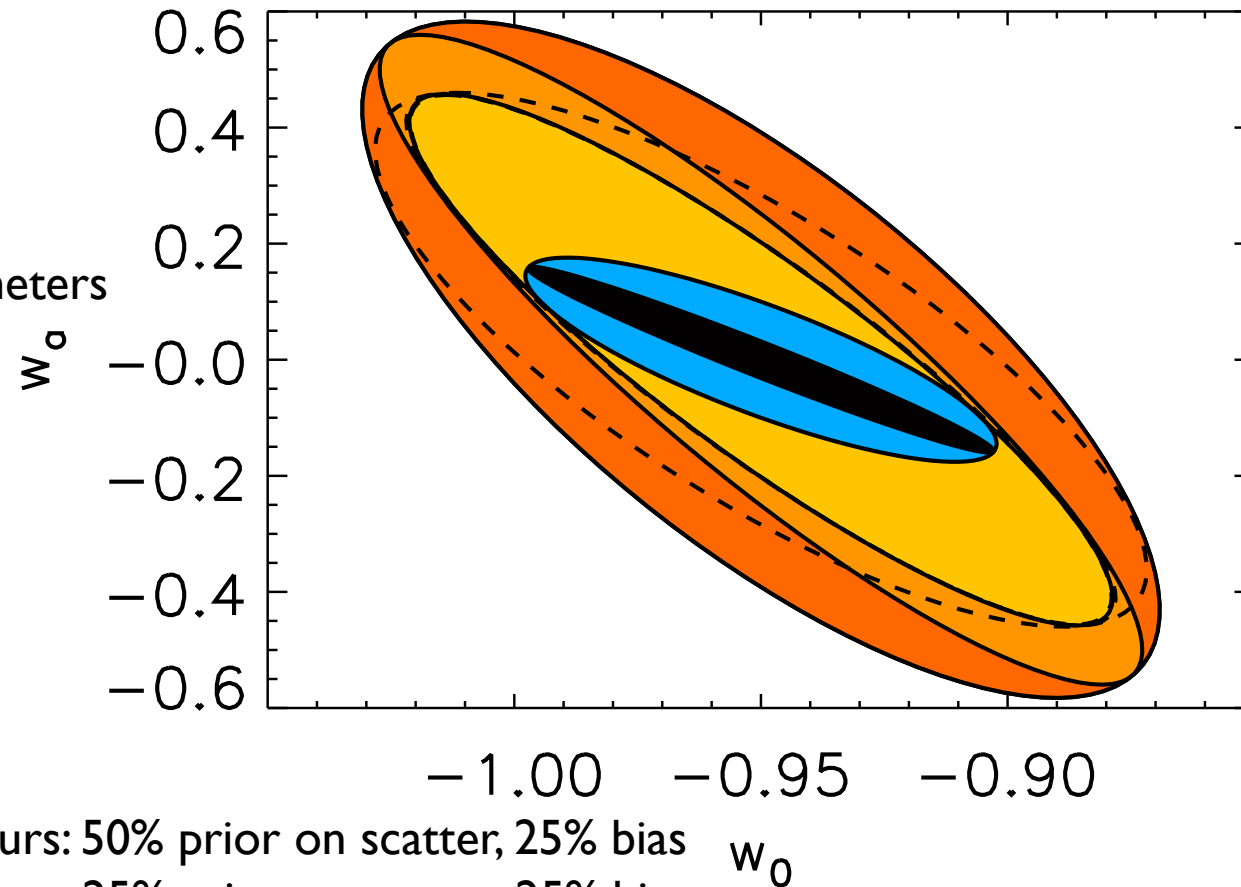


Including Planck priors and 5 cluster nuisance parameters; prior on scatter: 25%



# Cosmology and Priors on the Mass – Observable Relation

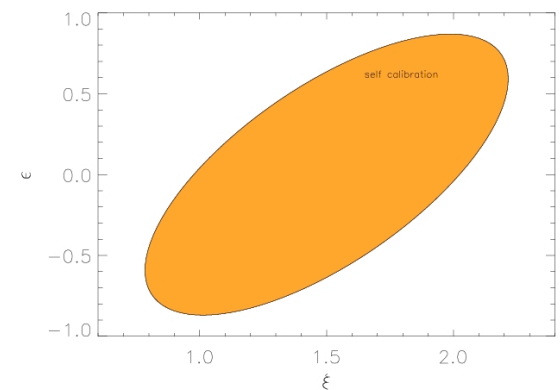
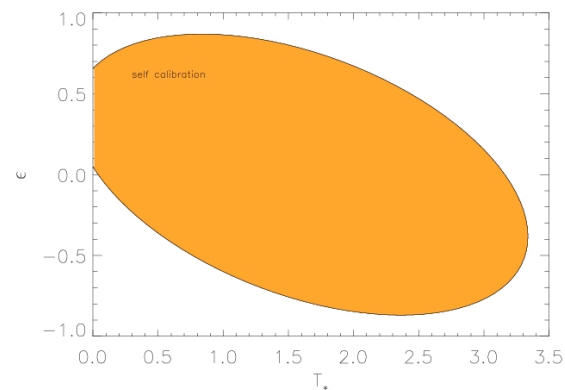
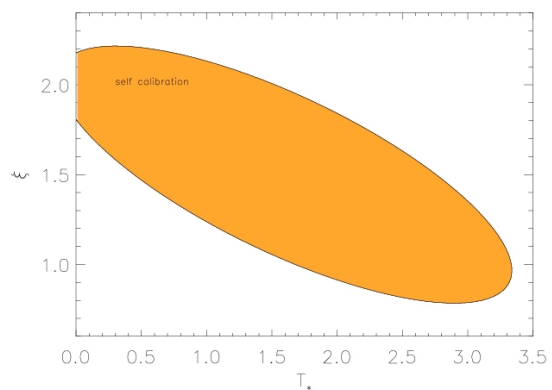
1,2 and 3  
scatter parameters



orange contours: 50% prior on scatter, 25% bias  
dashed contours: 25% prior on scatter, 25% bias  
blue contour: fixed scatter  
dark contour: fixed scatter and bias

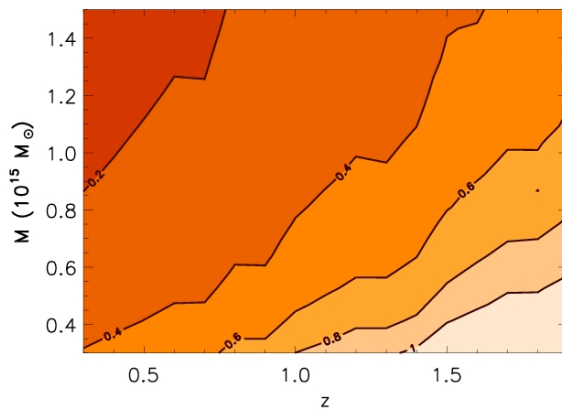
# Self-Calibrate Uncertainty in Mass – Temperature Relation

- Relevant for SZ and x-ray surveys
- In addition to cosmological parameters fit for cluster parameters  $T_*$  ;  $\xi$  ;  $\epsilon$



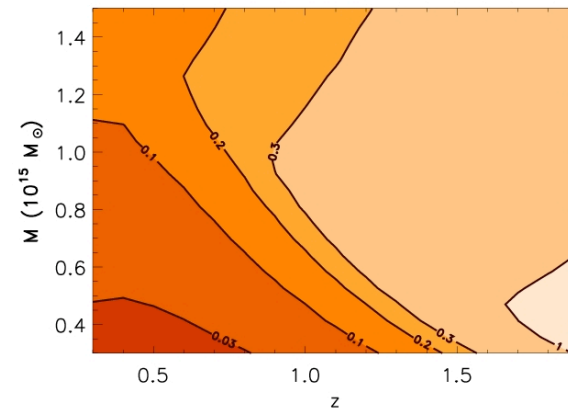
# Weak Lensing Calibration of Mass - SZ Observable Relation

- Here simple estimate: 15 background (DES) galaxies/sq. arcmin
- Distribution:  $dn/dz = \exp(-z/z_c)$ ;  $z_c=0.5$



Projected errors on single cluster

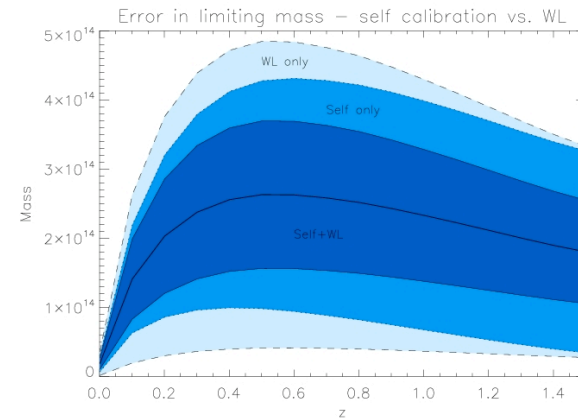
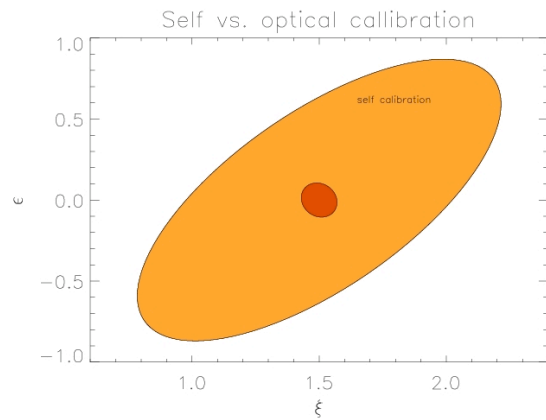
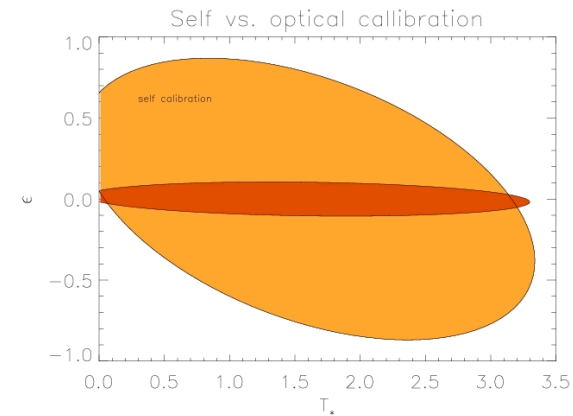
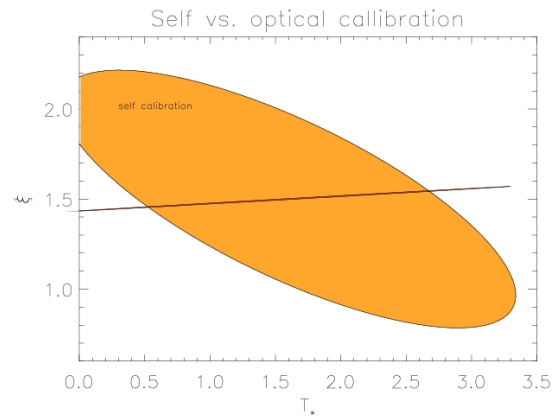
Dodelson & Weller:  
DES and SPT



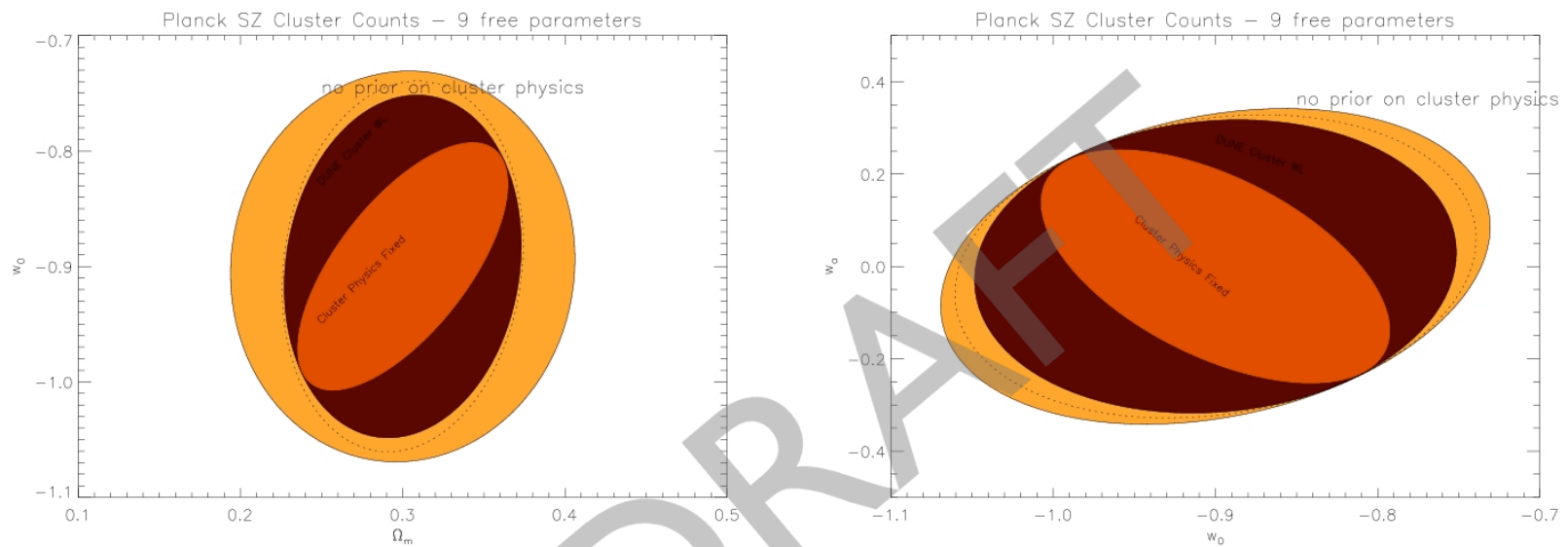
Fractional errors on cluster mass after **stacking** in redshift bins

$$\Delta z = 0.1 \text{ and } \Delta M = 10^{14} M_{\odot}$$

# Weak Lensing Calibration



# How can Euclid help Planck-SZ Clusters – *Very Preliminary!*



**NO SCATTER; NO Planck Prior, see also Cunha et al., Wechsler et al.  
But also vice versa: Improvement of FoM could be 50% from WL and x-ray**



# Conclusions

- EIS cluster counts complementary to primary science drivers
- sensitive in particular to modified gravity
- crucial to understand and control systematic, scatter and scaling
  - next step: simulations to understand selection and optimize method
  - lessons to be learned from surveys like DES
- in particular complementary to other full sky cluster probes
- ‘self-calibration together with Euclid Spectroscopic Survey !