

# New results on the formation of the Moon

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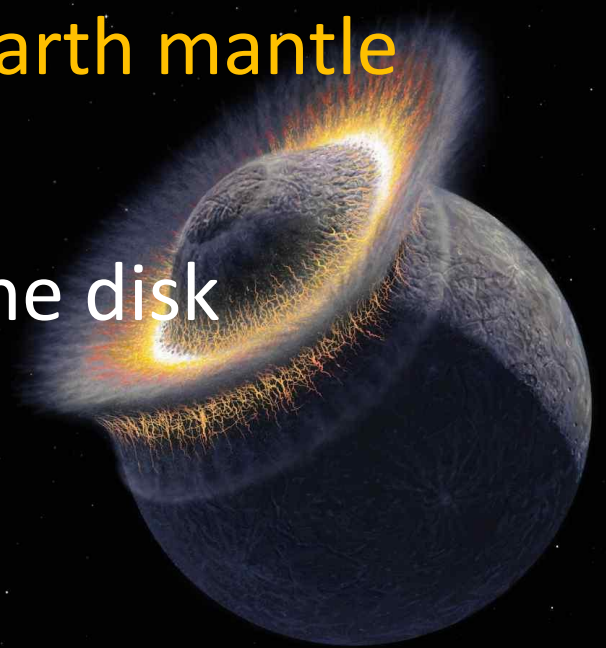
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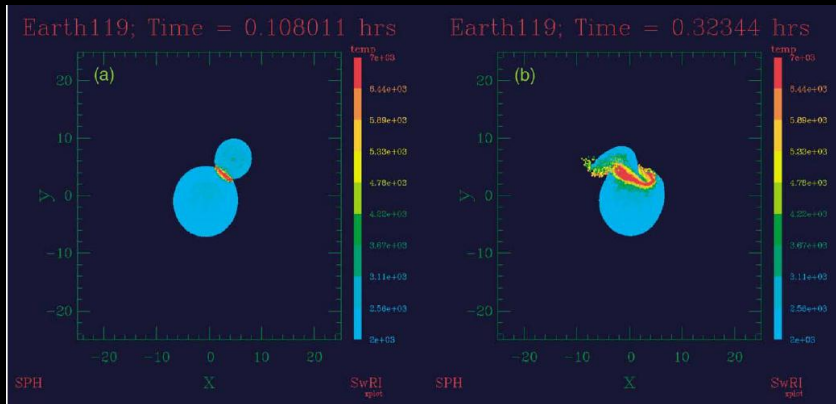
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# Giant impact hypothesis

- Impact of a ~Mars-size object on proto-Earth (Hartmann & Davis 1975 ; Cameron & Ward 1976)
- Formation of a circumterrestrial disk **from impactor debris and ejected Earth mantle**
- Accretion of the Moon from the disk



# Previous work



Giant impact simulations:  
formation of a  $1.5\text{-}2 M_L$  disk  
(e.g. Benz et al. 1986, Canup 2004, 2008)

Moon accretion: **N-body** simulations of protolunar disk (Ida et al. 1997, Kokubo et al. 2000)

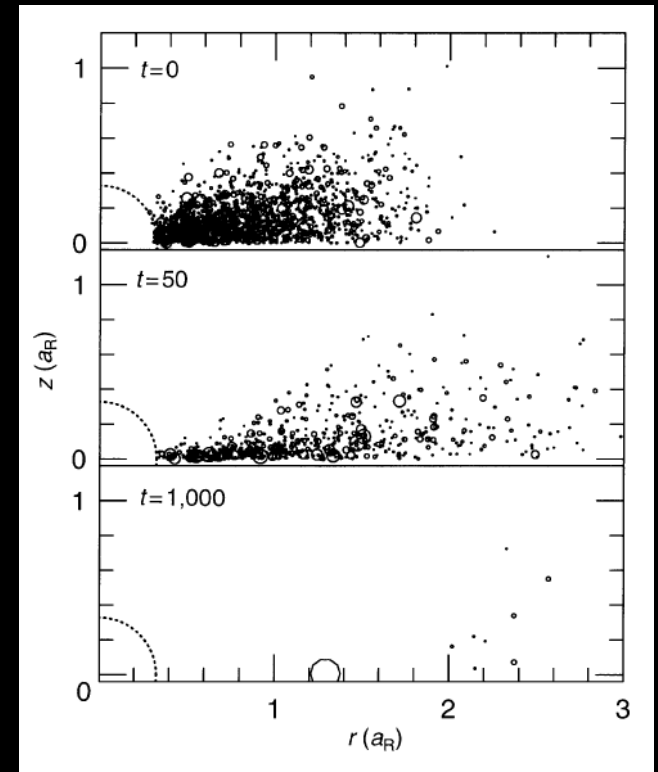
– Accretion of the Moon in **< 1 year**

**BUT...**

– Disk = **mostly impactor debris**

⇒ Earth-Moon isotopic similarities ?

– Such fast accretion implies **completely molten Moon**

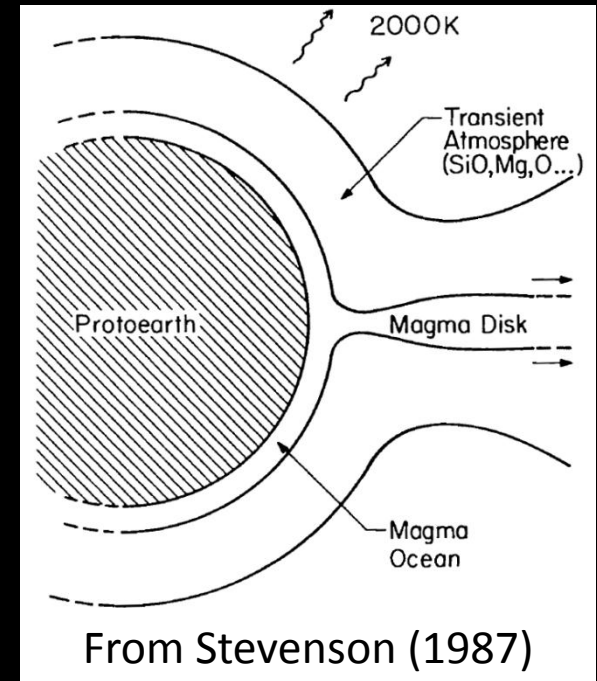


# Issues with pure N-body model

- Within Roche limit: gravitational instabilities + tidal disruption
  - ⇒ high collision rates
  - ⇒ a particle disk would rapidly vaporize
- Post-impact disk is melt + vapor  
≠ individual particles

A more accurate modeling is needed

- Fluid disk within Roche limit
- Disk thermodynamics



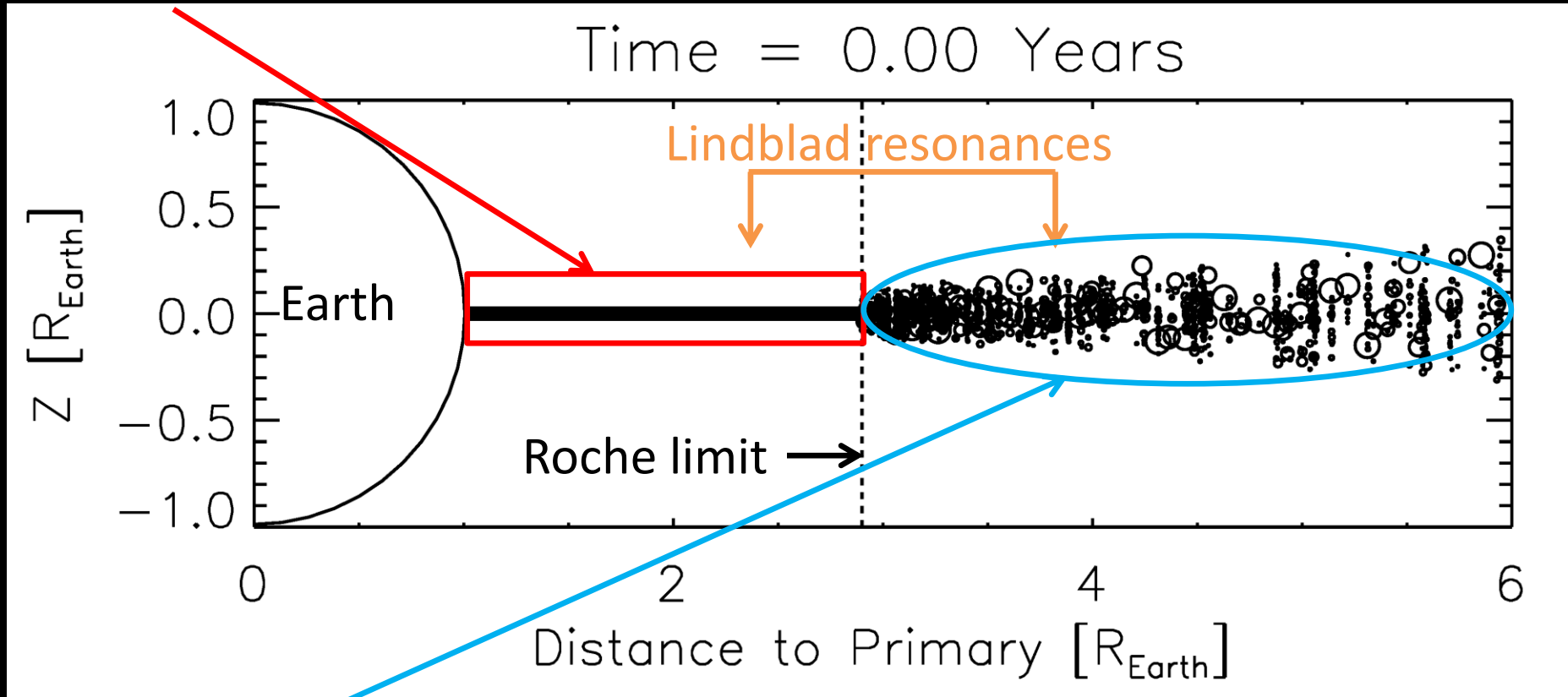
# Question

Dynamics of lunar accretion from a fluid disk?

- Can we still **form a ~ lunar mass** object ?
- Accretion **timescales** ?
- Influence of the disk's **thermodynamics** ?
- Implications for Earth-Moon **isotopic similarities** ?

# Our concept model

within Roche limit: uniform fluid disk



beyond Roche limit : individual particles tracked with N-body code SyMBA

See also Canup & Ward (2000)

# Physical processes

- Roche-interior disk spreads viscously
  - Physically motivated viscosity model  
(Ward & Cameron 1978; Thompson & Stevenson 1988)
  - Disk **loses mass** as it spreads onto planet
  - As material spreads beyond Roche limit, **new moonlets added to N-Body code**
- N-body outer disk: collisions treated with **tidal accretion criteria**
- Inner disk and outer moonlets interact through strongest Lindblad resonances
  - Moonlets orbits **recede away from disk**
  - Inner disk **confined within Roche limit**

# Recycling moonetesimals

- Close encounters between outer moonlets can lead to **scattering toward the Earth**  $\Rightarrow$  tidal disruption

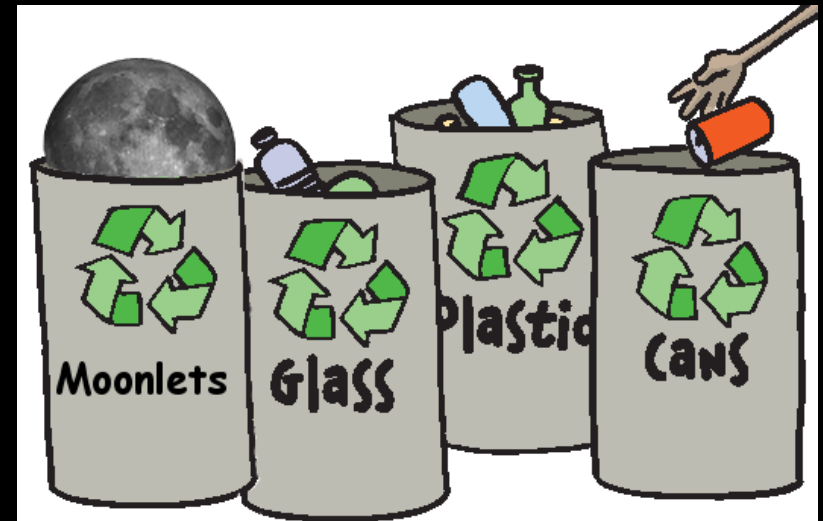
- Tidal disruption criteria

- Mass  $< 10^{-5} M_{\oplus}$

- **Position  $< 2 R_{\oplus}$**

- Body removed from N-body code

- Mass and angular momentum **added to inner disk**





# Initial setups

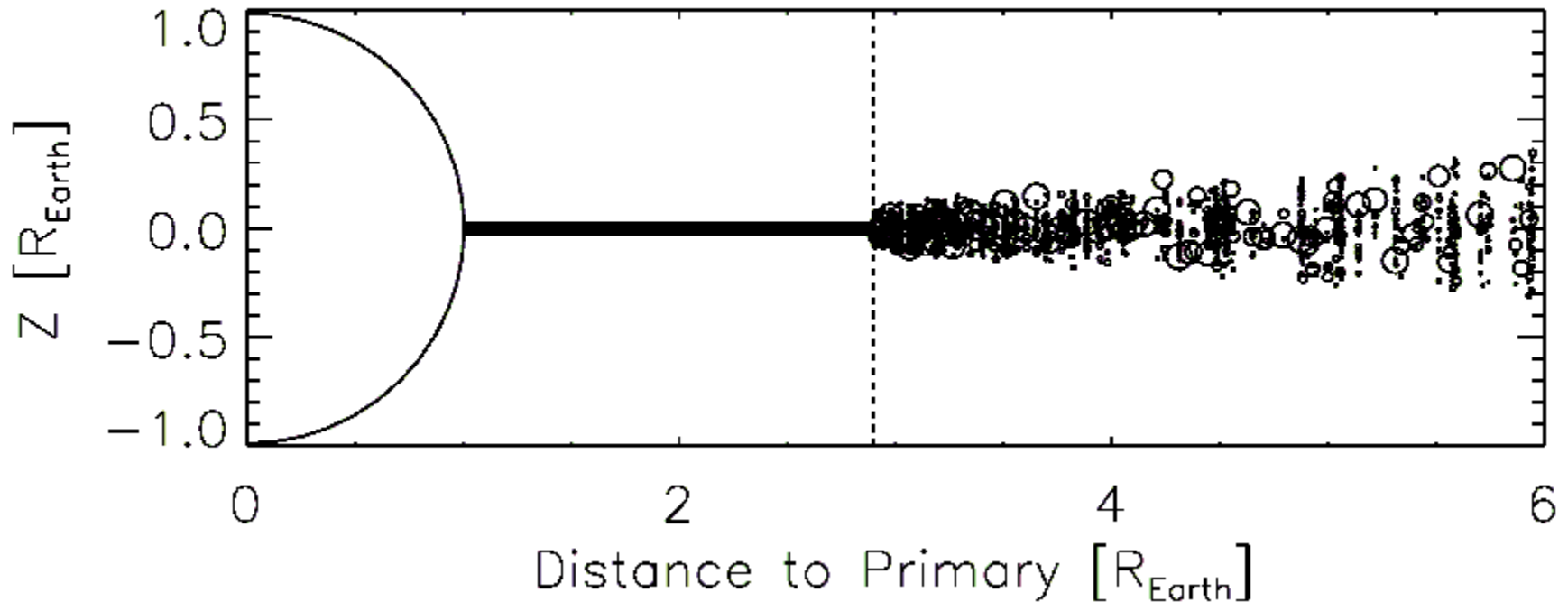
Table 3. Hybrid simulations parameters.

Run	$L_d/M_d$ ( $\sqrt{GM_\oplus/a_R}$ )	$L_d$ ( $L_{EM}$ )	$M_d$ ( $M_\oplus$ )	$M_{in}$ ( $M_\oplus$ )	$M_{out}$ ( $M_\oplus$ )	$q$	$a_{max}$ ( $a_R$ )
1	0.843	0.304	2.00	2.00	0.00	N/A	1
2	0.843	0.365	2.40	2.40	0.00	N/A	1
3	0.955	0.345	2.00	1.00	1.00	5	1.4
4	0.960	0.347	2.00	1.00	1.00	3	1.4
5	0.965	0.348	2.00	1.00	1.00	1	1.4
6	0.955	0.414	2.40	1.20	1.20	5	1.4
7	0.960	0.416	2.40	1.20	1.20	3	1.4
8	0.965	0.418	2.40	1.20	1.20	1	1.4
9	0.899	0.325	2.00	1.50	0.50	5	1.4
10	0.901	0.326	2.00	1.50	0.50	3	1.4
11	0.904	0.326	2.00	1.50	0.50	1	1.4
12	0.899	0.390	2.40	1.80	0.60	5	1.4
13	0.901	0.391	2.40	1.80	0.60	3	1.4
14	0.904	0.392	2.40	1.80	0.60	1	1.4
15	0.888	0.401	2.50	2.00	0.50	5	1.4
16	0.890	0.402	2.50	2.00	0.50	3	1.4
17	0.892	0.403	2.50	2.00	0.50	1	1.4
18	0.880	0.477	3.00	2.50	0.50	5	1.4
19	0.882	0.478	3.00	2.50	0.50	3	1.4
20	0.884	0.479	3.00	2.50	0.50	1	1.4
21	0.986	0.356	2.00	1.00	1.00	5	2.1
22	1.009	0.365	2.00	1.00	1.00	3	2.1
23	1.036	0.374	2.00	1.00	1.00	1	2.1
24	0.986	0.427	2.40	1.20	1.20	5	2.1
25	1.009	0.437	2.40	1.20	1.20	3	2.1
26	1.036	0.449	2.40	1.20	1.20	1	2.1
27	0.914	0.330	2.00	1.50	0.50	5	2.1
28	0.926	0.335	2.00	1.50	0.50	3	2.1
29	0.940	0.339	2.00	1.50	0.50	1	2.1
30	0.914	0.396	2.40	1.80	0.60	5	2.1
31	0.926	0.401	2.40	1.80	0.60	3	2.1
32	0.940	0.407	2.40	1.80	0.60	1	2.1
33	0.900	0.406	2.50	2.00	0.50	5	2.1
34	0.909	0.411	2.50	2.00	0.50	3	2.1
35	0.920	0.416	2.50	2.00	0.50	1	2.1
36	0.890	0.482	3.00	2.50	0.50	5	2.1
37	0.898	0.487	3.00	2.50	0.50	3	2.1
38	0.907	0.492	3.00	2.50	0.50	1	2.1
39	1.068	0.386	2.00	1.00	1.00	1	2.4
40	1.068	0.463	2.00	1.20	1.20	1	2.4
41	0.998	0.361	2.00	1.00	1.00	5	2.8
42	1.043	0.377	2.00	1.00	1.00	3	2.8
43	1.099	0.397	2.00	1.00	1.00	1	2.8
44	0.998	0.433	2.40	1.20	1.20	5	2.8
45	1.043	0.452	2.40	1.20	1.20	3	2.8
46	1.098	0.476	2.40	1.20	1.20	1	2.8

- 46 initial configurations using parameters from impact simulations
  - Total disk mass: 2 to 3  $M_\oplus$
  - Inner disk mass: 50 to 100% of total mass
  - Outer disk edge: 4 to 8  $R_\oplus$
- 1500 initial particles in outer disk

# A typical simulation

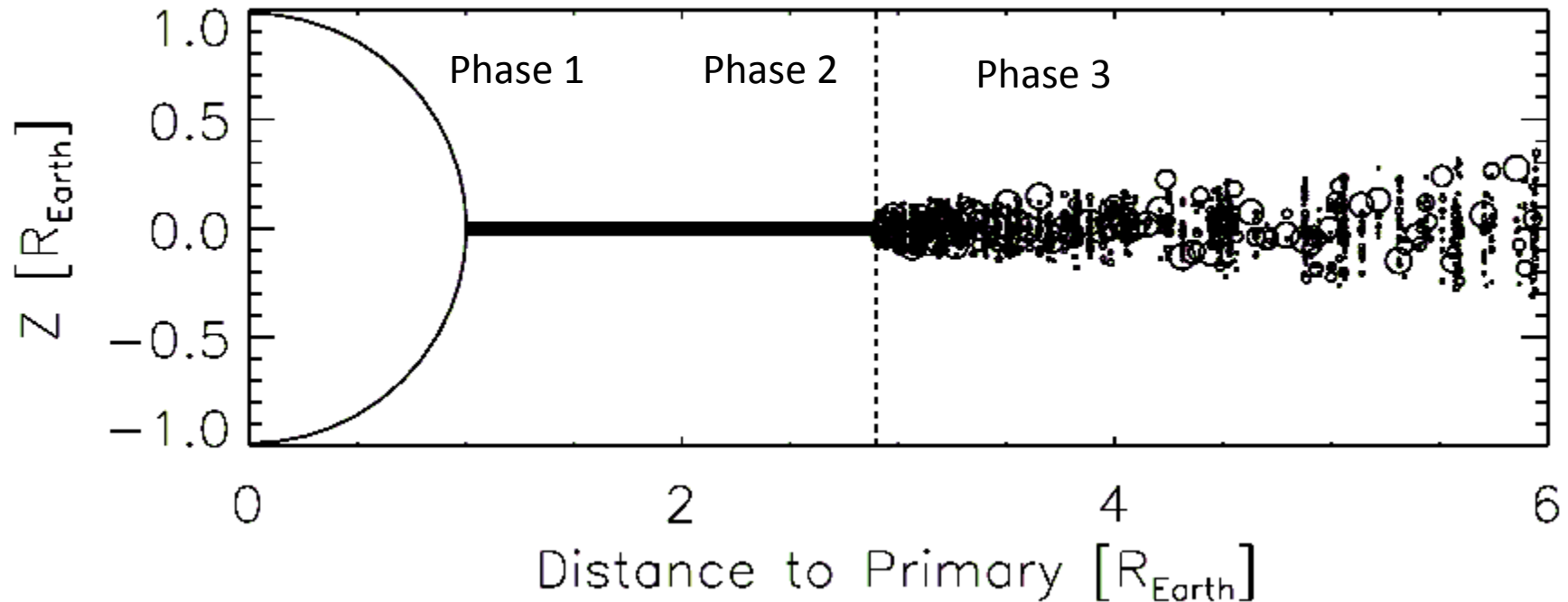
Time = 0.00 Years



- Mass inner disk:  $2 M_L$
- Mass outer disk:  $0.5 M_L$
- Outer edge:  $6 R_{\oplus}$

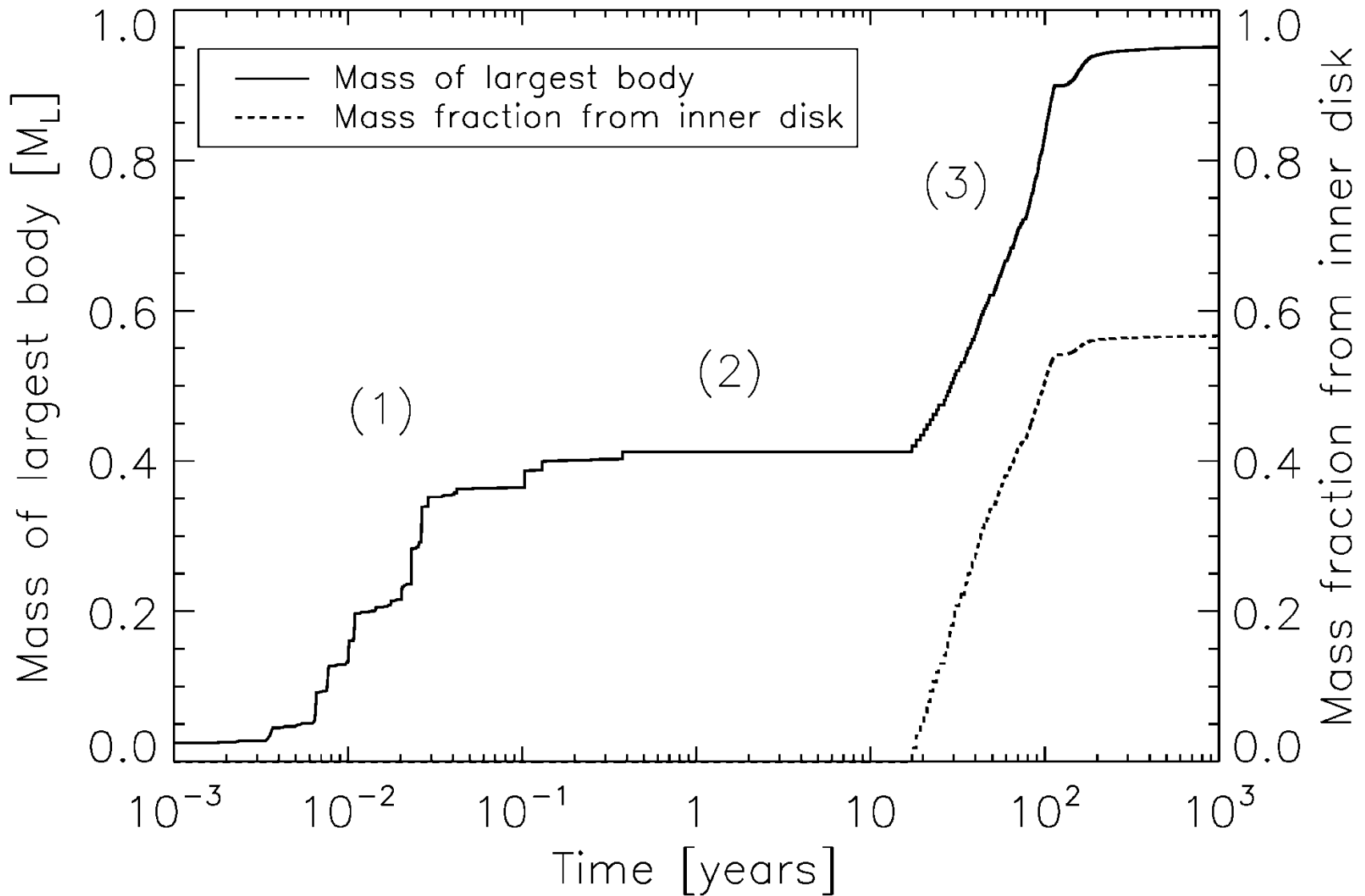
# A typical simulation

Time = 0.00 Years

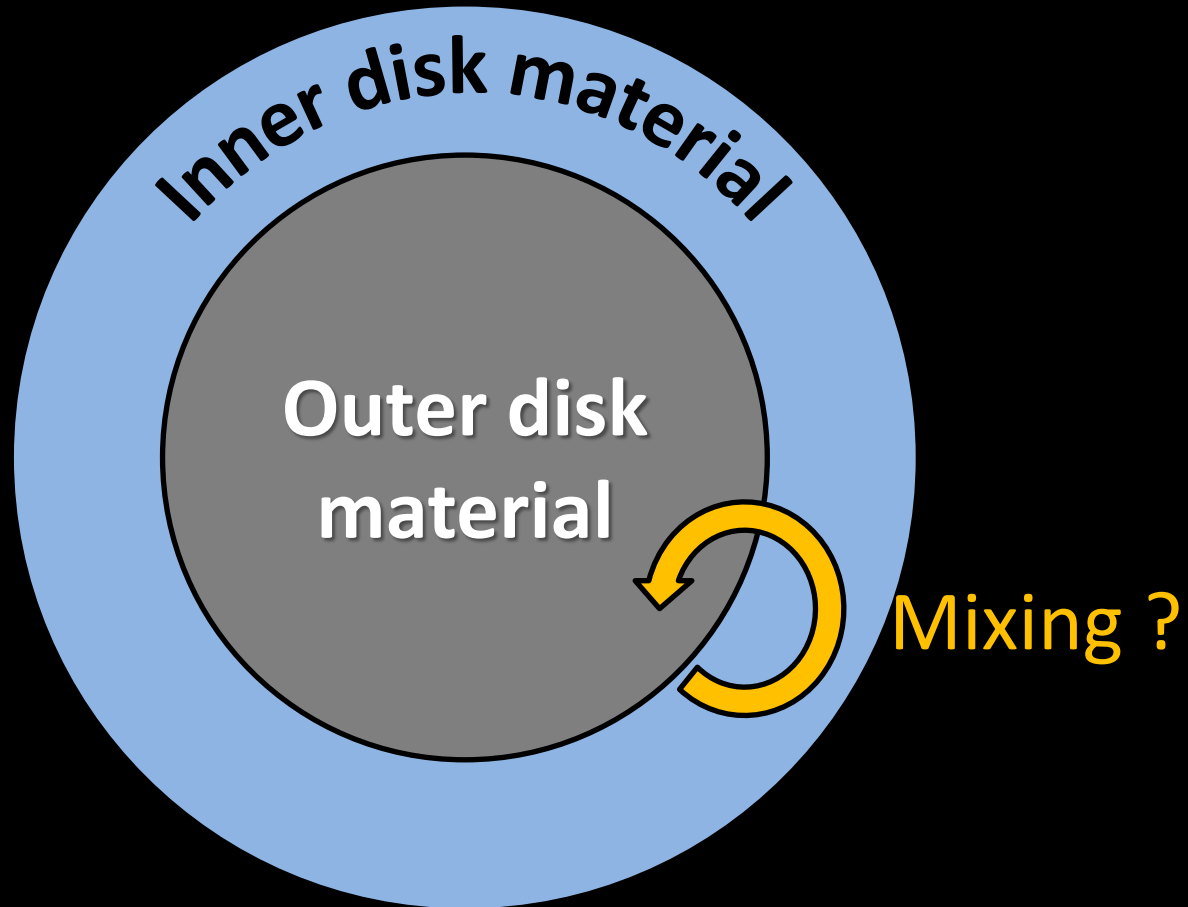


- Phase 1: outer bodies accrete and confine inner disk inside Roche limit
- Phase 2: inner disk slowly viscously spreads back out
- Phase 3: new bodies accrete at Roche limit and continue growth of the moon + serve as relay with inner disk causing moon orbit to expand

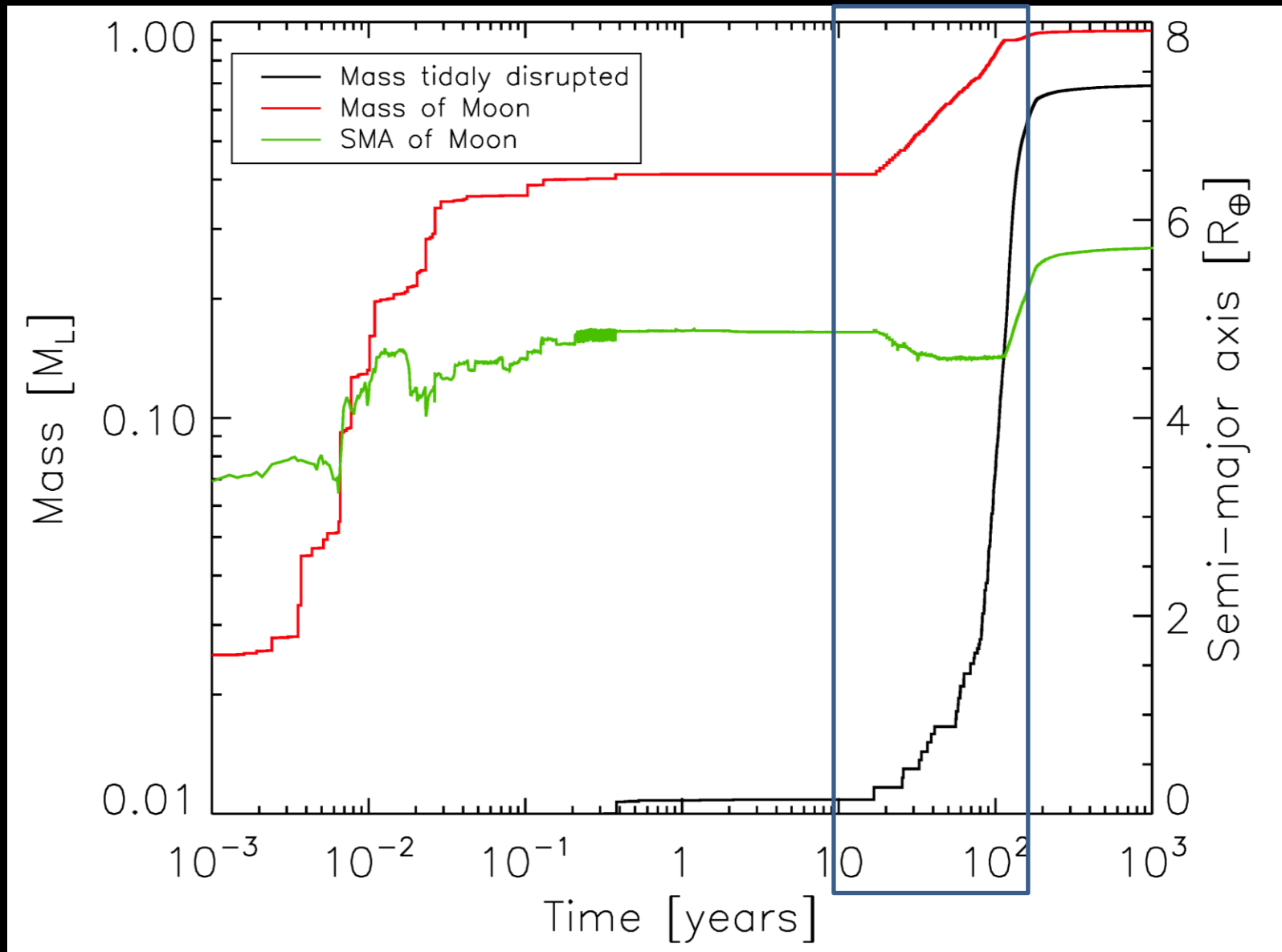
# A long 3-step accretion



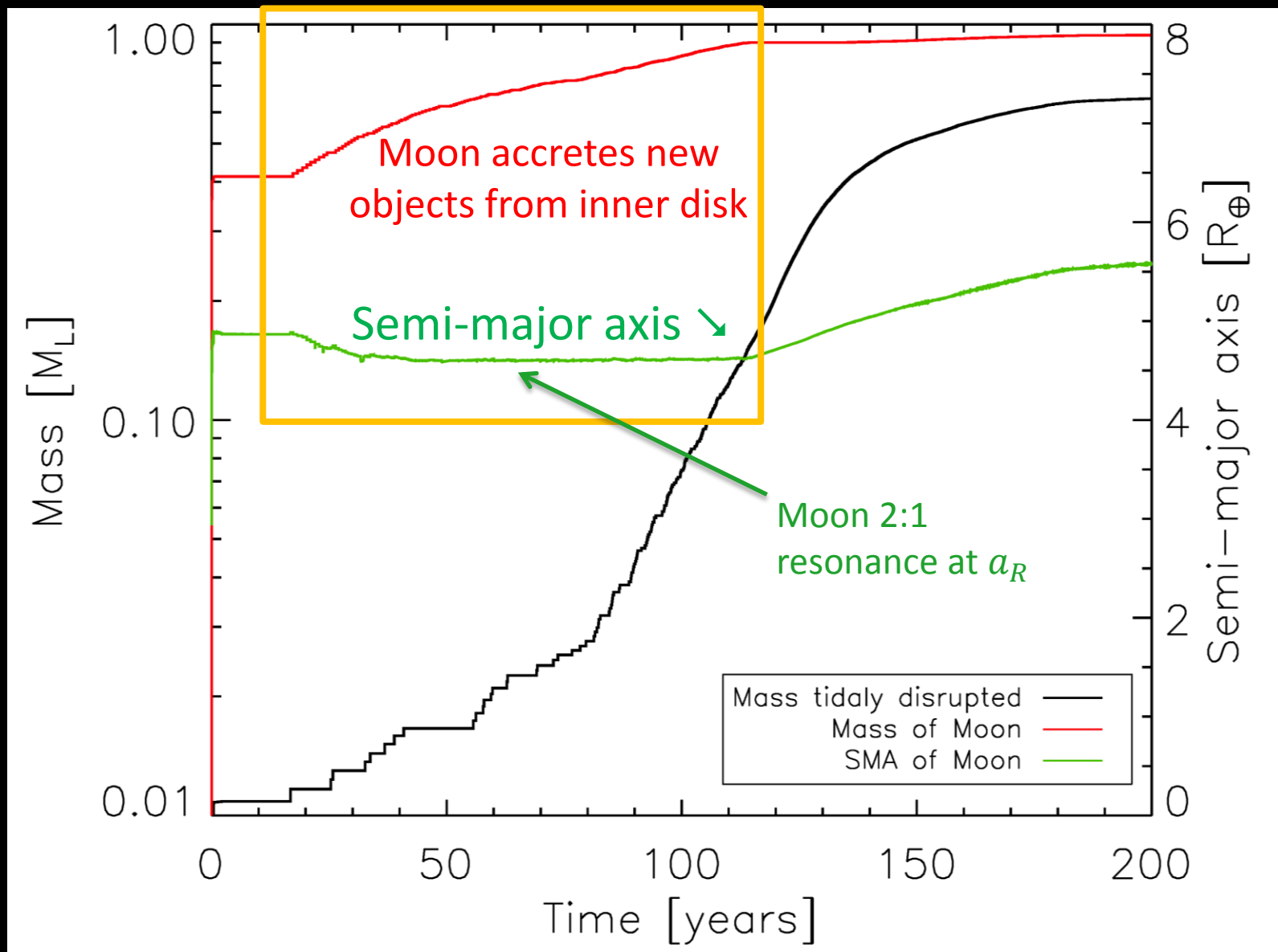
# Resulting Moon structure ?



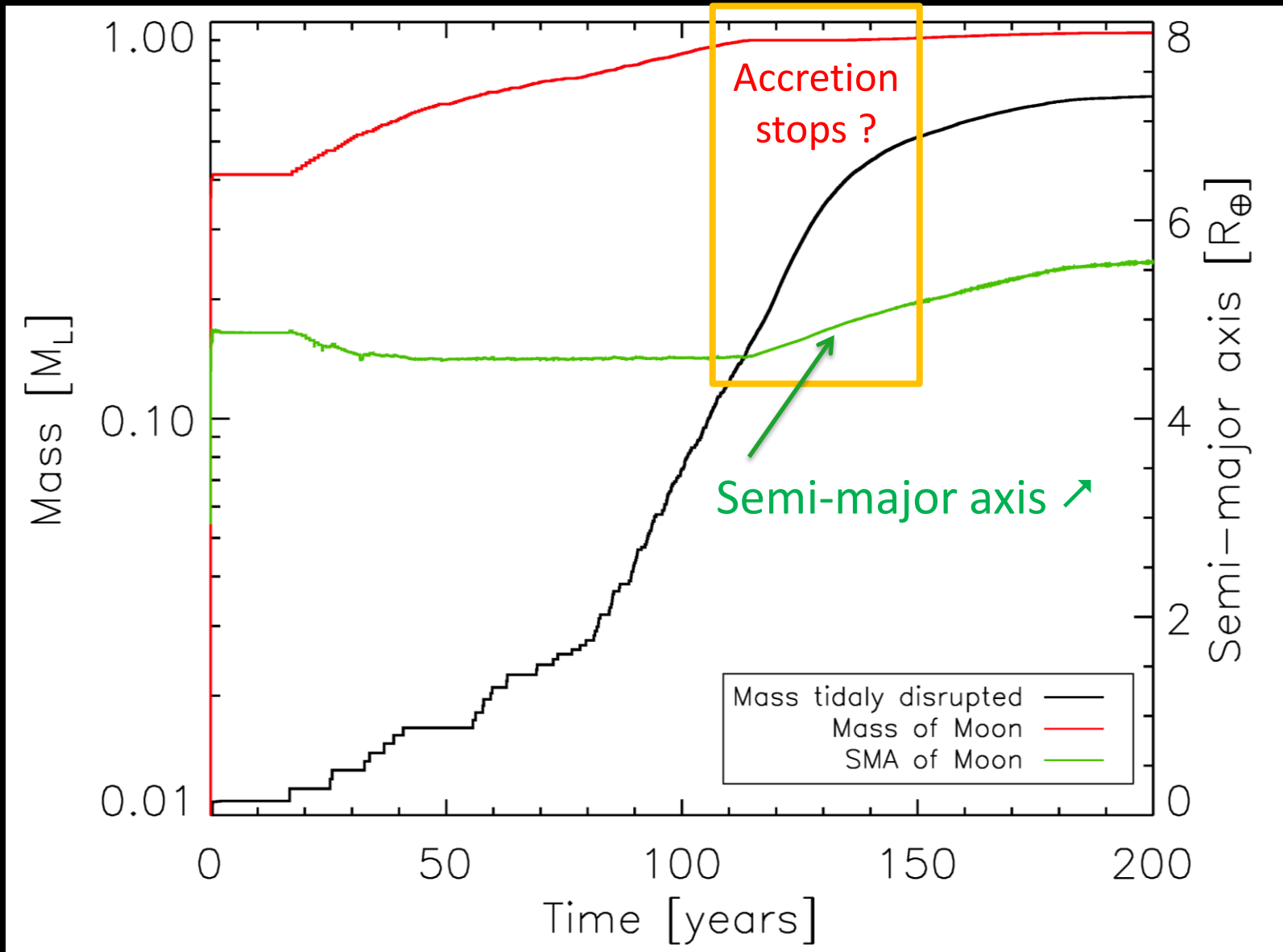
# Moon mass and position



# Moon mass and position



# Moon mass and position





# Conditions for accretion

- To accrete on Moon, bodies spawned at Roche limit must get on moon-crossing orbits

⇒ expand sma and/or increase eccentricity

Disk resonant  
torque

Close encounter  
with Moon

- If particles gets high ecc before sma is expanded
  - Pericenter  $< 2R_{\oplus} \Rightarrow$  Tidal disruption
- Each scattering event leads to increase of Moon semi-major axis (cf. planetesimal driven migration)

# Conditions for accretion

As time goes by:

1. inner disk mass decreases

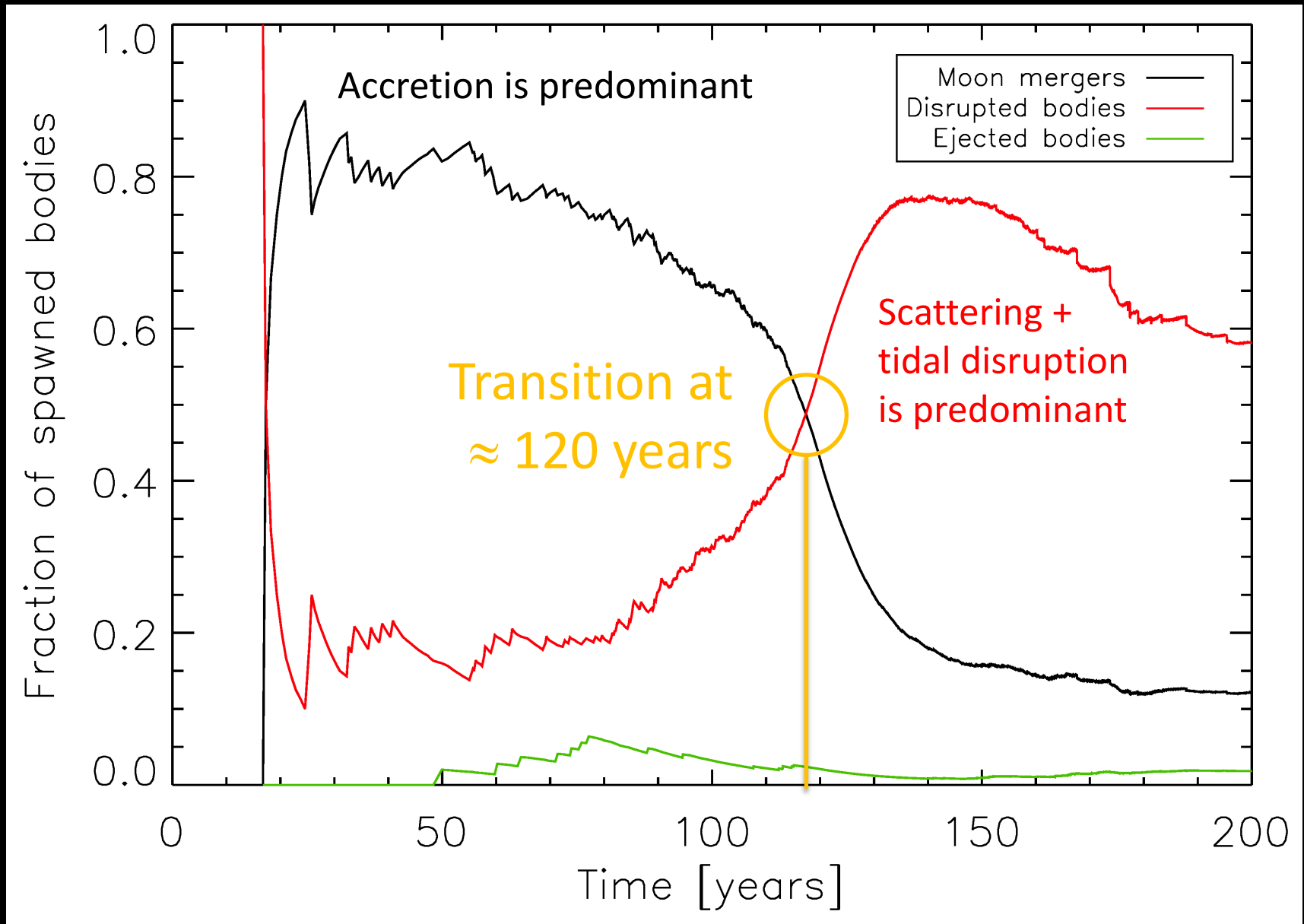
- Resonant torque decreases
- Moonlets sma expansion timescale increases

2. Moon mass increases

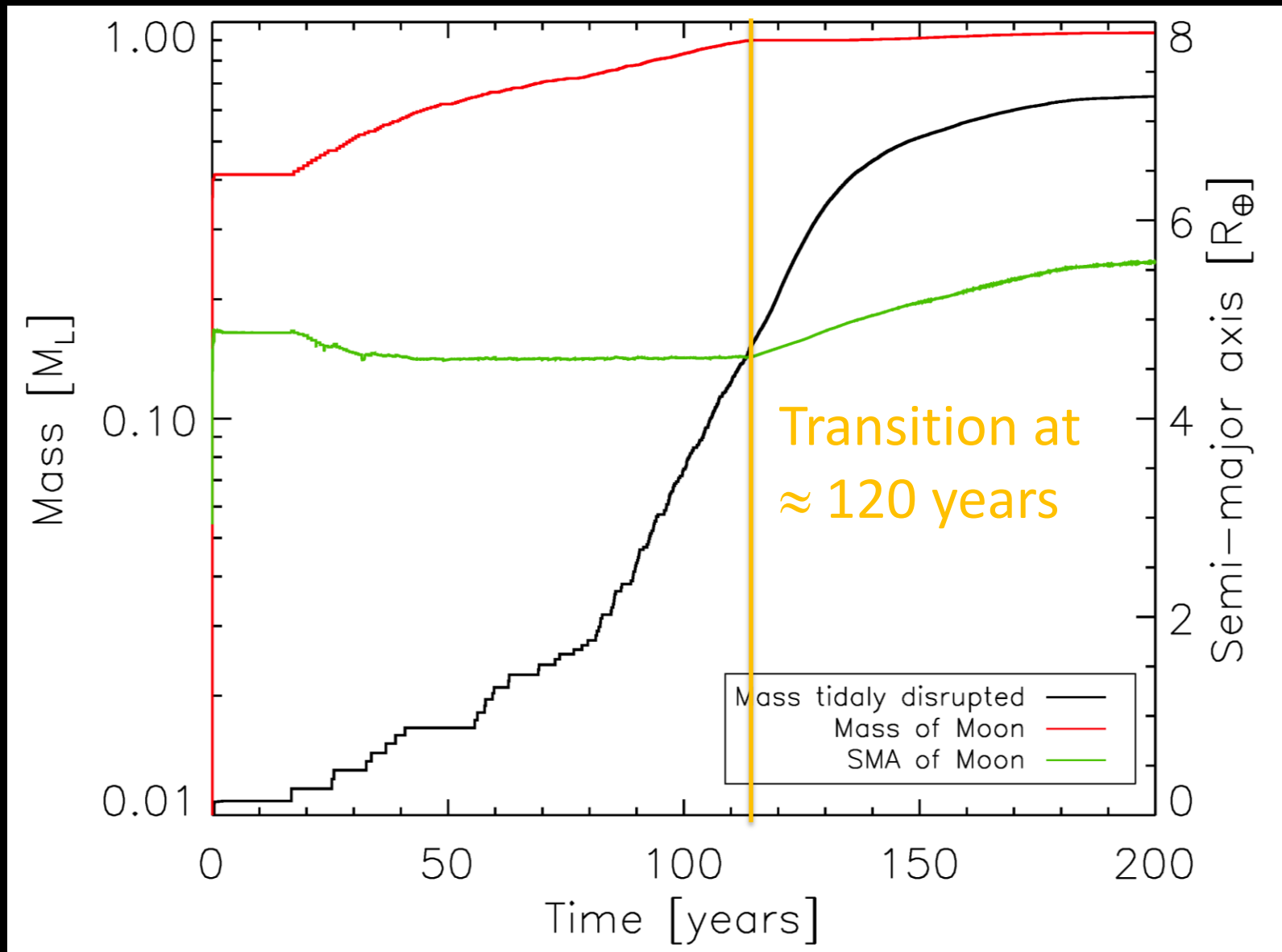
- Scattering efficiency increases
- Moonlets eccentricity excited more rapidly

**It becomes increasingly difficult for new objects to collide with the Moon before being tidally disrupted**

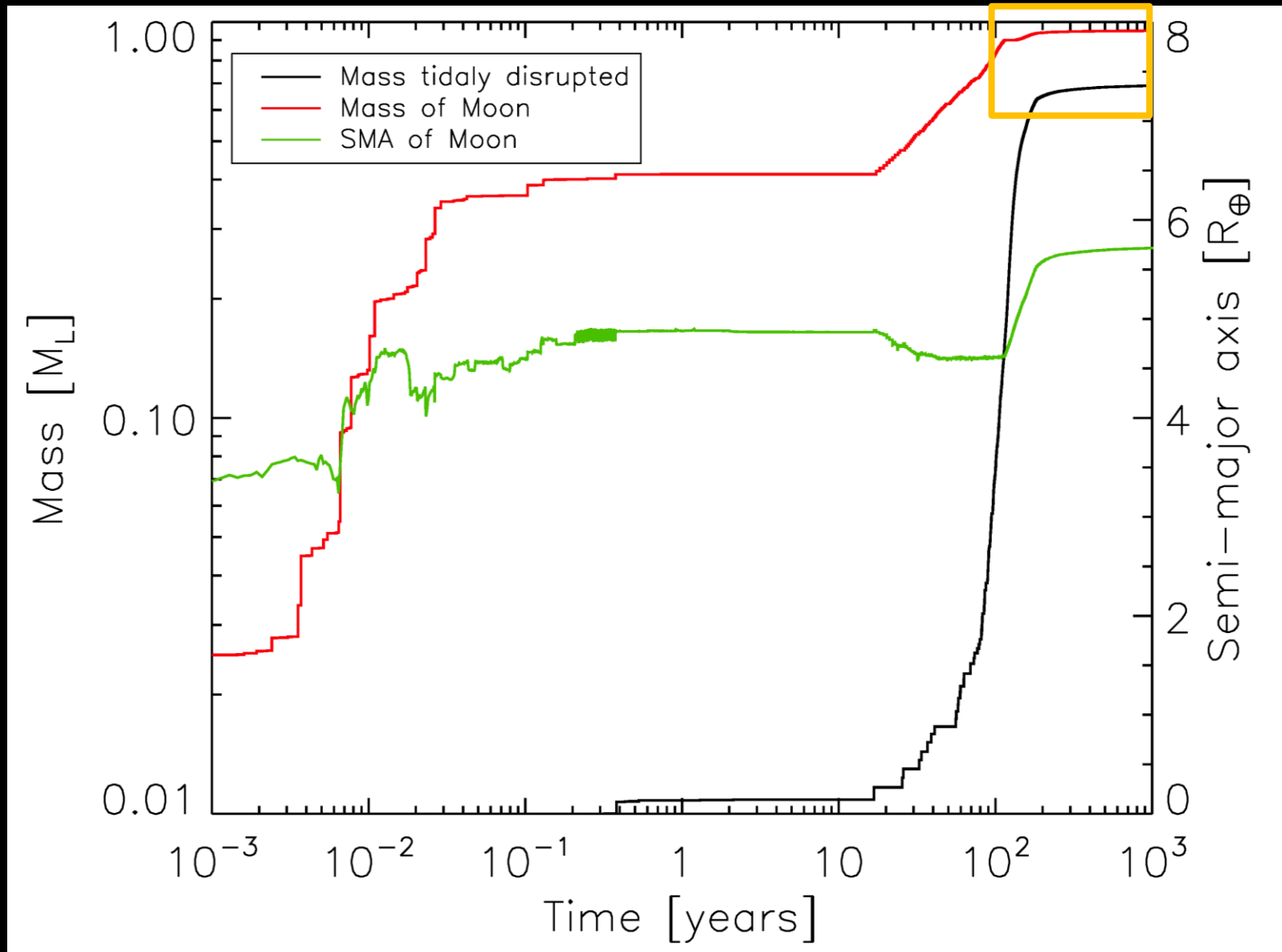
# Fraction of new objects merging with Moon



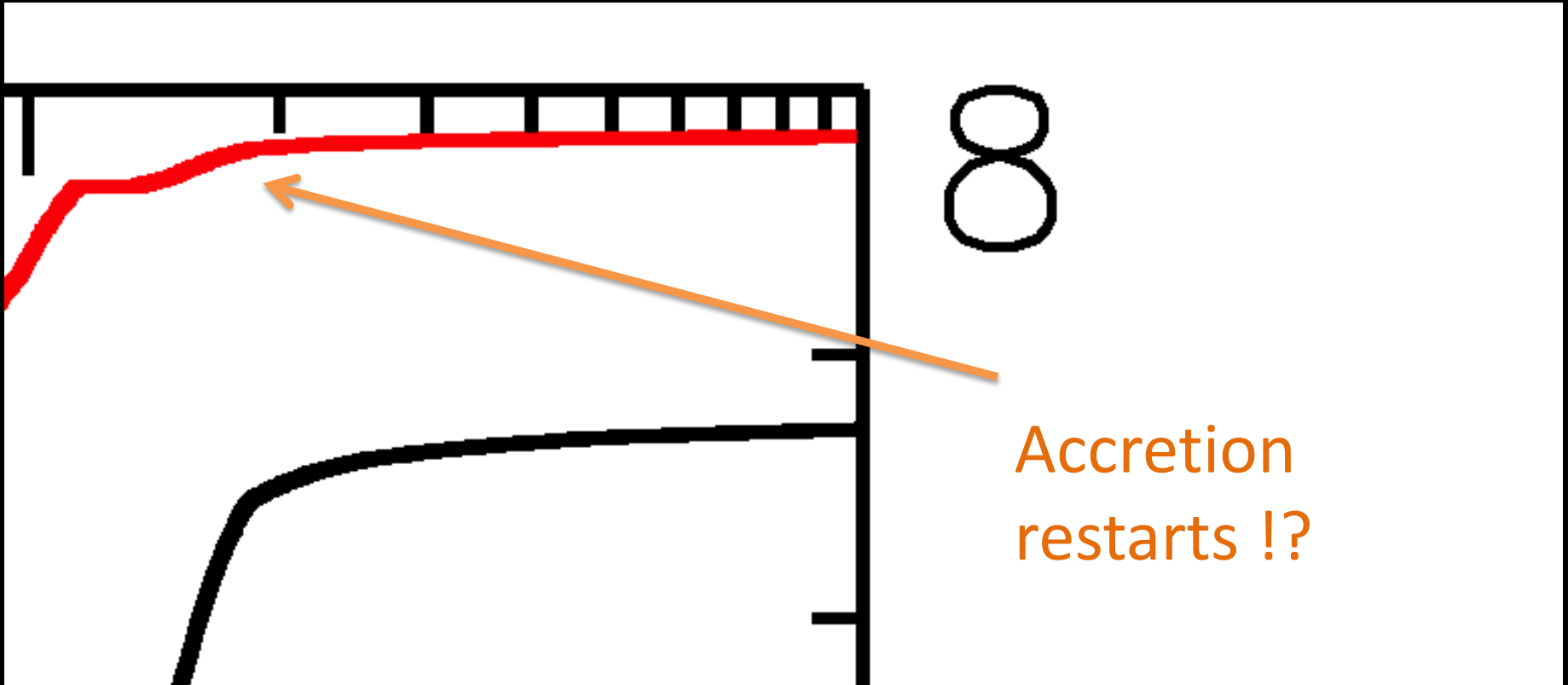
# Moon mass and position



# Late evolution



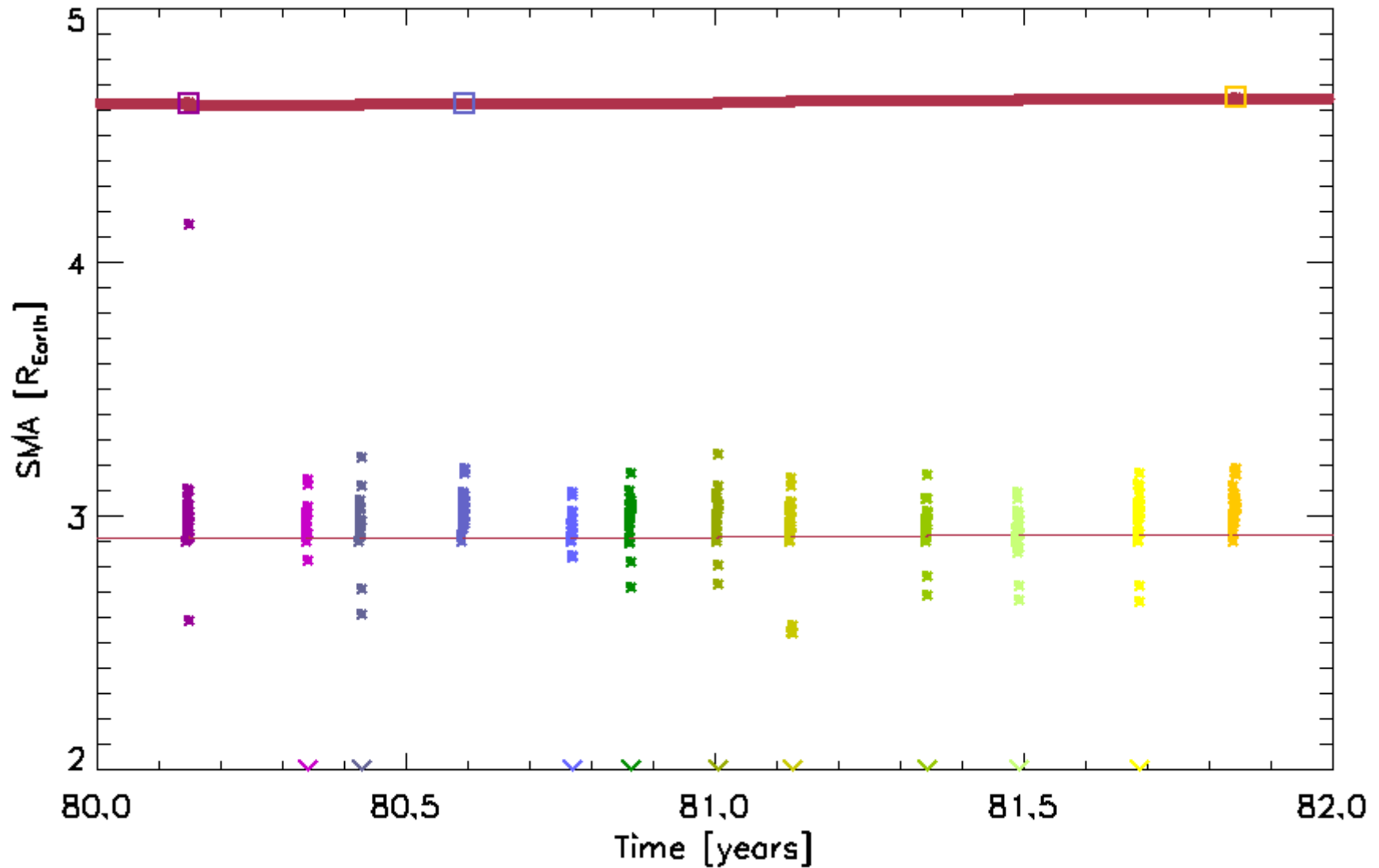
# Late evolution



# Capture in resonance

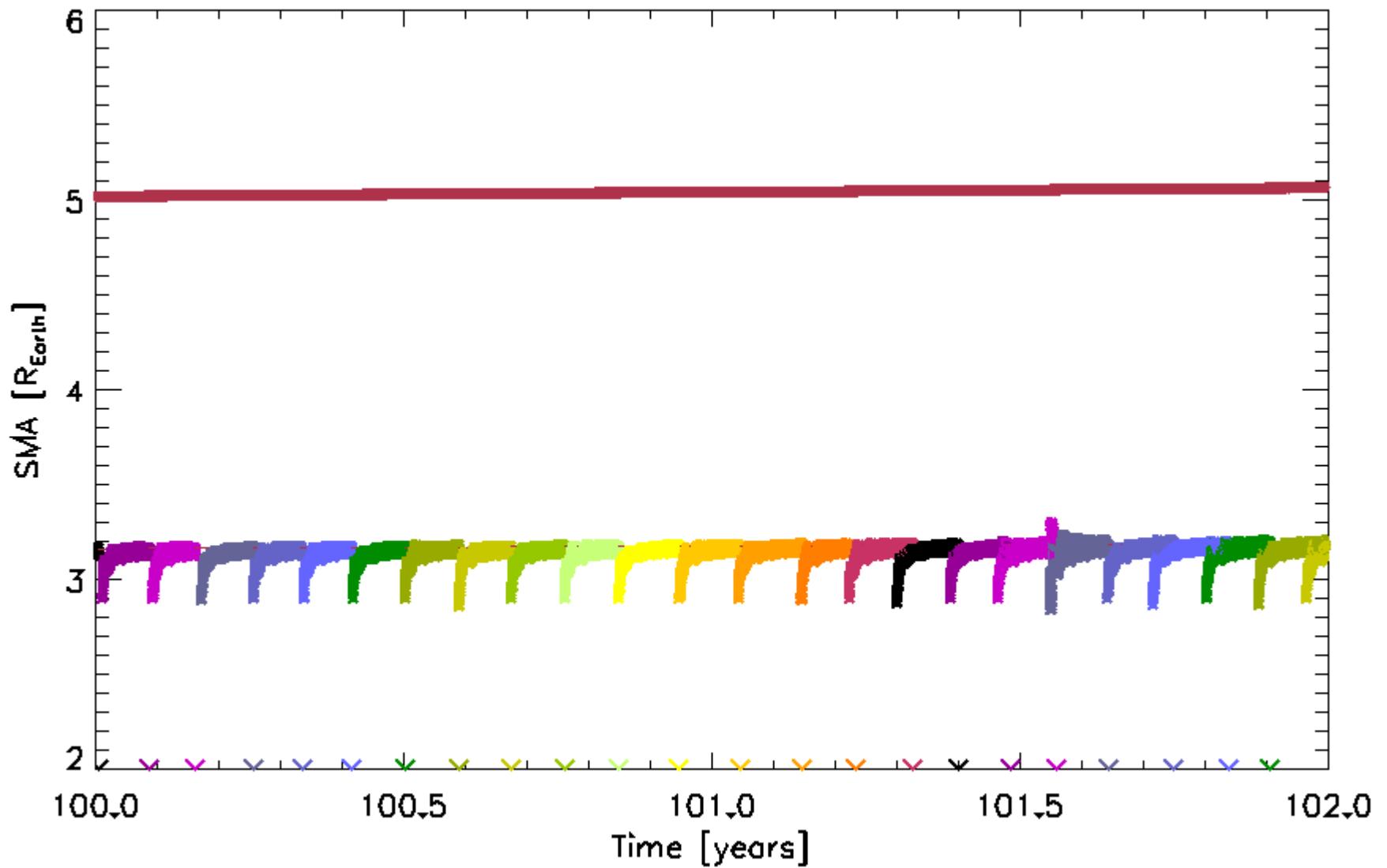
- At end of Phase (1), Moon's 2:1 mean motion resonance lies just outside of inner disk
- First new moonlets move outward rapidly and **cross the resonance**
- Later, disk push less efficient + Moon farther away  $\Rightarrow$  **capture**

# First moonlets cross the resonance

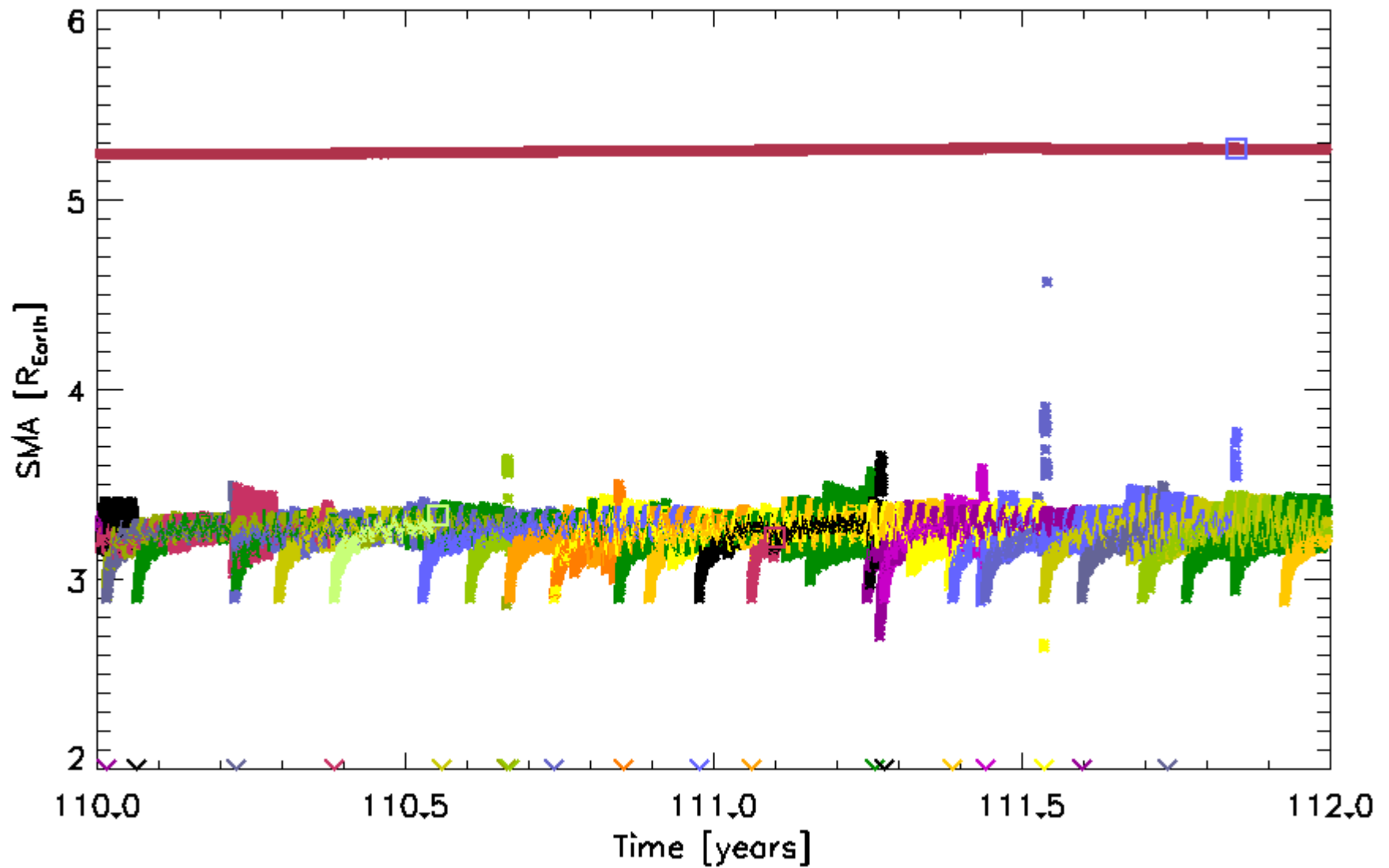




# Capture into resonance



# Ejection from the resonance



# Summary

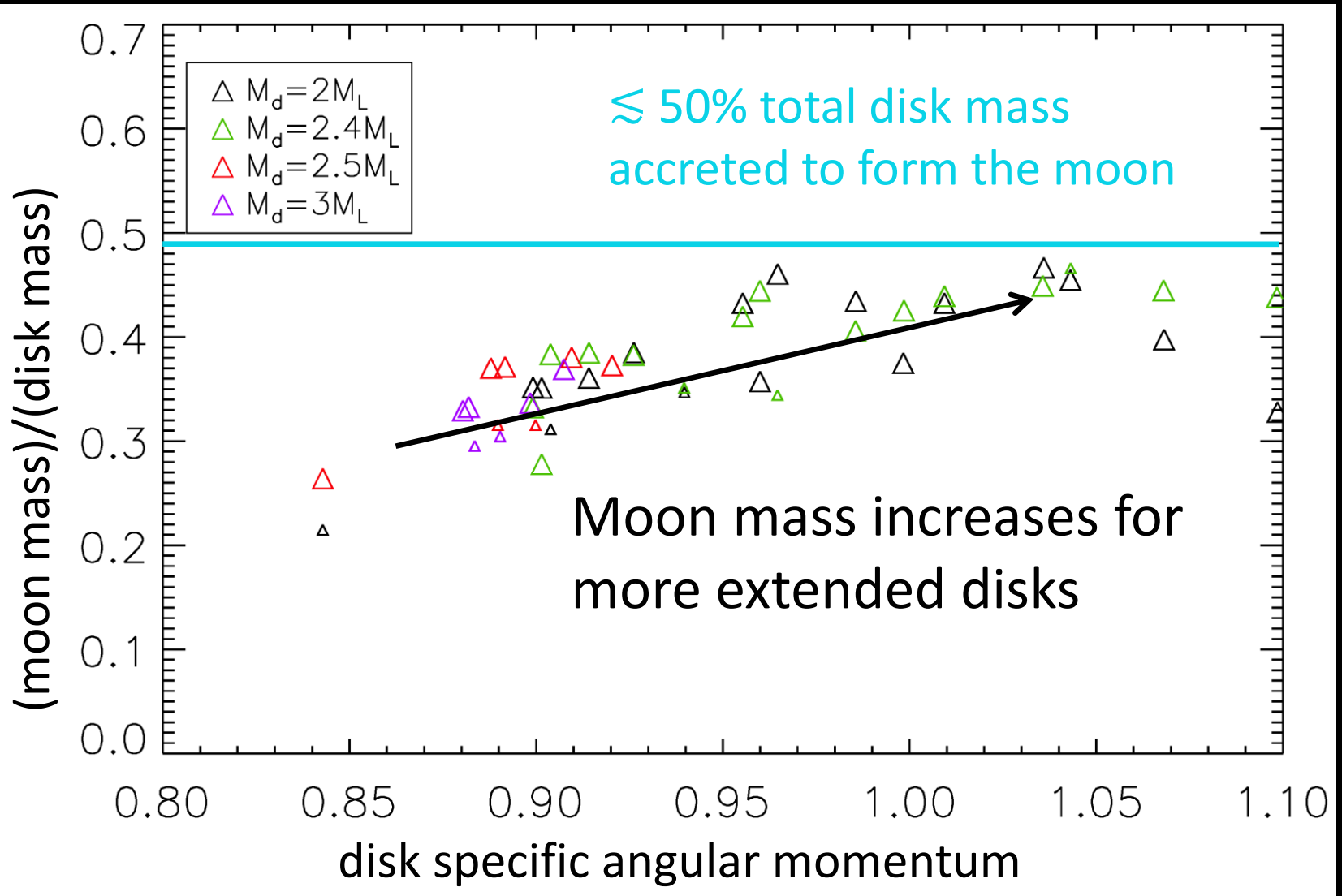
1. Initial outer bodies form a **lunar « core »**
2. New bodies formed at Roche limit **pushed by disk** and accrete on moon
3. Disk push becomes less efficient
  - a. Moonlets scattered inward
  - b. Moon **migrates outward**
4. Moonlets get **captured into moon resonance**
  - a. Scattering continues
  - b. moonlets **ejected from resonance** through mutual interactions can accrete on moon

# Global results

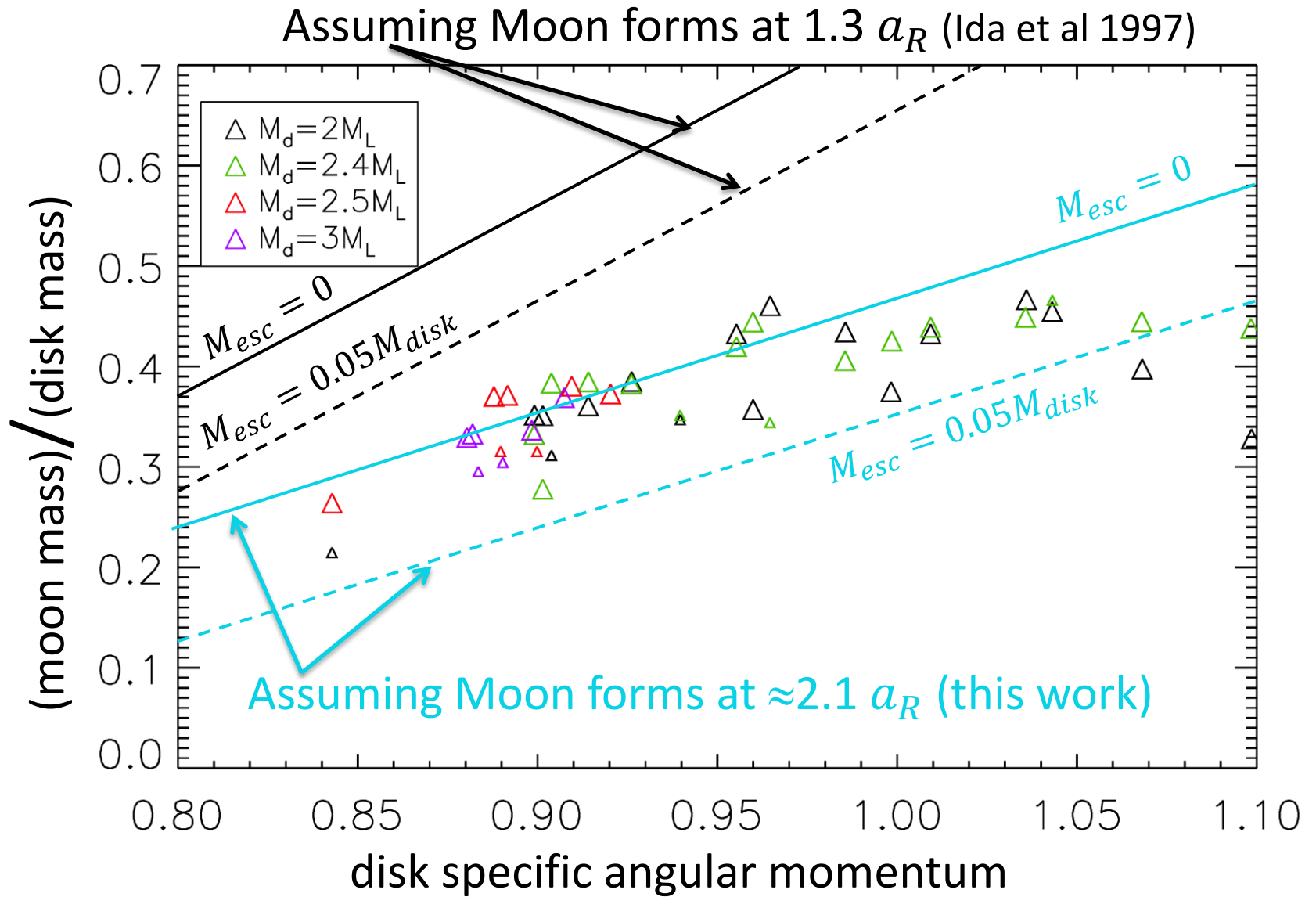
Average moon properties at  $t=1000$  years

- Mass:  $0.81 \pm 0.21 M_L$
- Semi-major axis:  $2.15 \pm 0.3 a_R$ ,  $> 1.3 a_R$  in N-body
- Accretion timescale  $\sim 10^2$  years,  $\gg 1$  year in N-body
- Mass fraction of inner disk material: 5 to 65%

# Moon mass Vs. disk specific angular momentum

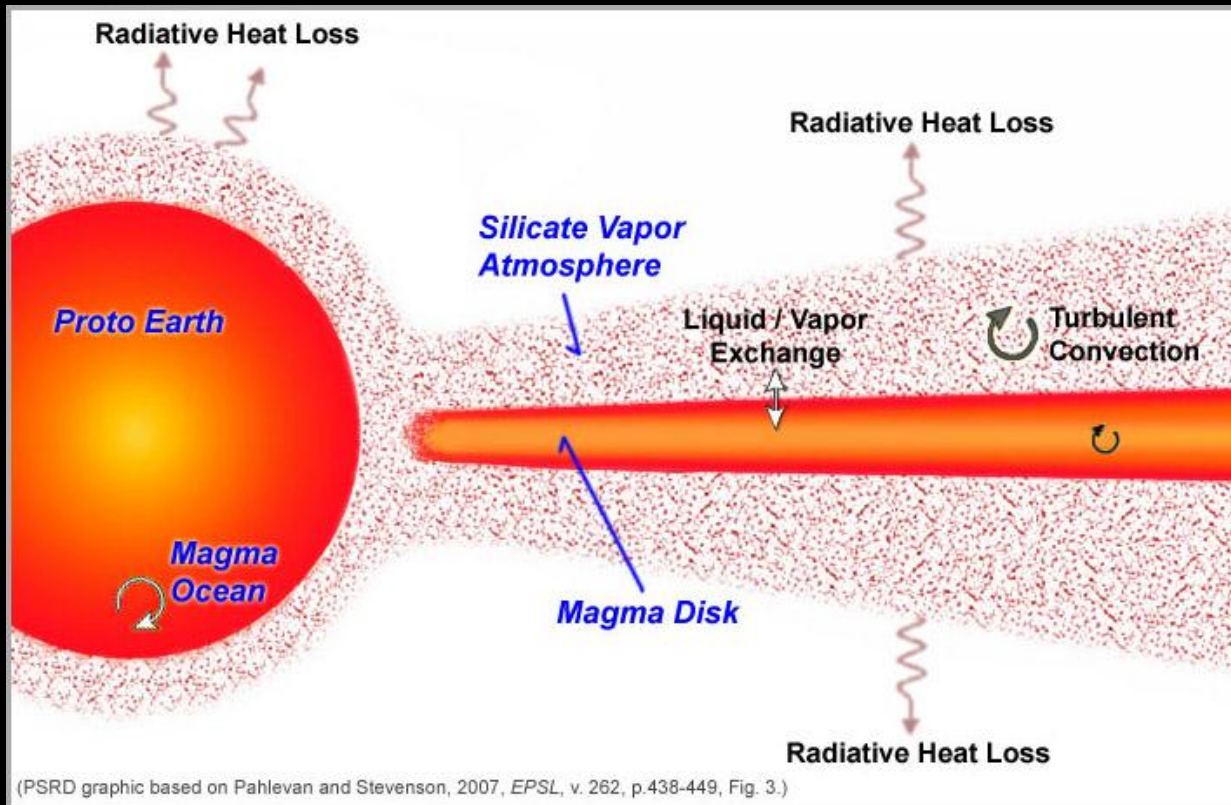


# Analytical estimates



# Equilibration

- Earth and Moon share striking **isotopic similarities** (O, Ti, W, ...)
- Impact simulations: disk is mostly **impactor material** ≠ Earth ?



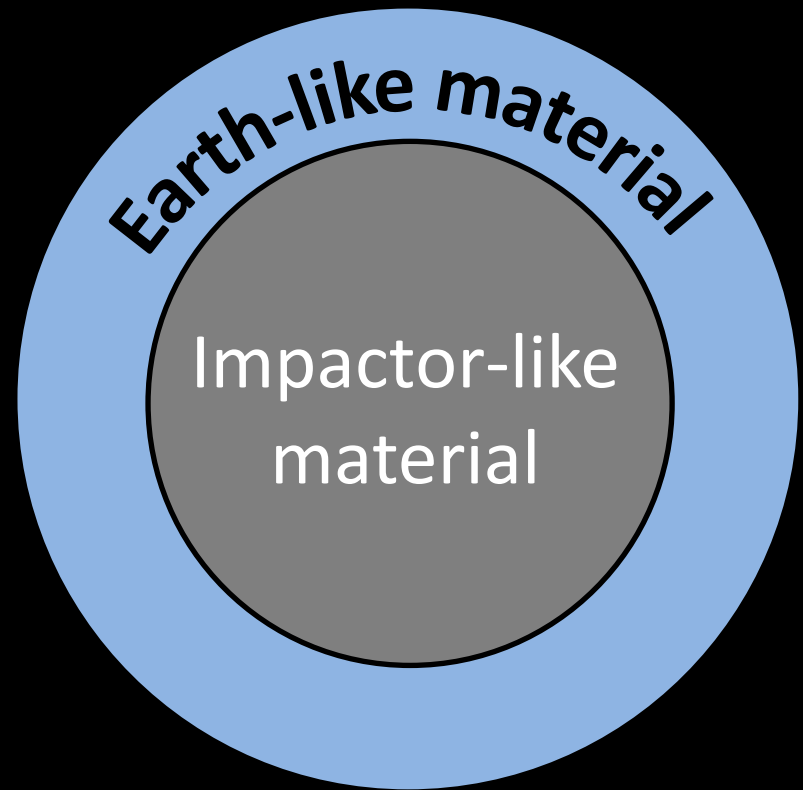
- **Material exchange** between Earth and disk's atmospheres
- Compositional equilibration in **~100-1000 years** (Pahlevan & Stevenson 2007)

# What our results imply

- Accretion timescales  $\sim 200$  years  
 $\Rightarrow$  compatible with estimated equilibration timescales
- 3-steps accretion: “Earth-like” material accreted last

A  $1 M_L$  object with 60%  
inner disk material  
 $\Rightarrow \sim 460\text{km-deep}$   
“Earth-like” outer layer

Mare basalts estimated to  
have formed at  $\sim 500\text{km}$





# Conclusion

Consideration of a fluid inner disk drastically changes the dynamics of Moon accretion

- 3-stage accretion
- Longer timescales  $\sim 200$  years
- Moon forms farther away

Accretion limited by confinement of inner disk + scattering/capture in resonance of moonlets

Positive implications regarding isotopic similarities

Paper submitted to ApJ

# Future work

- Full hydro simulation of the inner disk (e.g. Charnoz, Salmon & Crida 2010)
- Improved inner disk model from recent theoretical studies (Ward 2012)
- Further explore the range of initial parameters



# Full Moon

29.01 sábado  
Duro Beach Hotel